*t*P40 carbon: A novel superhard carbon allotrope^{*}

Heng Liu(刘恒)¹, Qing-Yang Fan(樊庆扬)^{1,†}, Fang Yang(杨放)¹, Xin-Hai Yu(于新海)², Wei Zhang(张伟)³, and Si-Ning Yun(云斯宁)^{4,‡}

¹College of Information and Control Engineering, Xi'an University of Architecture and Technology, Xi'an 710055, China

²Department of Mechanical and Electrical Engineering, Hetao College, Bayannur Inner Mongolia 015000, China

⁴Functional Materials Laboratory, School of Materials Science and Engineering,

Xi'an University of Architecture and Technology, Xi'an 710055, China

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In this work, a novel carbon allotrope tP40 carbon with space group P4/mmm is proposed. The structural stability, mechanical properties, elastic anisotropy, and electronic properties of tP40 carbon are investigated systematically by using density functional theory (DFT). The calculated elastic constants and phonon dispersion spectra indicate that the tP40 phase is a metastable carbon phase with mechanical stability and dynamic stability. The B/G ratio indicates that tP40 carbon is brittle from 0 GPa to 60 GPa, while tP40 carbon is ductile from 70 GPa to 100 GPa. Additionally, the anisotropic factors and the directional dependence of the Poisson's ratio, shear modulus, and Young's modulus of tP40 carbon at different pressures are estimated and plotted, suggesting that the tP40 carbon is elastically anisotropic. The calculated hardness values of tP40 carbon are 44.0 GPa and 40.2 GPa obtained by using Lyakhov–Oganov's model and Chen's model, respectively, which means that the tP40 carbon can be considered as a superhard material. The electronic band gap within Heyd–Scuseria–Ernzerhof hybrid functional (HSE06) is 4.130 eV, and it is found that the tP40 carbon is an indirect and wider band gap semiconductor material.

Keywords: novel carbon allotrope, elastic properties, anisotropy, superhard material

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1. Introduction

Carbon can be widely found in the air and in Earth's crust in diverse forms; it can chemically self-associate, forming three flexible hybridization bonds (sp, sp², and sp³) in diamond, graphite, and other carbon allotropes.^[1–36] Carbon allotropes play increasingly a critical role in biology and commerce due to their complex structures and diverse properties, which are a hot research topic.

A considerable research has predicted the properties of many carbon allotropes in recent years. For example, all-sp³ hybrid carbon allotropes incorporate *Z* carbon,^[21] *T*E-C36 carbon,^[22] *K*6 carbon,^[23] *Cmmm*-C₃₂ and *P*6/*mmm*-C₅₄,^[24] and other hybridized carbons include *m*C16,^[25] *H*18 carbon,^[26] and *m*C12.^[27] In addition, several novel super-hard carbon materials have also been predicted in recent years, such as *bct*-C4,^[28] *O*-carbon,^[29] C14 carbon,^[30] and *Amm2*-carbon.^[31,32] Previous research by Li *et al.*^[33] identified a new carbon allotrope, denoted as C₉₆ carbon, with a porous nanocube network. The calculated bulk modulus and hardness of C₉₆ carbon (279 GPa and 25 GPa) are higher than those of T carbon,^[34] and it was found that C₉₆ carbon can be considered as a semiconductor material with an indirect band gap of

1.85 eV. Wang et al.^[35] proposed a cubic sp³hybridized carbon material called C₂₀-T carbon, they found that C₂₀-T carbon has a high hardness (72.76 GPa) and it is a transparent insulator with an indirect band gap 5.44 eV. In addition, the interesting structure of C₂₀-T carbon has large cavities with a diameter of about 3 Å. A potential superhard carbon material P2/m C₅₄ was proposed by Li and Xing.^[36] The P2/mC₅₄ remains stable mechanically and dynamically at 100 GPa, and the relative formation enthalpy of P2/m C₅₄ was calculated to be higher 0.581 eV/atom than that of graphite, and it is less 0.729 eV/atom than that of T carbon, and T carbon has already synthesized by Zhang et al.^[37] According to Chen et al.'s model^[38] and Lyakhov and Oganov's model,^[39] the obtained hardness of P2/m C₅₄ is 54.1 GPa and 70.4 GPa, which reveals its superhard characteristics. In addition, Zhang et al.^[24] predicted two new carbon allotropes (Cmmm-C₃₂ and $P6/mmm-C_{54}$) with a full sp³ bonding network, both of these new carbon materials have honeycomb structures. By using Lyakhov–Oganov model,^[39] the hardness values of Cmmm- C_{32} and $P6/mmr-C_{54}$ were estimated to be 83.72 GPa and 54.01 GPa, respectively, indicating that they are identified to be superhard materials.

[†]Corresponding author. E-mail: qyfan_xidian@163.com; fanqy@xauat.edu.cn

³School of Microelectronics, Xidian University, Xi'an 710071, China

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[‡]Corresponding author. E-mail: alexsyun1974@aliyun.com; yunsining@xauat.edu.cn

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In this work, based on first-principles calculations, a novel carbon allotrope, which is called tP40 carbon, is predicted to possess the space group P4/mmm in sp³ bonding networks by space group and graph theory (RG2).^[40,41] The tP40 carbon is not included in SACADA^[42] (http://sacada.sctms.ru), nor Materials Project (https://materialsproject.org/), nor Reticular Chemistry Structure Resource (RCSR,^[43,44] http://rcsr.net/). The crystal structural stability, anisotropic and electronic properties of tP40 carbon are investigated systematically.

2. Computational details and theory

The structural optimization and property calculations of tP40 carbon were completed by using density functional theory (DFT)^[46,47] as implemented in the Cambridge Serial Total Energy Package (CASTEP).^[48] The exchange-correlation (XC) energy functionals are approximated by the generalized gradient approximation (GGA) parameterized by Perdew, Burke and Ernzerr (PBE)^[49] and local density approximation (LDA).^[50] The electronic properties were investigated by utilizing the Heyd-Scuseria-Ernzerhof hybrid functional (HSE06).^[51] In this work, the energy cut-off is 400 eV for the tP40 carbon. The Brillouin zone is sampled with a $5 \times 5 \times 9$ Monkhorst–Pack special k-point grid. Vanderbilt ultrasoft pseudopotential^[52] is used, and the Broyden-Fletcher-Goldfarb-Shanno (BFGS)^[53] minimization scheme is utilized for optimizing the structural geometry. The phonon spectra of tP40 carbon under 0 GPa and 100 GPa are found by adopting the density functional perturbation theory (DFPT) approach^[54] The convergence of the total energy difference is less than 5×10^{-6} eV/atom, the maximum Hellmann-Feynman force is 0.01 eV/Å, and the self-consistent field tolerance threshold is 5×10^{-7} eV/atom. When the crystal structure under high pressure is optimized, the applied pressure is hydrostatic pressure. The elastic constants are calculated by the strain-stress method.

3. Results and discussion

3.1. Structural properties

The crystal structure of *t*P40 carbon is presented in Fig. 1. From Fig. 1, it is found that *t*P40 carbon consists of five nonequivalent carbon atoms with the space group P4/mmm. C1, C2, C3, C4, and C5 are each depicted in a different colour. The *t*P40 carbon has 40 carbon atoms in each conventional cell occupying five different Wyckoff positions: C1 8*t* (1.13577, 1.5, 0.32069), C2 4*o* (1.5, 1.28224, 1.5), C3 4*k* (1.66058, 1.33942, 0.5), C4 8*r* (1.22628, 1.77372, 0.32633), and C5 16*u* (1.09773, 1.66284, 0.17872), and the details are shown in Fig. 1(c). It is found that the minimum bond length of *t*P40 carbon is 1.434 Å, the maximum bond length is 1.644 Å, the average bond length of C-C is 1.541 Å, and it is slightly smaller than that diamond (1.544 Å). The primary reason is the bond length of the three-membered ring consisting of C1 and C2 in Fig. 1(b) (the bond length of C1-C2 is 1.462 Å) and the eight-membered ring consisting of C2 and C3 (the bond length of C2–C3 is 1.434 Å) located in the middle of Fig. 1(c) are shorter. From Figs. 1(b) and 1(c), one can see that the *t*P40 carbon has a three-membered ring, five-membered ring, sixmembered ring, eight-membered ring, and twelve-membered ring, and there is only one kind of them except for the threemembered ring. The five-membered ring consists of the C1, C2, C3, C4, and C5 atoms. The six-membered ring comprises two kinds of atoms: C1 and C4. The eight-membered ring is made up of C2 and C3 atoms. The twelve-membered ring is composed of C4 and C5 atoms. While three-membered ring consists of the C1+C2 atoms, and another way to form it is C2+C4 atoms (see Fig. 1(b)). The crystal structure of tP40carbon is similar to that of P carbon,^[45] and the crystal structure of P carbon is shown in Fig. 1(d).



Fig. 1. Crystal structure of tP40 carbon (a) along the *a* axis (b) and *b* axis (c), and crystal structure of P carbon (d).

In this work, the calculated lattice constants of *t*P40 carbon within GGA and LDA, together with those of C₉₆, *Pnma*-BN,^[55] C₆₄,^[56] C72,^[57] and diamond, are listed in Table 1. Under an ambient pressure, the lattice parameters for *t*P40 carbon are a = 8.414 Å and c = 4.383 Å in a conventional cell. When using different methods to calculate the lattice parameters of diamond, the GGA level is closer to the experimental value, so all the discussion in this work is based on the results of GGA level. The calculated results show that the volumes per carbon atom of *t*P40 carbon, C₆₄, C72, and diamond are 7.756 Å³, 6.022 Å³, 11.760 Å³, and 11.341 Å³, respectively. In addition, the obtained density of *t*P40 carbon is 2.571 g/cm³, which is lower than that of C₉₆ (2.700 g/cm³)^[33] and slightly higher than that of C₆₄ (2.562 g/cm³)^[56] and C72 (1.690 g/cm³).^[57]

Table 1. Calculated values of lattice constant (in unit Å), cell volume (in unit Å³), and density (in unit g/cm³) for *t*P40 carbon, C_{64} , *Pnma*-BN, C_{96} , and diamond.

Crystal	Method	а	b	с	V	ρ
tP40 carbon	GGA ^a	8.414		4.383	7.756	2.571
	LDA ^a	8.314		4.329	7.482	2.666
C ₆₄		7.180 ^b		2.511	6.022	2.562
Pnma-BN	GGA ^c	4.890	2.589	4.284	13.557	
	LDA ^c	4.795	2.557	4.243	13.007	
C96	PW91 ^d	9.020				2.700
	GGA ^e	9.004				
C72		9.460^{f}			11.760	1.690
Diamond	GGA ^a	3.566			11.341	
		3.566 ^g			11.337	
	LDA ^a	3.526			10.961	
		3.525 ^g			10.950	
	Exp. ^h	3.567			11.346	

^aThis work, ^bRef. [56], ^cRef. [55], ^dRef. [33], ^eRef. [58], ^fRef. [57], ^gRef. [59], ^hRef. [60].



Fig. 2. Plots of ratios of (a) a/a_0 , c/c_0 and (b) V/V_0 versus pressure for tP40 carbon, C₉₆ carbon, P222₁ carbon, c-BN carbon, and diamond.

The ratios of a/a_0 , c/c_0 , and V/V_0 each as a function of pressure for *t*P40 carbon, C₉₆, *P*222₁, c-BN, and diamond are plotted in Fig. 2, where a_0 , c_0 , and V_0 are the lattice constants and cell volume at zero pressure, respectively. The values of a/a_0 , c/c_0 , and V/V_0 for these materials decrease at different rates as the pressure increases. There is no doubt that diamond is the most difficult to compress carbon material, because its hardness is the highest in nature. The values of a/a_0 and c/c_0 can be related to the compressibility of material. Thus, when hydrostatic pressure is applied to *t*P40 carbon, it is more easily compressed along the *c* axis. From Fig. 2(a), it can be easily seen that the a/a_0 ratio of *t*P40 carbon is larger than that of C₉₆, which indicates that *t*P40 carbon is less likely to be compressed along the *a* axis than C₉₆, when subjected to hydrostatic pressure. As is well known, the value of V/V_0 is related to the bulk modulus of the material, and the curve of diamond is the highest in all the materials under study here, so its bulk modulus is the largest. Apparently, the volume ratio V/V_0 of *t*P40 carbon is smaller than that of c-BN and P222₁ carbon. Therefore, it can be predicted that the bulk modulus of *t*P40 carbon is smaller than that of c-BN carbon and P222₁ carbon.

3.2. Elastic properties

To study the mechanical properties of *t*P40 carbon, the elastic constants C_{ij} , the bulk modulus, shear modulus, and Young's modulus for each of *t*PC₄₀ carbon, C₆₄, *Pnma*-BN, C₉₆, C72, and diamond are presented in Table 2. According to the elastic constants (C_{11} , C_{12} , C_{13} , C_{33} , C_{44} , C_{66}) given in Table 2, the mechanically stability of *t*P40 carbon can be estimated based on the criteria as follows: $C_{11} > |C_{12}|$, $2C_{13}^2 < C_{33}(C_{11}+C_{12}), C_{44} > 0, C_{66} > 0.$ ^[61] The calculated results show that the elastic constants satisfy the mechanical stability criteria. Therefore, *t*P40 carbon is mechanically stable under ambient pressure. To obtain more information about dynamical stability, the phonon spectra for *t*P40 carbon at 0 GPa and 100 GPa are shown in Fig. 3. There is no imaginary frequency in the whole Brillouin zone, which indicates that *t*P40 carbon is dynamically stable at 100 GPa.



Fig. 3. Phonon spectra for tP40 carbon at (a) 0 GPa and (b) 100 GPa.

Voigt states that the Voigt bond is the upper limit of the actual polycrystalline constant, whereas the Reuss bound is the lower limit. Based on the Hill approximation, the values of the bulk modulus B and the shear modulus G are equal to the arithmetic mean of the Voigt and Reuss and are expressed as^[63] $G = (G_{\rm R} + G_{\rm V})/2$ and $B = (B_{\rm R} + B_{\rm V})/2$. The calculated results show that the bulk modulus of tP40 carbon (259 GPa) is larger than that of C72 (183 GPa) and slightly smaller than that of C₆₄ (264 GPa), Pnma-BN (298 GPa), P carbon (334 GPa), and C_{96} (279 GPa). The value of B for tP40 carbon is about 66.4% of the bulk modulus for diamond (431 GPa). Of all the materials under study, C72 has the lowest bulk modulus. Additionally, it can be observed that the tP40 carbon has a higher shear modulus than the other four carbon materials except for diamond and P carbon, and the shear modulus of C72 is still the lowest. Young's modulus and Poisson's ratio are given by E = 9BG/(3B+G) and v = (3B-2G)/[2(3B+G)].^[63–65] The calculated Young's modulus of tP40 carbon is 540 GPa, which is greater than that of C_{64} by approximately 5.88%, C₉₆ by approximately 3.65%, C72 by approximately 172.72%, and slightly smaller 3 GPa than that of Pnma-BN. By using Chen's model^[38] and Lyakhov–Oganov's model,^[39] the hardness of tP40 carbon is 40.2 GPa and 44.0 GPa, respectively, slightly harder than that of Pnma-BN (33.0 GPa using Lyakhov-Oganov's model, which is in excellent agreement with the reported 33.3 GPa^[55]). Thus, it can be considered to be a superhard carbon material. The value of v for the tP40 carbon is 0.152 within GGA, which is lower than that of C72 (0.310) and C₆₄ (0.178) and higher than that of diamond (0.070). According to Pugh's research,^[66] the ratio of bulk to shear modulus (B/G) can be naturally related to the brittleness and ductility of crystal. If B/G > 1.75, the material is usually ductile; otherwise, it is brittle. The calculated B/G ratios of tP40 carbon under different pressures are listed in Table 3. In the case of tP40 carbon, the calculated results suggest that the tP40 carbon is brittle from 0 GPa to 60 GPa and that when the pressure exceeds 70 GPa, the tP40 carbon becomes ductile.

The elastic constants, bulk modulus *B*, shear modulus *G*, and Young's modulus *E* under pressures from 0 GPa to 100 GPa are illustrated in Fig. 4. In general, the elastic parameters of bulk modulus, shear modulus, and Young's modulus all increase at different rates as the pressure increases. The C_{44} and C_{66} of tP40 carbon increase slowly, whereas the C_{11} and C_{12} increase faster than the other parameters. The degree of dependence of the elastic parameters *B*, *G*, and *E* on pressure are calculated to be 3.36, 0.45, and 1.84, respectively, which indicates that the tP40 carbon has the fastest increase in bulk modulus and the slowest increase in shear modulus.

Table 2. Calculated values of elastic constants of C_{ij} (in unit GPa), bulk modulus *B* (in unit GPa), shear modulus *G* (in unit GPa), Young's modulus *E* (in unit GPa), Poisson's ratio *v*, and *B/G* ratio for each of *t*P40 carbon, C_{64} , *Pnma*-BN, C_{96} , C72, and diamond.

	<i>t</i> P40	$C_{64}{}^a$	Pnma-BN ^b	C_{96} ^c	C72 ^d	P carbon ^e	Diamond	Diamond ^f
<i>C</i> ₁₁	542	598	392	623	273	754	1053	1076
C_{12}	174		99	108	139	152	120	125
C_{13}	82		256			56		
C_{22}			770					
C ₂₃			116					
C_{33}	575	677	675			979		
C_{44}	240	254	299	194	81	401	563	577
C_{55}			272					
C_{66}	261		187			285		
В	259	264	298	279	183	334	431	442
G	234	217	227	219	75	360	522	
Ε	540	510	543	521	198	795	1116	
v	0.152	0.178			0.310	0.104	0.070	
B/G	1.106	1.220			2.46	0.928	0.826	

^aRef. [56], ^bRef. [55], ^cRef. [33], ^dRef. [57], ^eRef. [45], ^fRef. [62]-experimental.

The elastic Debye temperature Θ_D and the average sound velocity v_m are related by the expression^[67,68] $\Theta_D = v_m (h/k_B)[3n/(4\pi)(N_A\rho/M)]^{1/3}$, where *k* is Boltzmann's constant, *h* is Planck's constant, *n* is the number of atoms in the molecule, N_A is Avogadro's number, ρ is the density, and *M* is the molecular weight. Additionally, $v_m = [(2/v_s^3 + 1/v_p^3)/3]^{-1/3}$. The values of shear wave velocity (v_s) and compressional wave velocity (v_p) are estimated from Navier's equations: $v_s = (G/\rho)^{1/2}$ and $v_p = [(B+4G/3)/\rho]^{1/2}$. The calculation results of the average sound velocity, compressional and shear wave velocities, Debye temperature Θ_D , and B/G ratio results for tP40 carbon at different pressures are listed in Table 3. It is found that the Debye temperatures of tP40 carbon are 1579 K and 1682 K at 0 GPa and 100 GPa, respectively, and Θ_D generally increases with pressure increasing. The obtained Debye temperature of *Pnma*-BN is determined to be 1504 K at zero pressure by Ma *et al.*,^[55] which is slightly smaller than that of tP40 carbon. Fan *et al.*,^[69] calculated and discussed the Θ_D of *Pbca*-BN (1734 K), diamond (2230 K),^[70] Diamondyne (422 K)^[71] at ambient pressure. Of all the materials mentioned in this work, diamond has the highest Θ_D and is the hardest material, and the Debye temperatures of Diamondyne is the lowest.



Fig. 4. Plots of (a) elastic constants and (b) B, G, and E for tP40 carbon *versus* pressures.

Table 3. Estimated shear wave velocity (v_s) , compressional wave velocity (v_p) , average sound velocity v_m , Debye temperature Θ_D , and B/G ratio results for *t*P40 carbon.

	$v_{\rm p}/({\rm m/s})$	$v_{\rm s}/({\rm m/s})$	$v_{\rm m}/({\rm m/s})$	$\Theta_{\rm D}/{\rm K}$	B/G
0	14908	9545	10487	1579	1.106
10	15271	9568	10538	1606	1.229
20	15483	9447	10434	1607	1.352
30	15886	9546	10559	1641	1.435
40	16039	9387	10409	1633	1.586
50	16280	9397	10443	1649	1.668
60	16584	9504	10558	1681	1.712
70	17051	9578	10659	1701	1.847
80	16898	9356	10423	1682	1.929
90	17036	9278	10349	1680	2.039
100	17184	9227	10303	1682	2.134

3.3. Elastic anisotropy

The shear anisotropic coefficient can provide important information concerning the anisotropy of bonding between atoms in different planes. The shear anisotropic coefficient A_1 for the (101) shear plane between [011] and [010] is $A_1 = 4C_{44}/(C_{11} + C_{33} - 2C_{13})$;^[72] for the (010) shear plane between [101] and [001], $A_2 = 4C_{55}/(C_{22} + C_{33} - 2C_{23})$;^[72] and for the (001) shear plane between [110] and [010], $A_3 =$ $4C_{66}/(C_{11} + C_{22} - 2C_{12})$.^[72] The anisotropy of the bulk modulus along the *a* axis and *c* axis relative to that along the *b* axis are taken as $A_{Ba} = B_a/B_b$ and $A_{Bc} = B_c/B_b$,^[73] respectively. The bulk modulus along the *a* axis, *b* axis, and *c* axis are B_a , B_b , and B_c , respectively, which can be given by^[73] $B_a = \Lambda/(1 + \alpha + \beta)$, $B_b = B_a \alpha$, and $B_c = B_a/\beta$, whereas $\Lambda = C_{11} + 2C_{12} + C_{22}\alpha^2 + 2C_{13}\beta + C_{33}\beta^2 + 2C_{23}\alpha\beta$, $\alpha = [(C_{11} - C_{12})(C_{33} - C_{13}) - (C_{23} - C_{13})(C_{11} - C_{13})]/[(C_{33} - C_{13})(C_{11} - C_{13})(C_{11} - C_{13})]/[(C_{13} - C_{13})(C_{11}$ $(C_{13})(C_{22}-C_{12})-(C_{13}-C_{23})(C_{11}-C_{13})]$, and $\beta = [(C_{22}-C_{13})(C_{13}-C_{13})]$ $C_{12})(C_{11}-C_{13})-(C_{11}-C_{12})(C_{23}-C_{12})]/[(C_{22}-C_{12})(C_{33}-C_{12})]/[(C_{22}-C_{12})(C_{33}-C_{12})]/[(C_{22}-C_{12})(C_{33}-C_{12})]/[(C_{22}-C_{12})(C_{33}-C_{12})]/[(C_{22}-C_{12})(C_{33}-C_{12})]/[(C_{23}-C_{12})(C_{33}-C_{12})]/[(C_{23}-C_{12})(C_{33}-C_{12})]/[(C_{23}-C_{12})(C_{33}-C_{12})]/[(C_{23}-C_{12})(C_{33}-C_{12})]/[(C_{23}-C_{12})(C_{33}-C_{12})]/[(C_{23}-C_{12})(C_{23}-C_{12})]/[(C_{23}-C_{12})(C_{23}-C_{12})]/[(C_{23}-C_{12})(C_{23}-C_{12})(C_{23}-C_{12})]/[(C_{23}-C_{12})(C_{13}-C_{12})(C_{13}-C_{12})(C_{13}-C_{12})(C_{13}-C_{12}$ $(C_{13}) - (C_{12} - C_{23})(C_{13} - C_{23})]$. The calculated anisotropy factors $A_1, A_3, B_a, B_c, A_{Ba}$, and A_{Bc} are listed in Table 4. The values of shear anisotropic coefficients A_1, A_2 , and A_3 are important indices to measure whether the crystal has anisotropy. If A_1, A_2 , and A_3 are all equal to 1, then the material is isotropic; otherwise, it is anisotropic. Our results indicate that the tP40carbon is an elastic anisotropic crystal. The shear anisotropic factor A1 decreases by 19.35% from 0 GPa to 100 GPa, and shear anisotropic factor A_3 deceases from 0 GPa to 40 GPa, but increases from 50 GPa to 100 GPa. Apparently, the bulk modulus along the *a*-axis B_a has the same value along the *b*axis B_b , and B_a and B_c both increase with pressure rising. The obtained directional bulk modulus B_a is greater than B_c , which means that the compressibility along the c axis is the largest. The estimated anisotropy of the bulk modulus along the a-axis A_{Ba} is equal to 1 at all pressures. The values of A_{Bc} , which represent the anisotropy of the bulk modulus along the b axis and c axis, decrease with pressure increasing, while it reaches a maximum value at 70 GPa.

Table 4. Anisotropy factors of tP40 carbon from 0 GPa to 100 GPa.

Pressure	A_1	A_3	B_a	B_c	A _{Ba}	$A_{\rm Bc}$
0	1.008	1.421	807.58	721.47	1.00	0.893
10	0.994	1.487	928.01	817.32	1.00	0.881
20	0.981	1.491	1044.87	908.75	1.00	0.870
30	0.940	1.022	1179.82	990.59	1.00	0.840
40	0.932	0.932	1295.93	1081.51	1.00	0.835
50	0.922	0.984	1403.18	1160.81	1.00	0.827
60	0.910	1.159	1508.43	1241.13	1.00	0.823
70	0.765	1.307	1561.37	1619.36	1.00	1.037
80	0.865	1.338	1724.73	1394.34	1.00	0.808
90	0.825	1.440	1838.87	1456.74	1.00	0.792
100	0.813	1.567	1942.09	1529.97	1.00	0.788

To visualize and ensure the elastic anisotropy of *t*P40 carbon, the directional dependence of the shear modulus, Young's modulus, and Poisson's ratio at different pressures are plotted in Fig. 5. The directional dependence of the shear modulus, Young's modulus, and Poisson's ratio are predicted by Elastic Anisotropy Measures (ElAM) code.^[74] If a material is isotropic, then its three-dimensional surface constructions of shear modulus, Young's modulus, and Poisson's ratio appear as sphere,^[64,75–77] and the measured performance values of the material in different directions are exactly the same, while the degree of deviation from the sphere reflects the strength of anisotropy. It can be clearly seen from Fig. 5 that the three-dimensional surface constructions of Young's modulus under different pressures are not of sphere, which indicates that the materials show anisotropy. When the pressure is 100 GPa,

the three-dimensional shape deviates most from the sphere, indicating that the anisotropy is greater at 100 GPa than that at 0 GPa and 50 GPa. To investigate the elastic anisotropy of tP40 carbon in more detail, the maximum, minimum values of Young's modulus, shear modulus, and Poisson's ratio, and $X_{\text{max}}/X_{\text{min}}$ (X = E, G, v) of tP40 carbon are calculated and listed in Table 5. For anisotropic materials, the maximum and minimum values of Young's modulus, shear modulus, and Poisson's ratio measured in all directions are the same, so the ratio of the maximum value to the minimum value should be 1. The $E_{\text{max}}/E_{\text{min}} = 1.24$, $G_{\text{max}}/G_{\text{min}} = 1.42$, and $v_{\text{max}}/v_{\text{min}} = 3.44$ at ambient pressure, which suggests that the tP40 carbon shows elastic anisotropy. It can be seen in Table 5 that as the pressure increases the change of the anisotropy in the shear modulus, Young's modulus, and Poisson's ratio for tP40 carbon are irregular. Note that the tP40 carbon shows the weakest elastic anisotropy at 30 GPa. Furthermore, the anisotropy in Young's modulus and Poisson's ratio are the largest at 70 GPa, and the anisotropy in Poisson's ratio is the strongest at 100 GPa. The values of $X_{\text{max}}/X_{\text{min}}$ (X = E, (G, v) for diamond at the ambient pressure is 1.15, 1.21, and 11.00, respectively, which suggests that the tP40 carbon exhibits greater elastic anisotropy in Young's modulus and shear modulus and weaker elastic anisotropy in the Poisson's ratio than that of diamond.

To obtain more information about the mechanical anisotropy of Young's modulus, the maximum and minimum Young's modulus, and the value of $E_{\text{max}}/E_{\text{min}}$ in the (100), (010), (011), (101), (001), (110), and (111) planes are shown in Table 6. As is exhibited in Table 6, the maximum and minimum values of Young's modulus are consistent among some planes, such as the (100) and (010) planes, and the (011) and (101) planes. In the range from 0 GPa to 20 GPa, the anisotropy of the Young's modulus is the smallest along the (110) direction and the largest along the (001) direction. However, when the pressure is at 30 GPa, the anisotropy in the Young's modulus is the weakest in the (001) plane and the strongest in the (100) and (010) planes. At zero pressure, the value of $E_{\text{max}}/E_{\text{min}}$ of diamond is 1.11 in the (100), (010), and (001) planes, 1.15 in the (011), (101), and (110) planes, and 1.00 in the (111) plane, indicating that tP40 carbon exhibits weaker elastic anisotropy in the (110) plane and stronger anisotropy in the other six mean planes than diamond.



Fig. 5. Directional dependence of Young's modulus at (a) 0 GPa, (b) 50 GPa, and (c) 100 GPa; the shear modulus at (d) 0 GPa, (e) 50 GPa, and (f) 100 GPa; and Passion's ratio at (g) 0 GPa, (h) 50 GPa, and (i) 100 GPa for *t*P40 carbon.

Table 5. Mximum values and minimum values of Young's modulus (in unit GPa), shear modulus (in unit GPa), and Poisson's ratio and $E_{\text{max}}/E_{\text{min}}$, $G_{\text{max}}/G_{\text{min}}$, and $v_{\text{max}}/v_{\text{min}}$ for tP40 carbon.

	E _{max}	E _{min}	Ratio	G _{max}	G_{\min}	Ratio	v _{max}	v _{min}	Ratio
0	595	480	1.24	261	184	1.42	0.31	0.09	3.44
10	631	490	1.29	272	180	1.51	0.37	0.10	3.70
20	651	500	1.30	283	177	1.60	0.41	0.11	3.73
30	683	607	1.13	282	225	1.25	0.35	0.14	2.50
40	718	584	1.23	286	207	1.38	0.41	0.14	2.93
50	748	619	1.21	293	219	1.34	0.41	0.15	2.73
60	779	635	1.23	314	223	1.41	0.43	0.15	2.87
70	994	626	1.59	368	212	1.74	0.48	0.12	4.00
80	835	621	1.34	335	208	1.61	0.49	0.15	3.27
90	864	615	1.41	348	202	1.72	0.52	0.15	3.47
100	888	604	1.47	358	195	1.84	0.55	0.14	3.92

Table 6. Maximum and minimum Young's moduli and the values of E_{max}/E_{min} in different planes at different pressures for tP40 carbon.

р	(100) (010)		(((011) (101)			(001)			(110)				(111)				
1 .	E _{max}	E _{min}	Ratio	E _{max}	E _{min}	Ratio	Em	ax E	Emin	Ratio	-	Emax	E _{min}	Ratio		E _{max}	Emin	Ratio
0	555	480	1.16	562	480	1.17	59	5 4	480	1.24		595	548	1.09		595	520	1.14
10	604	490	1.23	595	490	1.21	63	1 4	490	1.29		631	585	1.08		631	543	1.16
20	645	500	1.29	618	500	1.24	65	1 5	500	1.30		651	613	1.06		651	563	1.16
30	683	607	1.13	627	607	1.03	61	66	607	1.01		683	615	1.11		642	614	1.05
40	718	614	1.17	645	607	1.06	61	4 5	584	1.05		718	584	1.23		660	584	1.13
50	748	626	1.19	662	626	1.06	62	66	619	1.01		748	619	1.21		683	619	1.10
60	779	635	1.23	688	635	1.08	70	4 6	635	1.11		779	688	1.17		710	665	1.07
70	994	626	1.59	708	626	1.13	75	8 6	626	1.21		994	708	1.40		765	665	1.15
80	835	621	1.34	713	621	1.15	76	5 6	621	1.23		835	711	1.74		765	664	1.15
90	864	615	1.40	720	615	1.17	80	1 6	615	1.30		864	713	1.21		801	675	1.19
100	888	604	1.47	735	604	1.22	83	96	604	1.39		888	725	1.22		839	656	1.28

3.4. Electronic properties

As is well known, the band structure provides important information concerning the electronic and optical properties of materials. The obtained band structures with DFT and HSE06 and the total and partial density of states (PDOS) of tP40 carbon at zero pressure are illustrated in Fig. 6. The dashed line in Fig. 6 represents the Fermi level. The valence band maximum (VBM) is located at the Γ point, and the conduction band minimum (CBM) is located between the Γ point and Z point, which indicates that the tP40 carbon presents an indirect semiconducting character. The band gap calculated by DFT is 3.088 eV. As is well known, the band gap calculated by density functional theory is usually underestimated by 30%–50%. Therefore, the band gap of tP40 carbon with HSE06 hybrid functional is 4.130 eV. To obtain more information about the electronic band structure, the partial density of states of tP40 carbon is shown in Fig. 6(c). It can be noted that the distribution disciplines of these five atoms in different energy ranges are different. For C1, C2, and C3 atoms, the main contribution comes from the s orbital with energy ranging from -23 eVto -20 eV, the contribution of the s orbital is very small compared with the p orbital with energy in a range from -21 eV to Fermi energy, and the contribution from the p orbital is great compared with that from the s orbital in an energy range from 4 eV to 8 eV. For C4 atom, the density of states (DOS) can be divided into three parts: the lower energy part (-23 eV to -15 eV) where the peak mainly originates from the s orbital, the part where the states from -15 eV to Fermi energy are mainly due to the contribution of the p orbital, and the part where the peak appears on condition that the band DOS (4 eV to 8 eV) of the DOS is mainly due to the contribution of the p orbital. Regarding the DOS of C5 atom, the contribution from the p orbital is very small in the lowest band (-23 eV to -12.5 eV), the main contribution comes from the p orbital in the middle band (-12.5 eV to 0 eV), and the contribution from the p orbital is great compared with that from the s orbital in the upper band (4 eV to 8 eV). The DOS for tP40 carbon at zero pressure can be summarized as follows: (i) in the energy range below -12.5 eV, the contribution from the s orbital of the carbon atoms is larger than that from the p orbital; (ii) the peak present in the energy part (-12.5 eV to 8 eV) of the DOS mainly originates from the p orbital; (iii) the peak present in the energy part (4 eV to 8 eV) of the DOS mainly originates from the p orbital of C1, C3, C4, and C5, while the contribution of p orbital electron of C2 atom is smaller than that of carbon atom at other positions.



Fig. 6. Electronic band phases according to (a) DFT, (b) HSE06, and (c) DOS for tP40 carbon at zero pressure.

4. Conclusions

In this work, a new carbon allotrope tP40 carbon is theoretically predicted, and its structural properties, elastic properties, and anisotropy are investigated with first-principles calculations. By studying the elastic constants and phonon spectra, the tP40 carbon is found to be stable mechanically and dynamically. The tP40 carbon is brittle in a pressure range from 0 GPa to 60 GPa, but becomes ductile when the pressure exceeds 70 GPa. The obtained bulk modulus, shear modulus, and Young's modulus of tP40 carbon are 259 GPa, 234 GPa, and 540 GPa, respectively, which are larger than those of C72. The hardness of tP40 carbon is 44.0 GPa, indicating that the tP40 carbon can be considered to be a superhard material. The directional dependence of shear modulus, Young's modulus, Poisson's ratio, and the $X_{\text{max}}/X_{\text{min}}$ indicate that the *t*P40 carbon shows elastic anisotropy. Comparing with diamond, the anisotropy in shear modulus and Young's modulus of *t*P40 carbon are larger, but in the Poisson's ratio, *t*P40 carbon exhibits smaller elastic anisotropy. The band structure of *t*P40 carbon indicates that it is an indirect band gap with a 4.130-eV band gap within HSE06, indicating that the *t*P40 carbon is a semiconductor material with an indirect and wider band gap.

References

- [1] Xing M, Li B, Yu Z and Chen Q 2015 J. Mater. Sci. 50 7104
- [2] Zhang W, Chai C, Fan Q, Song Y and Yang Y 2020 ChemNanoMat 6 139
- [3] Wang J T, Chen C, Mizuseki H and Kawazoe Y 2018 Phys. Chem. Chem. Phys. 20 7962
- [4] Zhang W, Chai C, Song Y, Fan Q and Yang Y 2020 J. Phys.: Condens. Matter 32 355701
- [5] Fan Q Y, Wang H, Song Y X, Zhang W and Yun S N 2020 Comput. Mater. Sci. 178 109634
- [6] Cheng J, Zhang Q 2020 Materials 13 2079
- [7] Wei Q, Zhao C Y, Zhang M G, Yan H Y, Zhou Y J and Yao R H 2018 *Phys. Lett. A* 382 1685
- [8] Wang J T, Weng H, Nie S, Fang Z, Kawazoe Y and Chen C 2016 Phys. Rev. Lett. 116 195501
- [9] Li Z, Hu M, Ma M, Gao Y, Xu B, He J, Yu D, Tian Y and Zhao Z 2016 Carbon 105 151
- [10] Lv Y, Wang H, Guo Y, Jiang B and Cai Y 2018 Comput. Mater. Sci. 144 170
- [11] Yang X, Yao M, Wu X, Liu S, Chen S, Yang K, Liu R, Cui T, Sundqvist B and Liu B 2017 Phys. Rev. Lett. 118 245701
- [12] He C, Zhang C, Xiao H, Meng L and Zhong J 2017 Carbon 112 91
- [13] Xing M J, Li B H, Yu Z T and Chen Q 2015 Commun. Theor. Phys. 64 237
- [14] Zhao C X, Niu C Y, Qin Z J, Ren X Y, Wang J T, Cho J H and Jia Y 2016 Sci. Rep. 6 21879
- [15] Fan Q, Zhao Y, Yu X, Song Y, Zhang W and Yun S 2020 *Diamond Relat. Mater.* **106** 107831
- [16] Li Z, Chen J, Nie S, Xu L, Mizuseki H, Weng H and Wang J T 2018 Carbon 133 39
- [17] Cui H J, Yan Q B, Sheng X L, Wang D L, Zheng Q R and Su G 2017 *Carbon* 120 89
- [18] Zhang W, Chai C, Fan Q, Song Y and Yang Y 2020 Materials 13 1926
- [19] Niu H, Chen X Q, Wang S, Li D, L. Mao W and Li Y 2012 Phys. Rev. Lett. 108 135501
- [20] Liu L, Hu M, Zhao Z, Pan Y and Dong H 2020 Carbon 158 546
- [21] Amsler M, Flores-Livas J A, Lehtovaara L, Balima F, Ghasemi S A, Machon D, Pailhès S, Willand A, Caliste D, Botti S, Miguel A S, Goedecker S and Marques M A L 2012 *Phys. Rev. Lett.* **108** 065501
- [22] Xu Y, Lu Y, Zhu X and Wang M 2018 RSC Adv. 8 1846
- [23] Niu C Y, Wang X Q and Wang J T 2014 J. Chem. Phys. 140 054514
- [24] Zhang W, Chai C, Fan Q, Song Y and Yang Y 2019 J. Appl. Phys. 126 145704
- [25] Zhang Z G, Liu H Y and Zhang M 2014 Europhys. Lett. 108 46006
- [26] Zhao C X, Niu C Y, Qin Z J, Ren X Y, Wang J T, Cho J H and Jia Y 2016 Sci. Rep. 6 21879
- [27] Wei Q, Zhang Q, Zhang M G, Yan H Y, Guo L X and Wei B 2018 Front. Phys. 13 136105
- [28] Umemoto K, Wentzcovitch R M, Saito S and Miyake T 2010 Phys. Rev. Lett. 104 125504
- [29] Wang J T, Chen C F and Kawazoe Y 2012 Phys. Rev. B 85 033410
- [30] Yang X, Lv C, Liu S, Zang J, Qin J, Du M, Yang D, Li X, Liu B and Shan C X 2020 *Carbon* 156 309
- [31] Zhang X X, Wang Y C, Lv J, Zhu C Y, Li Q, Zhang M, Li Q and Ma Y 2013 J. Chem. Phys. 138 114101
- [32] Xing M J, Li X Z, Yu S J and Wang F Y 2017 Commun. Theor. Phys. 68 395
- [33] Li D, Tian F B, Chu B H, Duan D F, Wei S L, Lv Y Z, Zhang H D, Wang L, Lu N, Liu B B and Cui T 2015 J. Mater. Chem. A 3 10448
- [34] Sheng X L, Yan Q B, Ye F, Zheng Q R and Su G 2011 Phys. Rev. Lett. 106 155703

- [35] Wang J Q, Zhao C X, Niu C Y, Sun Q and Jia Y 2016 J. Phys.: Condens. Matter 28 475402
- [36] Li X and Xing M 2020 Mater. Chem. Phys. 242 122480
- [37] Zhang J, Wang R, Zhu X, Pan A, Han C, Li X, Dan Z, Ma C, Wang W, Su H and Niu C 2017 Nat. Commun. 8 683
- [38] Chen X Q, Niu H Y, Li D Z and Li Y Y 2011 Intermetallics 19 1275
- [39] Lyakhov A O and Oganov A R 2011 Phys. Rev. B 84 92103
- [40] Shi X, He C, Pickard C J, Tang C and Zhong J 2018 Phys. Rev. B 97 014104
- [41] He C, Shi X, Clark S J, Li J, Pickard C J, Ouyang T, Zhang C, Tang C and Zhong J 2018 Phys. Rev. Lett. 121 175701
- [42] Hoffmann R, Kabanov A A, Golov A A and Proserpio D M 2016 Angew. Chem. Int. Ed. 55 10962
- [43] O'Keeffe M, Yaghi O M and Ramsden S, Reticular Chemistry Structure Resource, Australian National University Supercomputer Facility, http://rcsr.anu.edu.au/, accessed 5th March 2013
- [44] O'Keeffe M, Peskov M A, Ramsden S and Yaghi O M 2008 Chem. Res. 41 1782
- [45] Pan Y, Xie C, Xiong M, Ma M, Liu L, Li Z, Zhang S, Gao G, Zhao Z, Tian Y, Xu B and He J 2017 *Chem. Phys. Lett.* 689 68
- [46] Hohenberg P and Kohn W 1964 Phys. Rev. 136 B864
- [47] Kohn W and Sham L J 1956 Phys. Rev. 140 A1133
- [48] Clark S J, Segall M D, Pickard C J, Hasnip P J, Probert M I J, Refson K and Payne M C 2005 Z. Kristallogr 220 567
- [49] Perdew J P, Burke K and Ernzerhof M 1996 Phys. Rev. Lett. 77 3865
- [50] Ceperley D M and Alder B J 1980 Phys. Rev. Lett. 45 566
- [51] Krukau A V, Vydrov O A, Izmaylov A F and Scuseria G E 2006 J. Chem. Phys. 125 224106
- [52] Vanderbilt D 1990 *Phys. Rev. B* **41** 7892
- [53] Pfrommer B G, Côté M, Louie S G and Cohen M L 1997 J. Comput. Phys. 131 233
- [54] Baroni S, de Gironcoli S, dal Corso A and Giannozzi P 2001 Rev. Mod. Phys. 73 515
- [55] Ma Z, Han Z, Liu X, Yu X, Wang D and Tian Y 2017 Nanomaterials 7 3

- [56] Wei Q, Zhang Q, Yan H Y and Zhang M G 2017 J. Mater. Sci. 52 2385
- [57] Ma J L, Song D L, Wu Y L, Fu Z F, Zhou J P, Liu P, Zhu X and Wei Q 2020 Phys. Lett. A 384 126325
- [58] Xing M, Li B, Yu Z and Chen Q 2016 Eur. Phys. J. B 89 9
- [59] Fan Q, Wei Q, Chai C, Yan H, Zhang M, Lin Z, Zhang Z, Zhang J and Zhang D 2015 J. Phys. Chem. Solids 79 89
- [60] Petrescu M L 2004 Diamond Relat. Mater. 13 1848
- [61] Mouhat F and Coudert F X 2014 Phys. Rev. B 90 224104
- [62] Grimsditch M, Zouboulis E S and Polian A 1994 J. Appl. Phys. 76 832
- [63] Hill R 1952 Proc. Phys. Soc. London 65 349
- [64] Fan Q, Zhang W, Song Y, Zhang W and Yun S 2020 Semicond. Sci. Technol. 35 055012
- [65] Fan Q, Niu R, Zhang W, Zhang W, Ding Y and Yun S 2019 ChemPhysChem 20 128
- [66] Pugh S F 1954 Philos. Mag. 45 823
- [67] Anderson O L 1963 J. Phys. Chem. Solids 24 909
- [68] Panda K B and Ravi K S 2006 Comput. Mater. Sci. 35 134
- [69] Fan Q, Wei Q, Yan H, Zhang M, Zhang Z, Zhang J and Zhang D 2014 Comput. Mater. Sci. 85 80
- [70] Fan Q, Chai C, Wei Q, Wong K, Liu Y and Yang Y 2018 J. Mater. Sci. 53 2785
- [71] Fan Q, Duan Z, Song Y, Zhang W, Zhang Q and Yun S 2019 Materials 12 3589
- [72] Connétable D and Thomas O 2009 Phys. Rev. B 79 094101
- [73] Ravindran P, Fast L, Korzhavyi P A, Johansson B, Wills J and Eriksson O 1998 J. Appl. Phys. 84 4891
- [74] Marmier A, Lethbridge Z A D, Walton R I, Smith C W, Parker S C and Evans K E 2010 Comput. Phys. Commun. 181 2102
- [75] Ma Z Y, Wang P, Yan F, Shi C L and Tian Y 2019 Chin. Phys. B 28 036101
- [76] Zhang Q, Zou Y, Fan Q and Yang Y 2020 Materials 13 1280
- [77] Hu W C, Liu Y, Li D J, Zeng X Q and Xu C S 2014 Comput. Mater. Sci. 83 27