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Dielectric relaxation and scaling of AC conductivity observed in mixed valence perovskite Eu₂CoMnO₆

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Monophasic and polycrystalline double perovskite Eu₂CoMnO₆ has been synthesized, and its structural characterization, frequency and temperature-dependent dielectric relaxation have been studied. Observed thermally activated dielectric relaxation was explained using the empirical Havriliak–Negami (HN) dielectric relaxation function with an estimated activation energy $E \sim$ 0.22 eV and attempt frequency $f_0 \sim 2.46 \times 10^9$ Hz. The frequency-dependent AC conductivity data, over a wide range of temperature (100–325 K), followed the empirical universal power law behavior (~ f^n , n is the constant exponent) showing two different frequency exponents, respectively, in the high- and low-temperature regions. The high-temperature (>275 K) conductivity data followed the continuous time random walk (CTRW) approximation model proposed by Dyre. However, this model failed to reproduce the observed conductivity spectra in the low-temperature side (<200 K). Interestingly, both the high- and low-temperatures' conductivity data can be scaled to the master curve with suitably chosen scaling parameters.

Keywords: Dielectric relaxation; AC conductivity; scaling; perovskite.

1. Introduction

Ferromagnetic insulators showing remarkable physical properties have drawn considerable research interest in recent years.¹⁻³ In this group, double perovskite is an exciting class of ferromagnetic insulators having the general chemical composition $A_2BB'O_6$ (A is lanthanum or rare earth, B/B' are two different transition metals and O is oxygen).^{4–19} These multifunctional materials showed exciting multiferroic, magneto-dielectric and magneto-resistance properties having immense potential for their applications.⁶⁻⁹ La₂CoMnO₆ and La₂NiMnO₆ are isostructural compounds of this double perovskite family which showed ferromagnetism and magnetoelectric properties.⁹⁻¹² One of the unique features of these double perovskites is the creation of anti-site disorder or anti-phase boundaries during the preparation of the compounds. Anti-site disorder induced unusual dielectric and magnetic properties were reported in different double perovskite compounds.10-14

In the past, detailed structural, dielectric and magnetic properties of single phase Eu_2NiMnO_6 revealed ferromagnetism with low coercivity and high dielectric constant associated with magnetodielectric features.¹⁷ Recently, it was found that Eu_2CoMnO_6 showed unusual magnetic properties, Hopkinsonlike effect as well as the presence of volume spin-glass-like behavior.¹⁸ Though magnetic field induced metamagnetic, magnetocaloric and pyrocurrent were reported in the recent past,¹⁹ the dielectric and AC conductivity characteristics of Eu₂CoMnO₆ have not yet been thoroughly investigated. Since dielectric study provides additional information of conduction and magnetoelectric coupling for such compounds,9,10,20 our plan in this communication is to present detailed structural, dielectric and AC conductivity properties of Eu₂CoMnO₆ over broad ranges of temperature (80–350 K) and frequency (1 kHz-1 MHz). The observed temperature- and frequencydependent dielectric properties of Eu₂CoMnO₆ indicated quite a high value of relative dielectric permittivity $\sim 10^3$ in the kHz frequency region. Thermally activated Havriliak-Negami (HN) type asymmetric and broadened dielectric relaxation was also noticed. CTRW and empirical universal dielectric response (UDR) analysis of the AC conductivity data have also been explored. These conductivity data exhibited interesting time-temperature scaling behavior as shown in this paper.

2. Material and Methods

Polycrystalline Eu_2CoMnO_6 was prepared by the standard solid state reaction route from a stoichiometric mixture of high purity (>99%) precursor EuO, CoO and MnO₂ oxides. The oxide precursors were well mixed using an agate mortar and then calcined at ~1000 K for 24 h. After grinding the calcined powder, pellets of diameter ~8 mm and ~2 mm

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thickness were made and sintered again at ~1200 K for 48 h and the furnace was cooled to ambient temperature. The crystalline structure of the sample was investigated by X-ray powder diffraction (using XRD-Bruker D8 Advance) with Cu-K α radiation at ambient temperature and pressure. Dielectric permittivity and AC conductivity measurements were carried out using a HP 4192A impedance analyzer which was interfaced with a computer for automatic data acquisition. A good quality silver paste was used for the electrodes in the dielectric measurements. A Lakeshore 332 temperature controller was employed to control the sample temperatures with an accuracy of ~0.01 K. The refinement of the crystal structure was performed by the Rietveld method using the Material Analysis Using Diffraction (MAUD) program.

3. Results and Discussion

3.1. Structural properties

The crystallinity of the Eu₂CoMnO₆ compound was investigated from the analysis of the X-ray powder diffraction (XRD) as shown in Fig. 1. Monophasic and well crystalline nature of the prepared compound is evident from the observed sharp reflection lines. The X-ray diffraction patterns can be well fitted to the monoclinic space group P2₁/n. Based on the refinement result, a model crystal structure is developed and is shown in the inset of Fig. 1. The least square Rietveld refinement provides an estimate of lattice parameters a = 5.333, b = 5.565, c = 7582, $\alpha = 90.0^{\circ}$, $\beta = 89.99^{\circ}$ and $\gamma = 90^{\circ}$. Goodness of the fit indicators associated with the refinement was $R_{wp} = 4.6$, $R_p = 3.58$ and $\sigma = 1.09$. The derived crystallographic parameters based on the refinement results are presented in

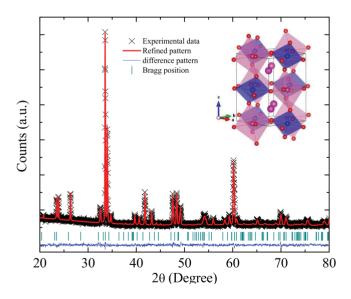


Fig. 1. (Color online) Powder X-ray diffraction pattern at room temperature. Red solid line is the least square Rietveld refinement of the XRD. The difference of observed and fitting result is shown by the blue continuous line. Green vertical ticks are Bragg positions for reflection lines.

Table 1. Comparison of structural information of Eu_2CoMnO_6 and isostructural Eu_2NiMnO_6 . The data for Eu_2NiMnO_6 are taken from Ref. 17.

Structural parameters	Eu ₂ CoMnO ₆	Eu ₂ NiMnO ₆
a (Å)	5.334	5.332
b (Å)	5.565	5.523
c (Å)	7.582	7.595
Unit Cell Volume (Å ³)	225.06	223.66
<co-o>(Å)</co-o>	1.858	_
<ni-o>(Å)</ni-o>		1.988
<mn–o>(Å)</mn–o>	2.106	1.989
Mn-O1-Co/ Mn-O1-Ni	150.3°	144.5°
Mn-O2-Co/ Mn-O2-Ni	153.3°	141.7°
Mn-O3-Co/ Mn-O3-Ni	147.3°	163.3°
NiO ₆ polyhedral volume	_	9.8726 (Å ³)
CoO ₆ polyhedral volume	8.3785 (Å ³)	
MnO ₆ polyhedral volume	10.3325 (Å ³)	12.3008 (Å ³)

Table 1. A comparison of the Eu₂CoMnO₆ structure with the previously reported¹⁷ isostructural and closely related double perovskite Eu₂NiMnO₆ is made and shown in a separate column in Table 1. The TM–O (TM = Ni, Mn, Co) bond distances are reduced for Co–O and enhanced for Mn–O when compared to Ni–O and Mn–O bond lengths observed in Eu₂NiMnO₆. In comparison to Eu₂NiMnO₆, the unit cell volume is slightly expanded; appreciable distortion and volume changes in the CoO₆ and MnO₆ polyhedral are also noticed. Interestingly, in comparison to Eu₂NiMnO₆, a significant deviation of the linear 180° situation of TM–O–TM in the apical 'c' direction is observed for the Eu₂CoMnO₆ compound. However, with respect to Eu₂NiMnO₆, the TM–O–TM angle in the basal plane deviates less from 180° in Eu₂CoMnO₆.

3.2. Dielectric relaxations

The measured frequency and temperature dependent relative dielectric permittivity (ε_r) of the pellet sample is shown in Fig. 2(a). At low frequency (*f*), quite a high value of $\varepsilon_r \sim 10^3$ (at 1 kHz) is observed even at a temperature as low as 185 K. With increasing frequency, the dielectric permittivity relaxes to a lower static dielectric value ($\varepsilon_{\infty} \sim 15$). The typical dielectric relaxation behavior shown in Fig. 2(a) differs appreciably from that of the ideal Debye type dielectric relaxation.²¹ As shown in Fig. 2(a), the dielectric relaxation behavior can be fitted to the Havriliak–Negami (HN) dielectric relaxation model²² described by

$$\varepsilon_r = \varepsilon_{\infty} + \Delta \varepsilon \left(1 + 2\left(\omega\tau\right)^{\beta} \cos\left(\frac{\pi\beta}{2}\right) + \left(\omega\tau\right)^{2\beta} \right)^{-\frac{\gamma}{2}} \cos(\gamma\varphi),$$
(1)

where $\Delta \varepsilon$ = dielectric strength, ω = angular frequency, τ = HN relaxation time, β , and γ parameters represent the symmetric and asymmetric broadening of the relaxation, respectively, and

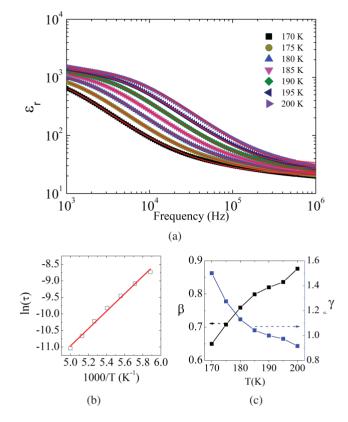


Fig. 2. (Color online) (a) Frequency variation of dielectric permittivity at some selected temperature. The solid red line is the best fit of HN relaxation function Eq. (1) discussed in text. (b) Arrhenius plot of the HN relaxation time; red line is best linear fit. (c) Temperature variation of asymmetric (β) and symmetric (γ) broadening parameters.

$$\varphi = \arctan\left(\frac{(\omega\tau)^{\beta}\sin\left(\frac{\pi\beta}{2}\right)}{1+(\omega\tau)^{\beta}\cos\left(\frac{\pi\beta}{2}\right)}\right).$$

It is seen from the red continuous line in Fig. 2(a) that the HN function replicated the observed dielectric relaxation quite reasonably. The temperature-dependent HN relaxation time τ obtained from the best fit to Eq. (1) is shown in Fig. 2(b) as a function of inverse temperature. An Arrhenius type thermally activated relaxation governed by $\tau = \tau_0 \exp\left(\frac{E}{kT}\right)$ (where τ_0 is the pre-exponential factor, E is the activation energy, k is the Boltzmann constant and T is the temperature) is found to follow. The best linear fit to the data provides a reasonable value of activation energy E = 0.22 eV and attempt frequency $f_0 = 2.46 \times 10^9$ Hz. Temperature variation of the asymmetry and broadness parameters obtained from the HN fitting to the dielectric relaxation is shown in Fig. 2(c). The symmetry parameter β increases with temperature and the asymmetry parameter γ decreases with temperature. Thus, different broadening mechanisms appeared to dominate at different temperatures.

The nonDebye type dielectric relaxation behavior is also evident from the modulus representation. The complex

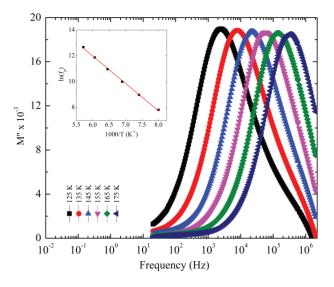


Fig. 3. (Color online) Thermally activated relaxation in the modulus representation. Inset shows the Arrhenius plot of the relaxation peak at different temperatures. Red line is the best linear fit.

electric modulus $M^*(\omega)$ is related to the Fourier transform of the time derivative of the electrical relaxation function, $\varphi(t)$, specifically, $M^*(\omega) = M_{\infty} \left| 1 - \int_0^{\infty} \exp(-i\omega t) \frac{d\varphi}{dt} dt \right|$, where $M_{\infty} = \frac{1}{2}$. Imaginary component (M'') of the complex electric modulus is shown in Fig. 3 as a function of frequency at various fixed temperatures. Signature of the asymmetric and significantly broad relaxation peak is observed from the frequency-dependent dielectric modulus as shown in Fig. 3. Interestingly, the width of the relaxation peaks decreases (from ~ 2.2 to ~ 1.8 decades) with an increase in temperature from 135 to 175 K. This value is considerably larger than the full width at half maximum (~1.14 decades) in ideal noninteracting dipolar relaxation described by the Debye relaxation function. Again, the relaxation peak frequency (f_p) is found to follow thermally activated Arrhenius behavior as shown in the inset of Fig. 3 which provides an estimation of the activation energy ~0.20 eV, close to the earlier mentioned estimated value.

The measured temperature-dependent dielectric permittivity at various fixed frequencies is shown in Fig. 4. In this measurement, the sample is first cooled to 80 K, and the dielectric permittivity was measured with increasing temperature. The thermally activated dielectric relaxation with temperature is shown by the arrow in Fig. 4. For all the measured frequencies, the dielectric constant drops to a very low value ~15 around liquid nitrogen temperature. Above and around room temperature, the dielectric permittivity shows a large value ~10³ and is relatively less sensitive to temperature also increases obeying the thermally activated dielectric relaxation. Frequency variation of the loss tangent showed the characteristic loss peak (Fig. 4(b)) which is also

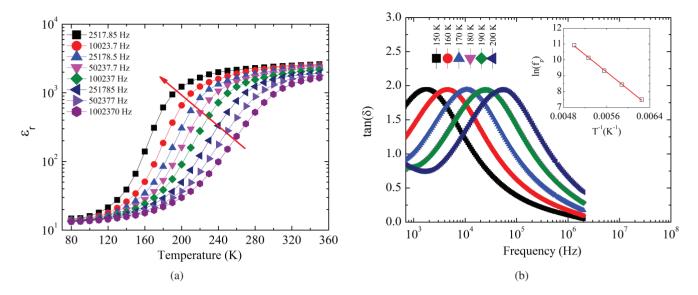


Fig. 4. (Color online) (a) Temperature variation of relative dielectric permittivity for different frequencies. Thermally activated relaxation is marked by the arrow in the figure. (b) Thermal variation of loss tangent at selected frequencies. Inset of (b) is the Arrhenius plot of relaxation peak frequency observed in figure (b). Red line is the best linear fit.

thermally activated with an estimated activation energy ~0.21 eV. For the Eu₂CoMnO₆ compound with two different transition metal (Co and Mn) ions, a virtual hopping of charges between two dissimilar metal ions generates hopping polarization which gives rise to the observed dielectric relaxation. A similar dielectric relaxation due to hopping polarization was also observed in the closely related double perovskite La₂NiMnO₆.¹⁰

3.3. AC conductivity and scaling

AC conductivity (σ_{ac}) measurements provide considerable insight into the nature of conduction in disordered solids.²³ The conductivity spectra are shown in Figs. 5(a) and 5(b) for the low- and high-temperature regions, respectively. Figures 5(a) and 5(b) can be clearly divided into two separate regions. A plateau is noticed in the low-frequency side. For higher frequencies, on the other hand, a gradual dispersion sets in and indicates a power law ($\sim f^n$, *n* is constant) type dependence. Significant temperature dependence of conductivity is noticed in the low-frequency region in comparison to that in the high-frequency domain. The overall feature of the conductivity spectra appears to follow the empirical universal power law²³ behavior described by

$$\sigma_{\rm ac}\left(f\right) = \sigma_0 + A f^n, \qquad (2)$$

where $\sigma_{\rm ac}(f)$ represents the frequency-dependent AC conductivity, σ_0 is the limiting value of AC conductivity when $f \rightarrow 0$,

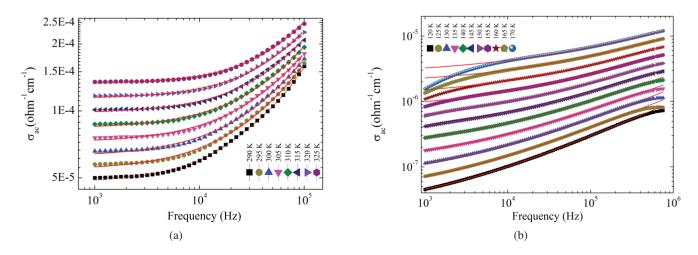


Fig. 5. (Color online) AC conductivities as a function of frequency at different fixed temperatures are shown in figure (a) and in figure (b) for the high- and low-temperature regions, respectively. Red solid lines are the best fit to Eq. (2).

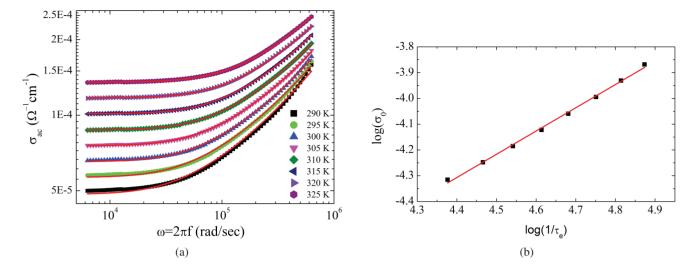


Fig. 6. (Color online) (a) Frequency variation of AC conductivity data fitted to Eq. (3) shown by red continuous line. (b) The fitting parameters τ_e and σ_0 of Eq. (3) are plotted to show the Barton–Nakajima–Namikawa (BNN) relation.

and A and n are two constants related to the strength of polarizability of the medium and interaction of mobile ions and lattices, respectively. The characteristic feature of the charge transport in many of the disordered semiconducting oxides and glassy materials usually obeys Eq. (2), referred to as the universal dynamic response (UDR).²³ Though a reasonable fitting is achieved with Eq. (2), it is important to mention that the exponent parameter *n* markedly differs in high and low temperatures. As mentioned earlier, the constant n is related to the interaction of the mobile ions and lattice, so this changing interaction with temperature may be responsible for the temperature dependence in n. The estimated exponent n = 0.99 at 325 K is found to monotonically decrease to 0.85 at 290 K. The frequency exponent n also decreases with temperature and lies between 0.6 and 0.4 in the temperature range (120-170 K) as seen in Fig. 5(b).

It is to be noted that Eq. (2) was derived based on the empirical description of σ_{ac} reportedly applied for a wide

range of compounds. The σ_{ac} data were also analyzed in the light of the macroscopic theoretical model proposed by Dyre^{24,25} where conductivity can be expressed by the relation

$$\tau_{\rm ac}\left(\omega\right) = \frac{\sigma_0 \omega \tau_e \arctan\left(\omega \tau_e\right)}{\frac{1}{4}\ln^2\left(1 + \omega^2 \tau_e^2\right) + \left(\arctan\left(\omega \tau_e\right)\right)^2}.$$
 (3)

Here $\sigma_{\rm ac}(\omega)$ is the (angular) frequency dependent real part of the complex AC conductivity, σ_0 is the limiting value of $\sigma_{\rm ac}$ when $f \rightarrow 0$, ω is the angular frequency and τ_e is the relaxation time. Equation (3) provides a basis to analyze conduction phenomena on a theoretical level which is based on the random free energy barrier model developed by Dyre.²⁴ Within the CTRW approximation, conduction is assumed to take place by the hopping of charge carriers in a spatially randomly varying energy landscape. Interestingly, reasonable fitting with Eq. (3) is also observed in the high-temperature region (red continuous line in Fig. 6(a)). However, the said

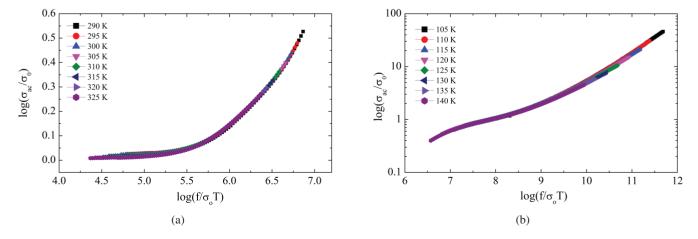


Fig. 7. (Color online) Scaling of AC conductivity in high- and low-temperature regions is presented in figures (a) and (b), respectively.

macroscopic theoretical CTRW model (Eq. (3)) failed to fit the corresponding low-temperature (not shown) conductivity data. Thus, it is apparent that two different microscopic conduction mechanisms are operative at high- and low-temperature regions. It is noteworthy to mention that the fitting parameters τ_e and σ_0 are in good agreement with those of the Barton–Nakajima–Namikawa (BNN) relation²⁶ which is evident from the straight-line feature of the curve shown in Fig. 6(b).

Scaling is widely used to investigate the possible underlying common physical mechanisms for conduction.^{27,28} Hence, the scaling characteristics of the σ_{ac} spectra are also examined for the present sample. The result presented in Figs. 7(a) and 7(b) indicates that the conductivity spectra can be scaled to a master curve in both the high- and low-temperature regions. The zero frequency limiting value of AC conductivity σ_0 was taken as the scaling parameter for σ_{ac} . The products of σ_0 and T were used for the scaling parameters for the frequency scale. The choice of scaling parameter is identical to that of canonical scaling.²⁸ Similar scaling characteristics were also reported in disordered semiconductor type materials.^{29,30} The estimated scaling parameters suggested that the shape of the relaxations' function was not dependent separately on the frequency and temperature, but together as a product of frequency and temperature. Though low-temperature data could not be reproduced by Eq. (3), the scaling properties retained in the conductivity spectra (with the same choice of scaling parameters similar to the high-temperature side) as shown in Fig. 7(b). Although the time scale of the relaxation varies with temperature, it is apparent that the spectral features of the relaxation functions contribute at all temperatures to preserve the scaling features.

4. Conclusion

We have synthesized the single phase double perovskite Eu_2CoMnO_6 and compared the structural properties with another closely related isostructural compound Eu₂NiMnO₆ which revealed the interesting role of bond lengths, bond angles, polyhedral shape and volume on the physical properties of Eu₂CoMnO₆. Quite a high value of relative dielectric permittivity $\sim 10^3$ with weak temperature dependent behavior (for frequencies below 100 kHz) was detected around ambient temperatures. The observed dielectric relaxation was attributed to the hopping polarization between two different Co and Mn cationic potential wells in a disordered cationic environment. The nature of dielectric relaxation is successfully explained with the HN type relaxation function revealing the important role of anti-site disorder in the dielectric properties. Asymmetric and broadened dielectric relaxations in both temperature and frequency variations indicated the prospective role of anti-site disorder developed during the growth of the double perovskite Eu₂CoMnO₆. The AC conductivity qualitatively followed empirical UDR governed by the Jonscher power law. However, it is noted that the

macroscopic CTRW approximation model proposed by Dyre is applicable only in the high-temperature region. Hence, it can be concluded that some different or additional microscopic conduction mechanism influences the conductivity behavior in the low-temperature region. Finally, success to scale different data sets to collapse all to one common master curve indicates that the underlying conduction mechanism can be separated into a common physical mechanism modified by thermodynamic scales only.

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