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# Ultra-short-pulse high-average-power megahertz-repetition-rate coherent extreme-ultraviolet light source

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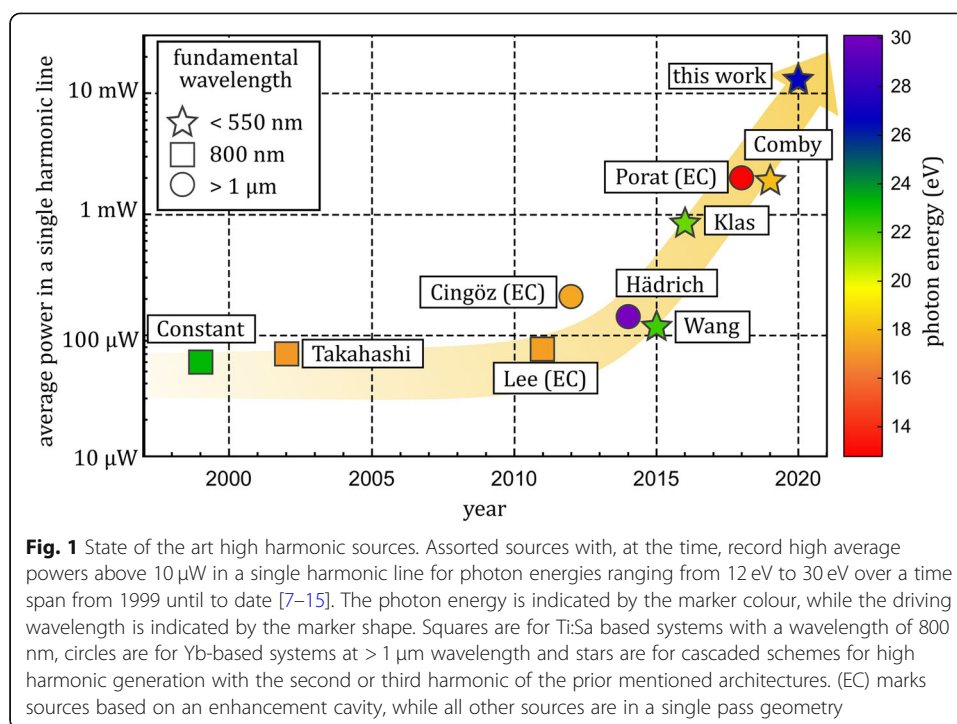
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## Abstract

High harmonic generation (HHG) enables coherent extreme-ultraviolet (XUV) radiation with ultra-short pulse duration in a table-top setup. This has already enabled a plethora of applications. Nearly all of these applications would benefit from a high photon flux to increase the signal-to-noise ratio and decrease measurement times. In addition, shortest pulses are desired to investigate fastest dynamics in fields as diverse as physics, biology, chemistry and material sciences. In this work, the up-to-date most powerful table-top XUV source with  $12.9 \pm 3.9$  mW in a single harmonic line at 26.5 eV is demonstrated via HHG of a frequency-doubled and post-compressed fibre laser. At the same time the spectrum supports a Fourier-limited pulse duration of sub-6 fs in the XUV, which allows accessing ultrafast dynamics with an order of magnitude higher photon flux than previously demonstrated. This concept will greatly advance and facilitate applications of XUV radiation in science and technology and enable photon-hungry ultrafast studies.

## Introduction

Since the first experimental demonstration of high harmonic generation in the late 1980s [1, 2], strong efforts have been made to enhance the average power of laser-like sources in the XUV [3], enabling applications on the atomic length-(nanometer) [4] and time-scale (femtosecond to attosecond) [5, 6]. In the early stages up to the year 2010 (Fig. 1), Ti:Sa based amplifiers have been proven as an effective driver for HHG [3, 7, 8], since they provide ultra-short pulse durations ( $\sim 25$  fs) at 800 nm wavelength and high pulse energies (several millijoule). However, their limited average power of a few tens of watts in best case [16], limited the XUV flux of such systems to sub-100  $\mu$ W per harmonic line (Fig. 1). An increase in XUV average power would help for example to mitigate space charge effects in photoelectron emission spectroscopy [17] (at high repetition rates), as well as to shorten acquisition times and, hence, enhance the signal-to-noise ratio in (time-resolved) coincidence measurements [18], XUV-absorption spectroscopy [19], XUV-ionization spectroscopy [20], coherent diffractive imaging of ultrafast magnetization dynamics [21], fluorescence spectroscopy [22] and



XUV-pump XUV-probe experiments [23, 24], among others. Furthermore, shortest pulses are desired to investigate fastest dynamics in atoms [6, 25], molecules [26], ions [23], solids [19] and compound materials [27].

Inherently, an increase in XUV average power can be achieved with high average power driving lasers. In recent years, enhancement cavities [9, 10] as well as Yb-based fibre lasers [11], which are capable of much higher average powers in the kilowatt regime (enabling megahertz repetition rates [28]), have shown a first increase in XUV average power demonstrating  $> 100 \mu\text{W}$  in a single harmonic line [10, 11], with typical conversion efficiencies  $< 10^{-5}$ . Further increase of the HHG efficiency and, hence, XUV average powers in the milliwatt-regime can be achieved by using a combination of an optimized enhancement cavity together with a high average power driving laser [12], or by using short wavelength drivers [13, 14]. The latter ones made use of the efficiency scaling of the single atom response with  $\lambda^6$ , where  $\lambda$  represents the driving wavelength [29], increasing the HHG efficiency by more than one order of magnitude.

Shorter driving pulses can enhance the efficiency and the cutoff energy of the XUV comb even more and naturally generate shorter pulses in the XUV. This can be understood since higher intensities  $I$  can be applied for phase-matched HHG [3]. Furthermore, the macroscopic yield scales with the square of the single atom dipole moment  $A_q$  [7], which increases with increasing intensity [7, 30–32]. In this manuscript the model by Lewenstein et al. is used [32], resulting in higher efficiencies for shorter pulses and a  $\sim 3$  times shorter XUV pulse duration (Supplement).

However, two-photon absorption in high-reflective and anti-reflective coatings as well as in transmission optics, and the consequential heating of the materials, makes it very challenging to generate high average power as well as ultra-short pulse duration driving lasers with  $< 550 \text{ nm}$  wavelength. Therefore, until now, short wavelength driven HHG

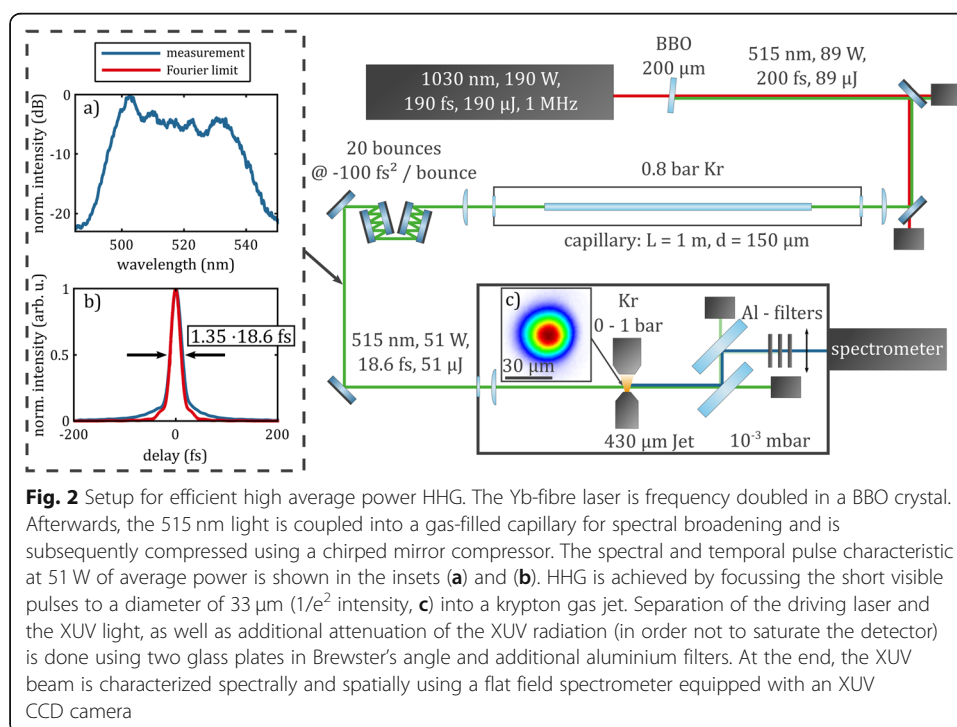
with milliwatt XUV average power was done using  $> 85$  fs pulses and average powers of a few Watt [12, 13].

In this letter, HHG driven by the unique combination of high average power (51 W), short driving wavelength (515 nm) and ultra-short pulse duration (18.6 fs) is demonstrated. These ultrashort visible pulses enable the generation of XUV pulses with a conversion efficiency of  $2.5 \cdot 10^{-4}$ , and, consequently the high average power of the driving laser boosts the photon flux to a record of  $12.9 \pm 3.9$  mW in a single harmonic line at 26.5 eV - surpassing previously demonstrated sources by an order of magnitude (Fig. 1).

## Results and discussion

### Pulse compression at high average power and 515 nm wavelength

For the experiment performed herein, a 515 nm laser at a repetition rate of 1 MHz, 89 W of average power and 200 fs is compressed, using a nonlinear hollow core fibre compressor. Careful selection of UV-grade fused silica glasses and coating materials for transmission and reflection optics, that have a low two-photon absorption and a large OH-content of up to 1000 ppm, make it possible to handle such high average powers at 515 nm. Simulations to optimize the output peak power while maintaining a low ionization level, revealed an optimal fibre diameter of  $150 \mu\text{m}$  at a fixed length of 1 m (Methods). Spectral broadening, shown in Fig. 2a, is achieved by filling such a capillary with 0.8 bar krypton. The transmission of 59% is the same for an evacuated as well as a gas-filled capillary, showing that no significant ionization is present. Temporal compression of the spectrally broadened pulses is done using a custom designed chirped mirror compressor, which shows virtually no heating of the chirped mirrors due to

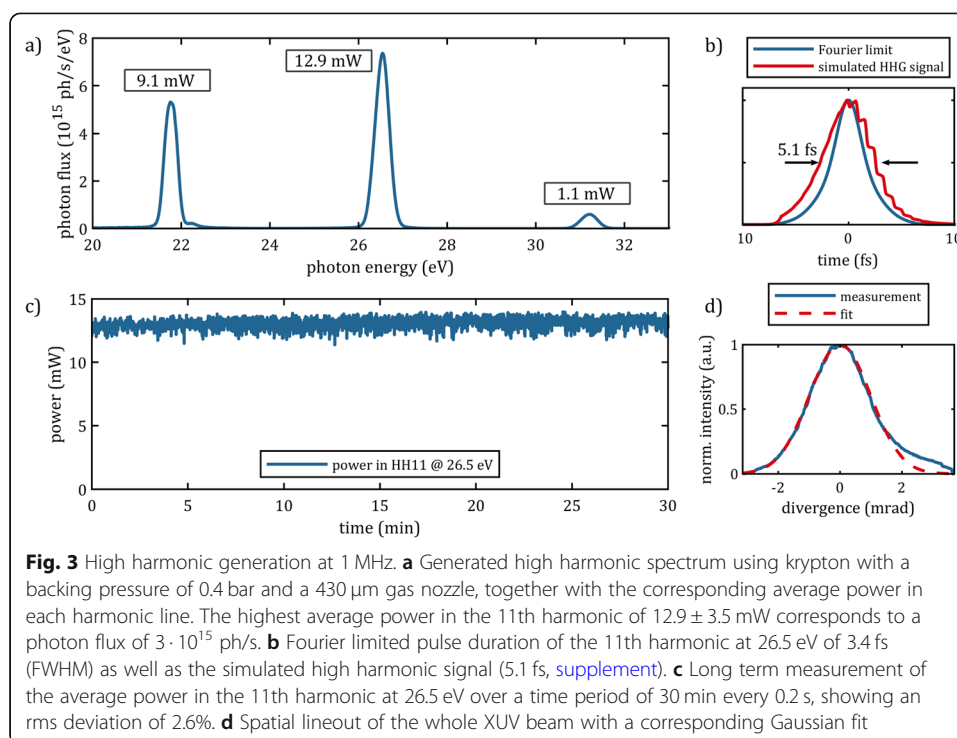


their high reflectivity, resulting in a transmission of 96%. The overall dispersion is  $-2000 \text{ fs}^2$  (20 bounces on  $-100 \text{ fs}^2/\text{bounce}$  mirrors), which is also compensating the glass dispersion of the used lenses and windows of  $1200 \text{ fs}^2$ . Fourier transforming the broadened spectrum (Fig. 2a)) reveals a deconvolution factor for the autocorrelation of 1.35, uncovering a compressed pulse duration of 18.6 fs (Fourier limit 16.5 fs) at a record average power of 51 W and a pulse energy of 51  $\mu\text{J}$ , resulting in a peak power of  $>2.5 \text{ GW}$ . Furthermore, a spatial characterization of this compressed beam shows a nearly diffraction limited beam quality with an  $M^2$  value of  $1.25 \times 1.26$ . This unique combination of short wavelength, ultrashort pulse duration, high average power and very good beam quality represents a novel class of driving laser for high harmonic generation at a five-fold higher average power compared to previous results [33, 34].

### High harmonic generation results

HHG is achieved by focussing these pulses to a diameter of  $33 \mu\text{m}$  ( $1/e^2$  intensity, Fig. 2c)) into a krypton gas jet. The generated harmonics and the remaining visible light pass through two glass plates in Brewster's angle and various  $1 \mu\text{m}$  thick aluminium filters, not only to separate the higher average power driving laser from the generated extreme ultraviolet light, but also to attenuate the XUV light for further analysis. Subsequently, a flat field spectrometer equipped with a CCD camera is used to analyse the XUV beam spectrally and spatially. Optimization of the XUV flux is done by iteratively optimizing the nozzle position on a 3D-translation stage and an iris in front of the vacuum chamber. The optimal phase-matching pressure is found via variation of the applied pressure, revealing an optimum at 0.4 bar. The result of a corresponding simulation with a one dimensional model support these findings, assuming a distance between the laser beam and the nozzle of  $144 \mu\text{m}$  (supplement). This results in a particle density in the interaction region of  $3.8 \cdot 10^{18} \text{ cm}^{-3}$  and an absorption length of  $130 \mu\text{m}$  at 26.5 eV. Consequently, the medium length defined by the nozzle diameter ( $430 \mu\text{m}$ ), which is much shorter than the Rayleigh length (1.3 mm), allows for absorption-limited HHG [7].

Due to the ultra-short pulse duration at 515 nm, the HHG efficiency into a single harmonic line at 26.5 eV is  $2.5 \cdot 10^{-4}$ , which is among the highest reported so far [8, 14]. The short pulse duration is important for this high efficiency since higher intensities can be applied for phase-matched HHG, compared to previous experiments using 85 fs driving laser pulses [13], the shorter driving laser pulses show a threefold increase in efficiency as well as a  $>5 \text{ eV}$  higher cut-off energy. Furthermore, the high average power (51 W) of the driving laser allows 23.1 mW of average power in the range from 20 eV to 35 eV (Fig. 3a)), with a record high average power of  $12.9 \pm 3.9 \text{ mW}$  in the strongest harmonic line at 26.5 eV. The relative uncertainty is estimated conservatively to be  $<30\%$ , with the main contributions originating from the measured filter transmission (7%) and the grating efficiency (20%). In addition, the increased cutoff allows for  $>1 \text{ mW}$  of average power above 30 eV. Note, that for a high flux delivery, a grating incidence plate [35] or annular beam driven HHG [36] in combination with a 100 nm aluminium filter could be used as a separator, resulting in an attenuation of the driving laser to  $<1 \mu\text{W}$  with  $>5 \text{ mW}$  usable XUV average power on target. The Fourier-limited pulse duration of a single harmonic line corresponds to 3.4 fs pulse duration in the



XUV (Fig. 3b)), which is in good agreement with the duration of the simulated phase-matching window (5.1 fs, [supplement](#)). Focussing these pulses to a spot size of 1  $\mu\text{m}$ , would result in an intensity  $>10^{14}$  W/cm<sup>2</sup>. Thus, even nonlinear XUV-techniques are in reach at a MHz repetition rate. A long-term stability measurement of the photon flux of the strongest harmonic line at 26.5 eV shows an rms-deviation of 2.6% over a time period of 30 min (Fig. 3c)). Furthermore, a spatial lineout integrated over the whole spectrum together with a Gaussian fit shows a Gaussian like beam profile of the XUV beam with a divergence of 2 mrad (Fig. 3d)), showing the great potential of this source for further experiments.

## Conclusion

In conclusion, a high power XUV source via HHG, delivering an average power of  $12.9 \pm 3.9$  mW in single harmonic line at 26.5 eV and  $> 1$  mW at photon energies above 30 eV is demonstrated. Furthermore, the spectrum supports a Fourier limited pulse duration of 3.4 fs and simulation results suggest that the time span of the efficient high harmonic generation is shorter than 6 fs. This record XUV power together with the cutoff enhancement is enabled by a new-class of driving laser providing a unique combination of a short wavelength (515 nm) and a short pulse duration (18.6 fs) at a record high average power of 51 W. Compared to state-of-the art XUV sources, the provided average power is one order of magnitude higher and the pulse duration is significantly shorter, which represents a major milestone for upcoming applications of coherent XUV radiation in science and technology. Especially compared to Yb-fiber laser driven HHG sources the overall system efficiency from the Yb-fiber CPA into the XUV is  $7 \cdot 10^{-5}$ , which is the highest efficiency ever shown for fiber laser driven HHG sources [10–14]. This will greatly advance and facilitate XUV application in various fields e.g.

investigating fastest dynamics using photoelectron emission spectroscopy, coincidence measurements, XUV- ionization and absorption spectroscopy, fluorescence spectroscopy, ultrafast XUV imaging and XUV-pump XUV-probe experiments, among others [17–24, 26, 27]. Due to the excellent scaling possibilities of energetic ultrafast Yb-based fibre lasers and the components for pulse compression to the kW-level and beyond [28, 37, 38], even upscaling of the presented approach to the 100 mW level seems possible.

## Methods

### Fibre laser setup and second harmonic generation

The high average power Yb-fibre laser system used for the experiments is similar to the one shown by Müller et al. [28]. For the experiments performed herein, four coherently combined amplifier channels are used. At a central wavelength of 1030 nm and a repetition rate of 1 MHz it delivers a pulse energy of 190  $\mu$ J at a pulse length of 190 fs, resulting in 190 W of average power. This laser is focused into a 200  $\mu$ m thick Type-I beta-barium-borate (BBO) crystal for second harmonic generation (SHG). Using an IR focal size of 590  $\mu$ m ( $1/e^2$  intensity) and a resulting intensity of 700 GW/cm<sup>2</sup>, an SHG efficiency of 47% is achieved. The resulting 89  $\mu$ J, 89 W and 200 fs pulses at 515 nm have an excellent spatial beam quality with an  $M^2$  value of smaller than 1.1 in both axes, as well as a negligible astigmatism.

### Hollow core fibre compression simulations

The numerical simulations of the pulse propagation in the hollow core fibre are performed based on the unidirectional field propagation equation for the fundamental mode [39]:

$$\partial_z E(z, \omega) = i \left( \beta(\omega) - \frac{\omega}{v} \right) E(z, \omega) + i \frac{\omega^2}{2 c^2 \epsilon_0 \beta(\omega)} P^{NL}(z, \omega)$$

with the electric field amplitude in the spectral domain  $E$ , the angular frequency  $\omega$ , the fundamental mode propagation constant  $\beta$ , the frame reference velocity  $v$ , the vacuum speed of light  $c_0$ , and the vacuum permittivity  $\epsilon_0$ . The nonlinear polarization  $P^{NL}$  includes the Kerr-nonlinearity and plasma formation (based on Amossov-Delone-Krainov ionization rates [40]).

### Characterization of extreme ultraviolet radiation

The generated photon flux is estimated by accounting for the known efficiencies in the detection apparatus, which are the CCD sensitivity and quantum efficiency (1 ph/count), the grating efficiency (0.11), the measured filter transmission ( $4 \cdot 10^{-4}$ ), the absorption due to the residual gas (0.7) and theoretical reflectivity of the Brewster plates [41] ( $6 \cdot 10^{-3}$ , which show a good agreement with calibration measurements [13, 35]). The values in the brackets are the correction factors used for the 13th harmonic at 26.5 eV. This technique was cross-calibrated using a photodiode (AXUV100G) in various previous experiments and always has shown a good agreement [11, 13].

### Abbreviations

HHG: High harmonic generation; XUV: Extreme ultraviolet; BBO: Beta-barium-borate; SHG: Second harmonic generation

## Supplementary Information

The online version contains supplementary material available at <https://doi.org/10.1186/s43074-021-00028-y>.

**Additional file 1:** This supplementary information provides details on the one-dimensional model used for simulating the high-harmonic build-up. Furthermore, details for the temporal phase-matching as well as for the XUV pulse duration are presented.

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Not applicable.

### Authors' contributions

J.L., J.R., S.H. and R. K conceived and planned the experiment. R.K., J.B., H. S, A.K, and M.G. built and optimized the ultrafast fibre laser and the nonlinear compression stage. R.K., A.K, J.B. and H.S. performed the HHG experiments. R.K., S.H. and M. G performed simulations and data analysis. All authors discussed and contributed to the interpretation of the results and to the writing of the manuscript. J.L. and J.R. supervised the project and acquired funding. The author(s) read and approved the final manuscript.

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### Availability of data and materials

The datasets used and/or analysed during the current study are available from the corresponding author on reasonable request.

### Declarations

#### Ethics approval and consent to participate

Not applicable.

#### Consent for publication

Not applicable.

#### Competing interests

S.H. is employed by Active Fiber Systems who distributes commercial XUV sources.

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