High quality-factor space-time metasurface for free space power isolation at near-infrared regime

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Abstract. Space-time metasurfaces are promising candidates for breaking Lorentz reciprocity that constrains light propagation in numerous practical applications. There is a substantial difference between carrier and modulation frequencies in space-time photonic metasurfaces that leads to negligible spatial pathway variation of light and weak nonreciprocal response. To surmount this obstacle, herein, design principle of a high quality-factor space-time gradient metasurface is demonstrated at near-infrared regime that increases the lifetime of photons and allows for strong power isolation by lifting the adiabaticity of modulation. The all-dielectric metasurface consists of an array of silicon subwavelength gratings (SWGs) that are separated from distributed bragg reflector by a silica buffer. The resonant mode with ultrahigh quality-factor exceeding $10^4$ is excited within the SWG, which is characterized as magnetic octupole and features strong field localization. The SWGs are configured as multijunction p-n layers, whose multigate biasing with time-varying waveforms enable modulation of carriers in space and time. The proposed nonreciprocal metasurface is exploited for free space optical power isolation by the virtue of modulation-induced phase shift. It is shown that under time-reversal and by interchanging the directions of incident and observation ports, power isolation of $\approx 35$ dB can be maintained between the two ports in free space.

Keywords: Space-time metasurface, high-$Q$ resonator, Optical nonreciprocity, Active photonic platform.

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1 Introduction

Metasurfaces, two-dimensional and planar arrays of subwavelength scatterers are of particular interest for sculpting the wavefront of light through imprinting local space-variant abrupt phase discontinuities to the incoming wavefronts. They have demonstrated unprecedented capability in a wide range of applications such as anomalous reflection, pulse shaping, polarization control, and beam focusing. The ultrathin and compact footprint of the metasurfaces as well as their great fabrication feasibility have held them a notable promise for optical component miniaturization and on-chip integration. The initial efforts toward the development of metasurfaces employed passive scatterers, whose optical responses are controlled by tailoring their geometrical parameters. The static nature of passive metasurfaces specifies their application to the initial functionality that they were designed for and ties the post-fabrication tunability of their optical response.
Many emerging applications including light detection and ranging (LiDAR), optical communication, augmented/virtual reality (AR/VR), and imaging, call for a new class of metasurfaces with the capability of achieving versatile dynamic response to shape the wavefronts at will.

An immense effort has been devoted to realizing active metasurfaces through dynamic manipulation of their constituent building blocks. Different stimulation mechanisms have been used to alter the resonant properties of the unit cells by triggering the refractive index of active material integrated into the metasurface or mechanically reconfiguring the dimension or position of the individual unit cells. In particular, electrical gating, optical pumping, thermal annealing, and current-induced heating can be employed for this purpose. Thus far, quantum-confined Stark effects in multiple quantum wells (MQWs), molecular phase transitions in vanadium dioxide (VO$_2$) or germanium antimony telluride (GST), reorientation of molecules in liquid crystals (LCs), ionic transparent, and carrier-induced field effects in semiconductors i.e., silicon (Si), gallium arsenide (GaAs), transparent conducting oxides (TCOs), indium arsenide (InAs), and atomically thin transition metal dichalcogenides (TMDCs), have been leveraged for index modulation. Among these tuning mechanisms, the free carrier-induced effects in doped semiconductors have yielded a great promise for active tuning thanks to higher modulation frequencies (up to several GHz), continuous tunability, and lower power consumption compared to techniques based on the Pockels effect or waveguide modulators based on lithium niobate. One major obstacle toward application of this method is the negligible strength of electro-refraction that occurs within a nanometer-thin active layer and results in small refractive index modulation. To partly surmount this challenge, dual-gated biasing technique has been proposed, which enhances the mode overlap with the active region by increasing the volume of the accumulation/depletion layers. In addition, the background doping density in semiconductors such as TCO, and InAs can
be judiciously adjusted such that the epsilon near zero (ENZ) phenomenon takes place within the active regions, resulting in strong electric field confinement and large tunability of the optical response. Increasing the light-matter interaction through careful design of the metasurface platform is an alternative method to achieve large amplitude/phase modulation at the output. Transitioning the resonant mode between the over- and under-coupled regimes, employing the Kerker’s resonators with two degenerate modes, or utilizing the resonators with ultrahigh Quality-(\(Q\)-)factor for increasing the life time of photons can be used to strengthen the mode overlap with the active tunable medium and yield strong light-matter interaction.

The free carrier-induced field effect in moderately doped semiconductors such as Si offers the ability to alter the refractive index within the entire material volume rather than being limited to the ultrathin accumulation/depletion layers. This can be maintained by configuring the host Si resonator into p-i-n/p-n junctions through doping the horizontal/vertical directions. Nevertheless, the maximum attainable refractive index change in such semiconductors is small and typically on the order of \(10^{-3} - 10^{-2}\) at near-infrared (NIR) regime, which hinders wide modulation of light due to the small spectral shift of the resonance. As such, a proper design paradigm with an ultrahigh \(Q\)-factor should be implemented to enhance the field confinement and lifetime of photons within the resonator. Thus far, several structures are proposed for increasing the light-matter interactions at nanoscale level. In particular, the widely used methods for the realization of high \(Q\)-factor modes are built upon the Fabry-Pérot cavity resonators, whispering gallery mode platforms, and guided mode resonators. More recently, the concept of bound states in the continuum (BICs) has triggered an extensive attention, since it is capable of yielding the \(Q\)-factor up to \(10^8\) in extended systems such as photonic crystal slabs or plasmonic and dielectric metasurfaces. Although for any platform comprising of regular materials, where the permittivity and
permeability are neither zero nor infinite, BICs can only be excited if the dimension is infinite, by modifying the parameters of a finite system to follow its infinite counterpart, quasi-BICs (QBICs) can be supported. Despite the ultrahigh $Q$-factor that ensures large change in the optical response of the resonators in response to the index modulation, they cannot be employed for designing the gradient metasurfaces. This is because the index contrast between the neighboring elements of the phase gradient metasurfaces leads to the emergence of epsilon-QBIC mode in systems with a broken symmetry in their permittivity.\textsuperscript{47} An alternative promising technique to boost the $Q$-factor of a resonator is engineering its dimension to support higher-order Mie resonances.\textsuperscript{48} Similar to their dipolar counterparts, the higher-order Mie modes leverage the confined field distribution that enables local wavefront manipulation, while featuring sufficiently high $Q$-factor that is obtained thanks to the reduction of radiative losses. Such characteristics make them great candidates for designing dynamically tunable phase gradient metasurfaces with wide modulation range of the scattering properties, while the refractive index modulation remains negligible.

Despite the fruitful progress, the performance of the phase gradient metasurfaces are constrained by Lorentz reciprocity. It is desired to break the reciprocity in order to achieve full-duplex communication for increasing the link capacity,\textsuperscript{49–51} power isolation, and circulation\textsuperscript{52–55} that have vital importance for optical communication, laser feedback systems, nonreciprocal waveguide walls, nonreciprocal quantum state mediation, illusion cloaks, Faraday isolators, and power dividers.\textsuperscript{56–59} Magneto-optical effects have been traditionally used for breaking the reciprocity by imparting a different momentum over the waves propagating in forward and backward directions. In this case, the permittivity tensor of the magneto-optic material exhibits a nonsymmetric response upon applying the DC magnetic field.\textsuperscript{60} However, these materials are lossy and bulky that prohibit them from being integrated to the photonic circuits. Alternatively, space-time metasurfaces can
be exploited for realizing magnetless nonreciprocity through circumventing the symmetry constraints upon introducing the spatiotemporal modulation. In fact, by introducing the space-time phase discontinuities to the interface of metasurfaces, they are no longer bounded by Lorentz reciprocity.\textsuperscript{51, 61, 62} In\textsuperscript{61} the concept of nonreciprocal wavefront engineering is experimentally demonstrated at microwaves, in which the nonreciprocity arises due to imposing drastically different phase gradients during the up/down conversion. In this case, the isolation response over 20 dB is attained by modulating the unit cells with phase delayed tones applied to the varactors. Alternative approaches based on nonlinear materials and Weyl semimetals are exploited for inducing nonreciprocity as well.\textsuperscript{63} Nevertheless, the former technique is limited by the substantial energy consumption, while the latter employs bulky multilayer configurations.

Moving beyond microwave frequencies to infrared and visible regime allows for high-speed platforms in free space communication, due to higher frequencies of the carrier signal. In another context, the concept of photonic transitions between two non-local modes by time-modulated metasurfaces for optical power isolation and circulation has been demonstrated.\textsuperscript{52} In this approach, by using opposite phases for frequency upward and downward transitions, the nonreciprocal response is acquired. However, the restriction is imposed on the frequencies of the two optical modes and the isolation is limited between two specific directions set by the dispersion of the supported modes. The arguably major challenge faced by nonreciprocal space-time metasurface paradigms at NIR regime is that only a negligible change is imprinted in the spatial pathway of light at the fundamental frequency and higher-order sidebands, under time-reversal. As a result, the weak power isolation level is obtained between the two directions. The underlying reason is the substantial difference between the carrier and modulation frequencies. In this case, for a space-time metasurface operating at the adiabatic regime, the wavelength of the scattered light shifts by undergoing
a frequency conversion at the same spatial pathway, however, the power isolation is considerably small because of the same frequency conversion performance.

In this paper, we propose and numerically demonstrate a robust method to obtain a strong power isolation in free space by using space-time gradient metasurface at NIR frequencies. For this purpose, we lift the adiabaticity of modulation by designing the ultrahigh $Q$-factor space-time metasurface that increases the lifetime of the photons such that the timescale of modulation becomes comparable with the optical oscillation of the resonator. The metasurface motif consists of a periodic repetition of amorphous silicon ($a$-Si) subwavelength grating (SWG), on a silica ($\text{SiO}_2$) buffer, where the entire structure is backed by distributed bragg reflector (DBR). The dimension of the SWG is judiciously adjusted to support higher-order Mie mode with the $Q$-factor exceeding $10^4$, that allows for local manipulation of the resonant properties of light. The SWGs are configured as multijunction p-n layers along the vertical direction to enable spatiotemporal index modulation based on carrier redistributions under the application of time-varying bias voltage. It has been demonstrated that in the non-adiabatic regime, the frequency conversion performance of the space-time metasurface is substantially different for up- and down-converted sidebands under time-reversal, even though the spatial pathway of light is identical. This ensures a strong optical power isolation in free space between any two arbitrary directions. By implementing a progressive phase delay across the space-time metasurface, the direction of the normally incident light (port 1) is steered toward the desired angle of $20^\circ$ (port 2) upon up-conversion. Under time-reversal, the incoming light from port 2 undergoes up-conversion and is steered to the initial spatial pathway at port 1. Nonetheless, due to the non-adiabatic modulation, the amplitude of the reflected power at port 1 is significantly suppressed and normalized power isolation over 35 dB is maintained.
Conceptual demonstration of light interaction with space-time gradient nonreciprocal metasurface. The metasurface comprises a periodic arrangement of $a$-Si SWG over the SiO$_2$ substrate that is backed by a four-layer DBR. The optimized dimensions are as follows (units in nm): $w = 853$, $h_1 = 684$, $h_2 = 749$, $h_3 = 104$, $h_4 = 266$, and $\Lambda = 1007$. The incoming TE polarized light with the frequency $\omega_c$ (electric field along the SWG) from port 1 is coupled to port 2 upon up conversion, while the incident light coming from port 2 is strongly suppressed after up conversion, when coupled to port 1. Therefore, the free space ports 1 and 2 are isolated. Close-up: the SWG that is configured as three pairs of p-n junctions and the multigate biasing scheme. The modulation is enabled by applying the time-varying signal with the modulation frequency $\omega_m$ and RF phase shifters to induce the required phase gradient across the metasurface.

2 Ultrahigh $Q$-factor resonant all-dielectric metasurface

Subwavelength high-index dielectric resonators with geometries such as grating, disk, and cuboid support Mie resonances. Thus far, the all-dielectric configurations supporting electric and magnetic dipolar modes have been widely used in designing metasurfaces by satisfying the first/second Kerker’s condition to suppress the backward/forward scattering, and giving rise to the transmission/reflection.$^{23,25,35,64}$ Nevertheless, the $Q$-factor of dipolar modes are not sufficiently high to provide the desired spectral shift by exploiting the refractive index change in the order of $\Delta n = 0.01$. Recently, higher-order Mie-type modes are used in several contexts to excite high
Q-factor resonances by increasing the overall dimension of the resonator. In a Huygens metasurface paradigm that consists of all-dielectric cuboids is proposed that leverages the higher-order Mie resonance to achieve two-dimensional static beam steering. In this regard, the major challenge is to keep the unit cell dimension as compact as possible to avoid the undesired artifacts at the optical response. However, reducing the resonator size while keeping the same operating wavelength implies the use of lower order Mie-type modes, whose higher radiative losses leads to a drop in the Q-factor of the resonance.

The schematic of space-time nonreciprocal metasurface is pictorially illustrated in Fig. 1. We consider a 1D array of a-Si SWG that is separated from the DBR through SiO$_2$ buffer. The DBR consists of four pairs of Si/SiO$_2$ stacks with Si as the topmost layer. The SWG is configured as three alternative pairs of p-n junctions along the vertical direction. The electrical biasing of this structure is enabled by application of time-varying signal into the SWGs, where p-type and n-type regions serve as the contact electrodes (see inset of Fig. 1). First, we consider the optical response of the unbiased metasurface when it is illuminated by the normally incident TE polarized light (electric field along the y-axis). For this purpose, the material properties of the undoped a-Si and SiO$_2$ are respectively extracted from the experimental data in and whereas the p- and n-doped Si layers are characterized by the Drude-plasma model as

$$\Delta n_{Si} = -(e^2 \lambda^2 / 8 \pi^2 c^2 \epsilon_0 n_0)[N/m_e^* + P/m_h^*]$$  \hspace{1cm} (1)

$$\Delta k_{Si} = -(e^3 \lambda^3 / 16 \pi^3 c^3 \epsilon_0 n_0)[N/m_e^* \mu_e + P/m_h^* \mu_h]$$  \hspace{1cm} (2)
In the above equations, \( e \) is the electron charge, \( \lambda \) is the operating wavelength, \( \epsilon_0 \) and \( n_0 \) are the permittivity of free space and nominal refractive index of undoped silicon, \( m_e^* = 0.27m_0 \) and \( m_h^* = 0.39m_0 \) are the effective mass of the electrons and holes with \( m_0 \) being the electron mass, \( \mu_e = 80 \text{ cm}^2/\text{V.s} \) and \( \mu_h = 60 \text{ cm}^2/\text{V.s} \) are the electron and hole mobility, while \( N \) and \( P \) are the carrier densities of electrons and holes, respectively. The p- and n-type regions are uniformly doped with the moderate carrier concentrations of \( N = P = 10^{18} \text{ cm}^{-3} \) that can be practically obtained with the current state-of-the-art of nanofabrication techniques. The geometrical parameters of the metasurface are optimized to excite the localized and high-\( Q \) mode within the SWG that affords a steep phase swing at NIR regime. The thicknesses of the alternating Si/SiO\(_2\) pairs in DBR configurations correspond to the effective quarter-wavelength in the high-index contrast materials with refractive indices identical to \( n_{\text{SiO}_2}=1.452 \) and \( n_{\text{Si}}=3.487 \) at 1.55 \( \mu\text{m} \). The structural parameters of the metasurface are revealed at the caption of Fig. 1.

The recent advances in the nanofabrication technology have made the fabrication of the proposed device feasible by using the chemical vapor deposition (CVD) and electron beam lithography (EBL).\(^{41,68,69}\) First, the DBR structure with 4 pairs of Si/SiO\(_2\) quarter-wave stack should be deposited over the glass substrate using the plasma-enhanced chemical vapor deposition (PECVD). Next, the SiO\(_2\) dielectric spacer and \( a\)-Si layer should be also deposited on the sample by PECVD. To form the SWGs, the top \( a\)-Si layer should be then patterned by EBL and dry etched in plasma. It is worth mentioning that the p-n multijunctions have been widely used in tandem solar cells and vertical-cavity surface emitting lasers (VCSELs).\(^{70}\) To implement the layered SWGs, the sputtering techniques can be used, wherein boron and phosphorous dopants (B\(^+\) and P\(^-\)) are utilized for achieving the desired background carrier distribution across the vertical direction by diffusion and ion implementation.\(^{71}\)
The optical response of the proposed metasurface is studied within the framework of rigorous space-time coupled-wave analysis (RSTWA) that enables analytical simulation of space-time metasurfaces without making any assumption on the frequency of modulation. RSTWA is the extension of Fourier-based rigorous coupled-wave analysis (RCWA), that solves the Maxwell equations through expanding them in the basis of plane waves for structures with both spatial and temporal variations. In this technique, the scattered fields are expanded in terms of space-time Fourier harmonics defined by the spatial and temporal periodicities of the structure and the relations between the incident and scattered fields are computed by transforming the periodic spatiotemporal profile of refractive index to the spectral domain. To start, we have obtained the metasurface optical response at the absence of any time modulation and the results are shown in Fig.2. For this aim, the number of temporal diffraction orders in RSTWA solver are adjusted to zero, while the Fourier modes along the spatial dimension are carefully chosen to ensure the convergence of the results. To validate the accuracy of the RSTWA simulations, we have compared them against the full-wave simulation results obtained by COMSOL Multiphysics and the details are expressed in section S1 of the Supplemental Materials. We have further studied the reflection spectra of the DBR consisting of different pairs and the sensitivity of the optical mode to the incident angle at Supplemental Materials section S2 and S3, respectively. Figure 2(a) depicts the reflection amplitude of the metasurface as functions of the incident wavelength and the width \( w \) of SWG, when it is varying in the range of 600 – 900 nm, while \( h_1 \) is fixed at 684 nm. On the other hand, the spectral variations of the reflection coefficient is shown at Fig. 2(b) as a function of SWG height \( h_1 \), when it is increasing from 400 nm to 700 nm, where \( w \) is adjusted to 853 nm. The results clearly indicate the emergence of two branches of the resonant modes that are marked by red and black circles, respectively. In both figures, the black circles correspond to the high-\( Q \) resonant modes, while the red branch in-
icates the reflection dips for the modes with relatively low $Q$-factors. The size of the circles are proportional to the $Q$-factor of the supported modes, whose approximate values are depicted at the insets of Figs. 2(a)-(b). The $Q$-factors of the supported modes on black and red branches are calculated and the results are illustrated in section S4 of the Supplemental Materials. By moving over the black branch, the mode exhibits linewidth narrowing and therefore, an increase in the $Q$-factor. The highest $Q$-factor is maintained at the anticrossing region between two branches at around 1312 nm, whose value reaches to the maximum of $\approx 16000$ that corresponds to the super-cavity mode, as shown in Fig. 1(a). This is while, for the red branch with moderately low-$Q$ mode, the $Q$-factor that is calculated as $\approx 2000$ remains almost unchanged by altering $w$. In an analogy to this case, one can observe that along the black branch at Fig. 2(b), an increase in the $Q$-factor is achieved for $h_1$ in the range of $600 - 630$ nm and $660 - 700$ nm and the maximum $Q$-factor of $\approx 20000$ is maintained. Similarly, the red branch corresponds to the low-$Q$ mode and the $Q$-factor of the resonant mode varies between 900 to 3000 for different values of $h_1$. To complete the characterization of the highlighted resonant modes, the near-field distribution of the $x$ component of the magnetic field is depicted for typical values of $w$ and $h_1$ along with the low-$Q$ and high-$Q$ branches in Figs. 2(a)-(b). It is noticeable that at the anticrossing point, the field is extremely confined within the SWG resonator with the small radiation loss that is the underlying reason for ultrahigh $Q$-factor at this point. At slightly higher widths with respect to the mode at the anticrossing point (Fig. 2(a)), it is observed that the energy leaks out of the resonator resulting in reduction of the $Q$-factor and increase in the radiation efficiency. The red branches in both Figs. 2(a)-(b) are governed by the lower-order Mie-type modes as discussed in.\textsuperscript{43} In addition, from the results in Figs. 2(a)-(b), one can observe that the resonant mode on the black branch strongly depends on $w$, while it is less sensitive to $h_1$. Specifically, when there is a 150 nm change in the width and height of the SWG
(\(w\) and \(h_1\) are altered within the intervals 720 – 870 nm and 550 – 700 nm), the resonant mode experiences spectral shift of 233 nm and 57 nm, respectively. As such, an almost four-fold larger spectral shift is noticed for width variation compared to the height, when they both are varying in the same range. The more sensitivity of the resonant mode to the width of resonator compared to its height is the characteristic of Mie-type resonances, which are formed by the multiple reflections from the left and right interfaces of the resonator, this is while the Fabry-Pérot mode is established based on the multiple reflections from the resonator top and bottom interfaces and therefore being more sensitive to height variations. The reflection amplitude and phase of the metasurface unit cell are calculated at the point denoted by magenta pentagonal marker at Figs. 2(a)-(b), which corresponds to \(w = 853\) nm and \(h_1 = 684\) nm and the result is shown at Fig. 2(c). The high-\(Q\) resonant mode can be identified from the steep and highly dispersive spectral phase accumulation of \(2\pi\) within < 1 nm wavelength interval, whose \(Q\)-factor reaches 11876 at 1548 nm. It is worth mentioning that although the loss of \(a\text{-Si}\) is negligible at near-infrared regime, the extreme light-matter interaction at the high-\(Q\) resonator gives rise to amplitude attenuation at the resonant wavelength. The real and imaginary parts of the reflection coefficient at this point are plotted at the alternative \(x\) and \(y\) axis of Fig. 2(c). The reflection coefficient shows a circle trajectory by progressing over the spectral wavelength that covers all four quadrants of the complex plane. This ensures a full \(2\pi\) spectral phase. Nevertheless, the distance of the points on the circumference from the origin are varying, which shows the non-uniform reflection amplitude, due to the loss. It should be noted that the excitation of the resonator can be generalized to TM polarization as well. In this case the avoided crossing of the modes is not always required for exciting the high-\(Q\) resonances. However, it is shown that the inter-element coupling between the adjacent unit cells are significant under TM polarization in comparison to TE, which leads to crosstalk and undesired sidelobes.\(^{73-75}\)
Simulated characteristics of all-dielectric high-$Q$ time-invariant metasurface under normal illumination of TE polarized light. The spectral distribution of the metasurface reflection amplitude as functions of (a) width ($w$) when $h_1$ is fixed at 684 nm and (b) height ($h_1$) when $w$ is set to 853 nm. The peak positions and the $Q$-factors of the two anticrossing modes are shown by black (high-$Q$ mode) and red (low-$Q$ mode) circles. The size of the circles are proportional to the $Q$-factor levels such that larger circles correspond to high-$Q$ resonances. The insets show the magnetic near-field maps within the SWG cross section for different dimension at their operating wavelengths over the low-$Q$ and high-$Q$ branches. (c) The amplitude (red) and phase (blue) of the reflected light as a function of incident wavelength when $w$ and $h_1$ are fixed to 853 nm and 684 nm. The alternative $x-$ and $y$-axis correspond to the real and imaginary parts of the complex reflection coefficient that illustrates a circle trajectory, while covering all four quadrants that ensures $2\pi$ phase swing. (d) Multipolar contribution of the scattering cross section of the metasurface. (e) Near-zone distribution of the magnetic field within the metasurface cross section at the resonant wavelength 1548 nm, that confirms excitation of higher-order Mie mode corresponding to magnetic octupole.
In order to get a better insight to the radiative properties of the resonant modes, we employ the multipole decomposition up to the forth-order, tied by electric and magnetic octupoles, to calculate the contribution of each multipole in the scattering response. For this purpose, we have conducted a theoretical analysis based on multipole decomposition method developed for light scattering.\textsuperscript{76–78} In this method, the total electric fields over the resonators composing the metasurface induced by the incident light are calculated and then the multipole moments of the resonators are extracted following their definition,\textsuperscript{79,80} in which the current density is replaced by the induced polarization vector. The detailed formulation regarding the computation of the multipole moments is indicated in section S5 of the Supplemental Materials. Figure 2(d) shows the normalized scattering cross section as a function of incident wavelength over a wide range, and the contribution of the multipole moments at the output response. It is shown that the lower-order modes, i.e., electric and magnetic dipoles are dominant at the longer wavelengths, where the periodicity of the unit cell is $\approx 1/4$ of the operating wavelength. The $Q$-factor of the dipolar modes are low as it is clear from Fig. 2(d). As a result, achieving a dynamic wide phase/amplitude modulation via the index changes induced by electro-optical carrier effects is limited. At shorter wavelengths and around 1.55 $\mu$m, the excitation of high-$Q$ modes can be noticed. They correspond to the higher-order Mie-type resonances as the size of the resonator increases with respect to the wavelength. At the wavelength 1548 nm, the contributions of electric and magnetic quadrupoles (EQ and MQ), as well as magnetic octupole (MO) are dominant. Nevertheless, as discussed earlier, the field confinement of MO is higher in comparison to the EQ and MQ, which makes its scattering efficiency to be smaller. As such, MO represents a decreased scattering cross section at 1548 nm, as can be verified from Fig. 2(d). To provide a fair comparison in terms of scattering efficiency, we have extracted the amplitude of the multipole moments in the same metric, normalized them to the maximum magnitude and
depicted the results in Fig. S5 of the Supplemental Materials. The contribution of multipoles reveal that the response is dominated by the MO moment at 1548 nm, confirming the nature of the resonant mode as magnetic octupole. To further elaborate on the origin of the resonance, the near-field distribution of the $x$ component of the magnetic field is demonstrated in Fig. 2(e). As it is expected, the near-field pattern illustrates the excitation of a resonant mode that is characterized as magnetic octupole and is mainly localized within the SWG. Nevertheless, there is seen a field enhancement between the adjacent metasurface unit cells that indicates the inter-resonator coupling of the elements and can lead to undesired artifacts manifested as sidelobes. However, the magnetic field amplitude localized within the SWG is at least twice of the inter-emitter coupling. It should be noted that our proposed metasurface paradigm supports an ultrahigh-$Q$ mode over a subwavelength unit cell. This is unlike the metasurfaces that enable the excitation of guided mode resonances or QBICs, which offer the $Q$-factors almost at the same order, while they require larger footprints for supporting in-plane propagation of the photons along the array before leaking out to the free space. Although high-$Q$ metasurfaces allow us to obtain wide modulation of optical response by subtle change of the refractive index, they are highly sensitive to small fabrication tolerances of the structural parameters as shown in Figs. 2(a)-(b). Another limiting factor in designing ultrahigh-$Q$ metasurfaces is the ohmic loss of the materials. The ohmic loss substantially reduces the $Q$-factor of the metasurface and prohibits us from further increasing the $Q$-factor as shown in Fig. 2(c). Alternative loss origin raised form fabrication imperfections can further reduce the $Q$-factor of the resonator. In addition, as it is observed in Fig. 2(e), although the field distribution is mainly confined within the resonator, the inter-element coupling between the adjacent unit cells is not negligible compared to the plasmonic resonators, for example. The nearest-neighbor coupling occurs along the phase gradient direction and therefore results in deviation of the obtained phase
from the desired one and local phase errors can arise from the coupling between the adjacent SWGs. It is worth mentioning that high-$Q$ modes usually suffer from low radiation efficiency due to the strong confinement of the energy. In section S6 of the Supplemental Material we have evaluated the radiation performance of the magnetic octupole mode and compared its result with a electric dipole mode with relatively low $Q$-factor.

3 Space-time metasurface platform

In this section, we study the space-time metasurface paradigm for optical power isolation through introducing time-modulation into the system. When the incident light with the angular frequency $\omega_c$ interacts with the space-time metasurface, the scattered light undergoes a frequency transition and higher-order sidebands are generated at the integer multiples of the modulation frequency $\omega_m$ ($\omega_n = \omega_c \pm n\omega_m$, where $n \in \mathbb{Z}$). The modulation frequency of the electro-optically tunable metasurfaces can be specified through the RC time-constant of their constituent elements and is estimated to be at the order of several hundreds of GHz, that is at least three orders of magnitude smaller than the carrier frequency at NIR regime. This limits the metasurface analysis to the adiabatic regime of modulation, wherein the spatial pathway of light remains almost unchanged for the fundamental frequency and the up and down modulation under time-reversal. Nevertheless, for the metasurfaces with high $Q$-factor, similar to our proposed design, the order of magnitude difference between the carrier and modulation frequencies is compensated. In this case, the $Q$-factor of the resonator is greater than 11000 and the carrier frequency is at NIR regime, therefore, the lifetime of the photons trapped in the SWG enters the nanosecond range, and becomes comparable with the modulation cycle. This renders the modulation process to be in the non-adiabatic regime. Throughout this manuscript, we have adjusted the modulation frequency at 55 GHz, which is consistent with the
experimental results for the Si-based electro-optical resonators\textsuperscript{71} and can be maintained by keeping the metasurface footprint, driver electronics, and wiring as compact as possible to reduce the RC time constant.

Here, the design goal is to obtain a nonreciprocal response by the space-time metasurface for achieving optical power isolation in free space. Basically, this can be yielded by imparting the desired momentum for photonic transitions between the fundamental frequency and higher-order sidebands and manipulating the output spectrum by optimizing the modulation waveform such that most of the input power transforms into the desired sideband and all the undesired mixing products are suppressed. The output spectrum with the desired spectral diversity and efficiency of the sidebands dictates the temporal response of the scattered fields at the steady state that can be expressed as

\begin{equation}
E_i(t) = E_0 \exp(i\omega_ct) \tag{3}
\end{equation}

\begin{equation}
E_r(t) = E_0 |r(t)| \exp(i\angle r(t)) \exp(i\omega_ct) = \sum_{n=-\infty}^{\infty} c_{n,r} \exp(i(\omega_c + n\omega_m)t) \tag{4}
\end{equation}

wherein $E_i$ and $E_r$ stands for the incident and reflected electric fields, $E_0$ expresses the amplitude of the incident field, $r(t)$ is the time-dependent reflection coefficient, $c_{n,r}$ is the frequency domain complex amplitude of the reflected field at the $n^{th}$-order sideband that can be obtained by Fourier transform of the time-domain reflection coefficient. In order to achieve the desired nonreciprocal response at the output spectrum, the inverse design and optimization methods should be employed for obtaining the complex modulation waveforms with strong time-reversal asymmetry (i.e., sawtooth-like pattern).\textsuperscript{83,84} However, these methods are time-consuming and as discussed
earlier, the spatial pathway of light at different sidebands cannot be sufficiently changed to impart nonreciprocity. Lifting the adiabaticity of modulation offers a pathway to attain a noticeable conversion from the fundamental to higher-order frequencies under time-reversal and substantially change the spatial pathway of light, without making any effort to optimize the modulation waveform. Throughout this manuscript, we have considered a sinusoidal modulation waveform to study the response of the space-time metasurface, unless otherwise is stated.

To realize the refractive index modulation within the SWG upon introducing the sinusoidal waveform, the electro-refraction in the multi-junction p-n layers is exploited. The carrier modulation in the $a$-Si p-n junctions has been previously used in optical modulators. To implement this method as the modulation mechanism of the space-time metasurface, we have divided the SWG into six sublayers along the vertical direction, where the alternative sublayers are uniformly doped by moderate hole and electron carriers with the concentrations of $P = 10^{18}$ cm$^{-3}$ and $N = 10^{18}$ cm$^{-3}$, respectively. The sublayers are arranged as three pairs of p-n junctions with the order of p-n-p-n-p-n from top to bottom as depicted in the inset of Fig. 1, where the thickness of each p- and n-type regions is $h_1/6 = 114$ nm. The p-doped and n-doped regions can be connected to the low-resistance contact pads from the edge of the metasurface and then they can be wire-bonded to the biasing circuit board. To characterize the electro-optical response of the p-n junctions to external modulation, we have calculated the carrier dynamics within the SWG and then linked the results to the optical properties of the p- and n-type regions through the Drude-plasma model described by equations (1)-(2). Lumerical device solver is utilized to calculate the bias-dependent carrier distribution of p-n junctions, which self-consistently solves the Poisson and drift-diffusion equations via finite element method. The profile of the modulation as a function of time that is applied to the metasurface is depicted in Fig. 3(a). It is a simple sinusoidal function that can be
expressed as \( V(t) = V_{DC} + \Delta V \sin(\omega_m t) \), where \( V_{DC} \) is the average of lower and upper bounds of the applied bias voltage and \( \Delta V \) is the modulation depth. The upper and lower bounds for the modulation waveform are chosen such that they assure the uniform distribution of the electrons and holes within the p-n multijunction. Further details in this regard are provided in section S7 of the Supplemental Materials. Indicated in Figs. 3(b)-(c), are the spatial distribution of the electrons and holes along the height of the SWG within a modulation cycle, respectively. The dashed lines demarcate the boundaries between the p-type and n-type regions. It is observed that upon applying the bias voltage, the electrons and holes are redistributed according to the magnitude and trajectory of the modulation waveform. Therefore, the carrier concentrations are modulated sinusoidally as functions of time through consecutive accumulation and depletion. As progressing in time, when the bias voltage becomes smaller than the DC voltage, the concentrations of electrons and holes decrease in the n-type and p-type regions. On the contrary, upon increasing the bias voltage above the DC level at the second half of the modulation cycle, the charge carriers start to accumulate within the p and n regions. It should be noted that the length of the SWGs along the \( y \)-direction can result in modulation of the charge carriers in the lateral direction by moving away from the contact pads where the bias voltage is applied. Therefore, the footprint of the SWGs should be chosen compact in practice \((< 10 \mu m)\) to avoid the carrier density change along the lateral direction that impacts the electro-optical performance of the metasurface and to minimize the RC time delay, which increases the response time. The spatial distributions of the real and imaginary parts of the refractive index in the multijunction p-n structure are obtained as functions of time within one modulation cycle at the operating wavelength of \( \lambda = 1548.2 \text{ nm} \) and the results are shown in Figs. 3(d)-(e). It can be observed that for the bias voltage sinusoidally modulating between \( 1 - 1.25 \) \( V \), the real part of the refractive index indicates the change of \( \approx -0.003 \), while the imaginary part
Fig 3  Space-time modulation of the high-Q metasurface. (a) The profile of the sinusoidal modulation waveform with time-reversal symmetry that is applied to the metasurface. The spatial distributions of the (b) electron and (c) hole carrier concentrations inside the multijunction p-n layers as functions of time depicted in one modulation cycle. (d) The real and (e) imaginary parts of the refractive index within the multijunction p-n layers as functions of time and space in one modulation cycle obtained at the operating wavelength of 1548 nm. The refractive index is sinusoidally modulated between 3.7295 and 3.7325. The white dashed lines demarcate the boundaries between the p-type and n-type regions.

remains below $3 \times 10^{-4}$. The small imaginary part is attained due to the moderate background doping of p- and n-type regions.

After characterizing the refractive index of p-n multijunction, we employ RSTWA to calculate the electro-optical response of the space-time metasurface to the modulation waveform depicted in Fig. 3(a). In order to account for nonuniformities of the permittivity according to the results in Figs. 3(d)-(e), we rigorously take into account their spatial distribution by discretization of the SWGs into several sublayers with homogeneous permittivity along the vertical direction. The number of sublayers are chosen to ensure the converged results as shown in section S7 of the Supplemental Materials. Figure 4(a) depicts the reflection amplitude spectra of the high $Q$-factor space-time metasurface as a function of sideband order and incident wavelength. It can be clearly seen from
the result that when the incident wavelength strays away from the resonance, the output spectrum becomes highly asymmetric despite the symmetric waveform that is utilized for the excitation. In particular, for an incident light coming at the wavelength of 1548.7 nm, the power is substantially up-converted, while the down conversion is strongly suppressed. On the other hand, for the incident wavelengths below the resonance, namely 1547.8 nm, the up-converted signal is strongly suppressed and power is mainly down-converted. To provide a better insight, we have plotted the reflection amplitude as a function of wavelength at the fundamental frequency and the first-order up- and down-converted sidebands in Fig. 4(b). For the up-converted sideband \((n = +1)\), we can observe two reflection peaks at the resonant wavelength \((\lambda = 1548.2 \text{ nm})\) and \(\lambda = 1548.7 \text{ nm}\), that corresponds to the up modulation of the resonant frequency such that \(\omega = \omega_r + \omega_m\). At the down conversion \((n = -1)\), the reflection peaks are located at resonant wavelength \((\lambda = 1548.2 \text{ nm})\) and its down modulation \((\omega = \omega_r - \omega_m)\) that corresponds to the wavelength \(\lambda = 1547.8 \text{ nm}\). At resonant wavelength, the reflection peaks at the up-converted and down-converted sidebands are degenerate, i.e., at the same wavelength. However, at off-resonance wavelengths the degeneracy of the peaks is lifted and they are shifted toward different directions at the opposite sides of the spectrum. This is thanks to the high \(Q\)-factor of the metasurface paradigm that induces the non-adiabatic modulation and leads to a well-separated sideband orders in the spectral domain and paves the way toward achieving the nonreciprocal response under time-reversal. To demonstrate the capability of our proposed space-time metasurface in power isolation between two arbitrary ports, we explored the output spectrum by exciting the metasurface under normal and oblique incidences, where the incident angles are adjusted to \(0^\circ\) and \(20^\circ\). Figure 4(c) shows the results in which the output spectrum of the reflected light at port 1 \((0^\circ)\) and port 2 \((20^\circ)\) are calculated in logarithmic scale by taking the Fourier transform of the time-domain reflection coefficient and the spectra are
normalized to the total scattered intensity from all the sidebands and the fundamental frequency. The operating frequency for the metasurface under normal illumination is at $\lambda = 1548.2$ nm, while it is adjusted to $\lambda = 1547.8$ nm for the oblique incidence. The difference between their corresponding angular frequencies is $\omega_m$, which is considered to minimize the interference between the two ports. As it can be seen from Fig. 4(c), the level of the up-converted reflected light from space time metasurface under normal incidence at port 1 is at least 35 dB larger than the one at port 2 and under oblique incidence. This shows a great isolation between the two ports.

It should be noted that the proposed unit cell is designed for nonreciprocal operation between any two arbitrary directions. This is in contrast to the previous magnetless time-modulated paradigm for power isolation in,\textsuperscript{52} wherein the restriction is imposed on the frequencies of the two supported non-local resonant modes and limits the isolation between only two specific directions. In addition, the proposed unit cell is composed of a single metasurface layer that allows for power isolation by leveraging the sharp contrast between the fundamental and up-converted signal which is achieved due to the high-$Q$ resonator. This is unlike the recent study in\textsuperscript{87} that employs an additional layer as a filter to increase the isolation level between the two ports. It is also worth mentioning that, we have not made any effort to optimize the modulation waveform in order to increase the isolation level and a simple sinusoidal waveform is employed which yields a noticeable conversion into higher-order sideband. However, in section S8 of the Supplemental Materials we have shown that by optimizing the modulation waveform, the isolation level can be further increased to 40 dB.
4 Gradient metasurface for nonreciprocal beam steering

In this section, we employ the proposed unit cell for constructing the time-modulated reflectarray that exhibits nonreciprocal response. To this aim, the sinusoidal modulation waveform indicated in Fig. 3(a) as well as the modulation-induced progressive phase delays are applied across metasurface to render a phase gradient reflectarray in space and time. The modulation profile can be synthesized by the arbitrary waveform generator (AWG). The measurement of the sidebands can be done directly by the optical spectrum analyzers if they are separated at a few GHz intervals or can be done with photo-detection and use of RF spectrum analyzers if their separation is less than 1 GHz. The RF phase shifts required for beam-steering toward the desired angle can be imparted by introducing the phase shift in different channels of the AWG addressing the array elements. Such an RF biasing network for implementing the time-modulated metasurface can lead to crosstalk between the adjacent metasurface elements. However, the signal distortion due to the crosstalk can be minimized by adjusting the inter-element spacing or coating the elements by a capping insulator layer that can further isolate the adjacent elements.
To verify the capability of the proposed space-time gradient metasurface for free space power isolation, we consider a periodic supercell that consists of five time-varying unit cells that are arranged along the $x$-axis. The separation distance between the elements is $\Lambda = 1007$ nm, which is around $\approx \lambda/1.5$ at the operating wavelength. The structure is normally illuminated by the $y$-polarized plane wave. The modulation waveform is kept unchanged as depicted in Fig. 3(a), while the progressive phase delay of $\alpha(x) = -k_0 x \sin(\theta_s)$ is implemented across the metasurface in accordance with the requirement for achieving the target steering angle of $\theta_s$ at the output. The steering angle is set to $\theta_s = 20^\circ$ for our studies. It is worth mentioning that the progressive phase shift imprinted on the wavefront of the reflected light at the sidebands is dispersionless and spans over the complete $2\pi$ range. This resembles the Pancharatnam-Berry (PB) phase shift, which occurs in half-wave plate converters upon polarization conversion, and makes the space-time metasurfaces to break away from the limitations caused by the dispersive nature of resonant unit cells. In addition, the phase profile of the up-converted signal provides a negative phase shift with respect to the down-converted case. This can be implied from equation (14) in Ref.\textsuperscript{84} that shows the imprinted phase gradients at the sidebands with the opposite orders are conjugate. The spatiotemporal permittivity change of the $a$-Si SWG, which is resulted by the sinusoidal modulation waveform can be described as $\epsilon_{SWG} = \epsilon_{dc} + \Delta \epsilon \sin(\omega_m t + \alpha(x))$, where $\Delta \epsilon$ is the modulation depth and defines the deviation of the permittivity with respect to the unbiased configuration, which is set to 0.008 in accordance with Fig. 3(d). The desired output spectrum of the sidebands is maintained by adequately tailoring the modulation depth that controls the level of the reflected power at different sidebands as depicted in Fig. 4(a).

In order to establish the isolation between the two ports in free space, that are selected as normal direction and $\theta_s = 20^\circ$, we apply the modulation waveform and required phase gradient across
the reflectarray. Under time-reversal, the incident light can undergo an up or down conversion and be steered toward the different spatial pathway defined by the imprinted phase gradient. In the account of the non-adiabatic frequency conversion performance, for the incoming light, whose wavelength is longer than the resonant wavelength, the down conversion is strongly suppressed, while for the light with the incident wavelength shorter than the resonant, the up conversion is eliminated. Figures 5(a)-(d) illustrate the wavefronts of the reflected light at the fundamental frequency and its up conversion, when the reflectarray is illuminated by the normal and oblique beams. For the sake of simplicity, the normal and oblique directions at $\theta = 0^\circ$ and $\theta = 20^\circ$ are called as port 1 and port 2, respectively. As it is clearly observed, for the incoming light from port 1 and at resonant frequency ($\omega_r$), the light is reflected back to port 1, since the direction of the fundamental frequency is governed by the specular reflection and cannot be actively tuned by changing the modulation induced phase shift. However, the reflected light at the up-converted sideband ($\omega_r + \omega_m$) is steered toward port 2 at $\theta = 20^\circ$. The perturbations in the wavefront of the magnetic field in Fig. 5(b) shows that the amplitude at the sideband does not remain constant at the non-adiabatic regime of modulation despite the adiabatic regime. However, the anomalous reflection of light to port 2 at the first-order sideband confirms that the dispersionless phase shift spanning on $2\pi$ persists in this regime. Figures 5(c)-(d) show the reflected light upon exciting the reflectarray by the incoming light from port 2. The frequency of the incident light is identical to up modulation of the resonant frequency and therefore its corresponding wavelength is shorter than the resonant. According to Fig. 4(a), in this case the up conversion of the incident light should be suppressed. Similar to the previous case, at the fundamental frequency ($\omega_r + \omega_m$), the incident light coming from port 2 undergoes a specular reflection and its spatial pathway is bent to the symmetrically opposite angle under oblique incidence ($\theta = -20^\circ$), which is well separated from port 1. On the
other hand, the up-converted light at \( \omega_r + 2\omega_m \) is steered toward its initial pathway at port 1, due to experiencing conjugate modulation-induced phase gradient, while its amplitude is significantly attenuated because of the non-adiabatic frequency conversion performance as it was expected. It can be concluded from the results in Fig. 5 that the incoming power from port 1 can be mainly coupled to port 2 under time-reversal, while the power coupling from port 2 into port 1 is significantly small that ensures optical power isolation in free space between the two ports. This concept can be easily expanded to establish isolated links between any arbitrary ports in free space. As it is shown in Fig. 4(c) the normalized isolation level between the ports is calculated as \( \approx 35 \text{ dB} \). It should be noted that the reciprocal metasurface would have steered the beam to its initial direction without any change in its amplitude.

5 Conclusion

In this paper, we numerically demonstrated the realization of high \( Q \)-factor space-time gradient metasurface operating at NIR regime for optical power isolation. For this purpose, we considered \( \alpha \)-Si SWG on top of the SiO\(_2\) substrate and DBR as the metasurface building block. To apply the time-varying biasing, the SWGs are configured as multijunction p-n layers with moderate doping that enable index modulation through electro-refraction induced by carrier accumulation within the entire SWG volume. The structural parameters of the metasurface are adjusted such that it supports a localized higher-order Mie resonance that is characterized as magnetic octupole. The \( Q \)-factor of the resonance is calculated as 11876 that gives rise to the photon lifetime within the resonator such that timescale of the optical oscillation becomes comparable with the modulation cycle and renders the non-adiabatic modulation process. The frequency conversion performance of the space-time metasurface in non-adiabatic modulation regime demonstrates nonreciprocal re-
Fig 5 Optical power isolation in free space. The wavefronts of the reflected light from the gradient space-time metasurface at the fundamental and first-order up-converted sidebands when the metasurface is illuminated by (a)-(b) normal light coming from port 1 and (c)-(d) oblique incidence coming from port 2. At resonant frequency ($\omega = \omega_r$) the up-converted normally incident light is steered toward port 2 ($\theta = 20^\circ$). The light incoming from port 2 at $\omega_r + \omega_m$ is bent toward port 1 at $\theta = 0^\circ$ upon up conversion, while its amplitude is strongly suppressed. The color bars are rescaled to provide a fair comparison. The magnetic field level in (d) is varying between $-0.01$ and $0.01$. 
sponse under time-reversal and allows for strong suppression of the frequency up conversion (down conversion) upon exciting the metasurface by up modulated (down modulated) incident light. By introducing the modulation-induced phase delay between the individual elements of the nonreciprocal metasurface, a phase gradient reflectarray is rendered in space and time that allows for optical power isolation between any two arbitrary ports in free space. We have considered the two ports as $\theta = 0^\circ$ (port 1) and $\theta = 20^\circ$ (port 2), respectively. The incoming light from port 1 is up-converted ($\omega_r \rightarrow \omega_r + \omega_m$) and steered toward port 2 on the virtue of modulation induced phase shift. On the other hand, the up-modulated incident light at port 2 undergoes an up conversion ($\omega_r + \omega_m \rightarrow \omega_r + 2\omega_m$) and points toward a well-separated angle at port 1 due to experiencing conjugate modulation-induced phase gradient. On the account of non-adiabatic frequency conversion performance, the reflected light at port 1 is substantially suppressed, while the dominant portion of the reflected field that does not undergo frequency conversion bends toward the specular reflection angle. The normalized isolation level between the ports is calculated as $\approx 35$ dB.

6 Disclosures

The authors declare no Conflicts of interest.

7 Code, Data, and Materials Availability

Structural parameters and simulated and experimental data have been provided within the main text and Supplementary Material of this paper. All the other data that support the findings of this study are available from the corresponding author upon reasonable request.
8 Acknowledgments

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References


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1 Conceptual demonstration of light interaction with space-time gradient nonreciprocal metasurface. The metasurface comprises a periodic arrangement of $a$-Si SWG over the SiO$_2$ substrate that is backed by a four-layer DBR. The optimized dimensions are as follows (units in nm): $w = 853$, $h_1 = 684$, $h_2 = 749$, $h_3 = 104$, $h_4 = 266$, and $\Lambda = 1007$. The incoming TE polarized light with the frequency $\omega_c$ (electric field along the SWG) from port 1 is coupled to port 2 upon up conversion, while the incident light coming from port 2 is strongly suppressed after up conversion, when coupled to port 1. Therefore, the free space ports 1 and 2 are isolated. Close-up: the SWG that is configured as three pairs of p-n junctions and the multigate biasing scheme. The modulation is enabled by applying the time-varying signal with the modulation frequency $\omega_m$ and RF phase shifters to induce the required phase gradient across the metasurface.
Simulated characteristics of all-dielectric high-\( Q \) time-invariant metasurface under normal illumination of TE polarized light. The spectral distribution of the metasurface reflection amplitude as functions of (a) width \((w)\) when \(h_1\) is fixed at 684 nm and (b) height \((h_1)\) when \(w\) is set to 853 nm. The peak positions and the \( Q \)-factors of the two anticrossing modes are shown by black (high-\( Q \) mode) and red (low-\( Q \) mode) circles. The size of the circles are proportional to the \( Q \)-factor levels such that larger circles correspond to high-\( Q \) resonances. The insets show the magnetic near-field maps within the SWG cross section for different dimension at their operating wavelengths over the low-\( Q \) and high-\( Q \) branches. (c) The amplitude (red) and phase (blue) of the reflected light as a function of incident wavelength when \(w\) and \(h_1\) are fixed to 853 nm and 684 nm. The alternative \( x \)- and \( y \)-axis correspond to the real and imaginary parts of the complex reflection coefficient that illustrates a circle trajectory, while covering all four quadrants that ensures \( 2\pi \) phase swing. (d) Multipolar contribution of the scattering cross section of the metasurface. (e) Near-zone distribution of the magnetic field within the metasurface cross section at the resonant wavelength 1548 nm, that confirms excitation of higher-order Mie mode corresponding to magnetic octupole.
Space-time modulation of the high-$Q$ metasurface. (a) The profile of the sinusoidal modulation waveform with time-reversal symmetry that is applied to the metasurface. The spatial distributions of the (b) electron and (c) hole carrier concentrations inside the multijunction p-n layers as functions of time depicted in one modulation cycle. (d) The real and (e) imaginary parts of the refractive index within the multijunction p-n layers as functions of time and space in one modulation cycle obtained at the operating wavelength of 1548 nm. The refractive index is sinusoidally modulated between 3.7295 and 3.7325. The white dashed lines demarcate the boundaries between the p-type and n-type regions.

The non-adiabatic frequency conversion performance of the normally-illuminated ultrahigh-$Q$ spatiotemporal metasurface under time-reversal. (a) The output spectrum of the reflection coefficient at the generated sidebands as a function of sideband order ($n$) and the incident wavelength. (b) The reflection amplitude at the fundamental ($n = 0$), first-order up converted ($n = +1$) and first-order down converted ($n = -1$) sidebands as functions of incident wavelength. (c) The normalized output spectrum of the reflected light when the space-time metasurface is under normal ($\theta_i = 0^\circ$) and oblique ($\theta_i = 20^\circ$) illumination. The isolation level more than 35 dB is observed.
Optical power isolation in free space. The wavefronts of the reflected light from the gradient space-time metasurface at the fundamental and first-order up-converted sidebands when the metasurface is illuminated by (a)-(b) normal light coming from port 1 and (c)-(d) oblique incidence coming from port 2. At resonant frequency \( \omega = \omega_r \) the up-converted normally incident light is steered toward port 2 \( \theta = 20^\circ \). The light incoming from port 2 at \( \omega_r + \omega_m \) is bent toward port 1 at \( \theta = 0^\circ \) upon up conversion, while its amplitude is strongly suppressed. The color bars are rescaled to provide a fair comparison. The magnetic field level in (d) is varying between \(-0.01 - 0.01\).

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