

# A 12-bit 30-MS/s VCO-based SAR ADC with NOC-assisted multiple adaptive bypass windows

Xiangxin Pan, Xiong Zhou, Sheng Chang, Zhaoming Ding, and Qiang Li<sup>†</sup>

Institute of Integrated Circuits and Systems, University of Electronic Science and Technology of China, Chengdu 610054, China

**Abstract:** This paper proposes a technique that uses the number of oscillation cycles (NOC) of a VCO-based comparator to set multiple adaptive bypass windows in a 12-bit successive approximation register (SAR) analog-to-digital converter (ADC). The analysis of the number of bit cycles, power and static performance shows that three adaptive bypass windows reduce power consumption, and decrease DNL and have similar INL, compared with the SAR ADC without bypass windows. In addition, a 1-bit split-and-recombination redundancy technique and a general bypass logic digital error correction method are proposed to address the settling issues and optimize the size of the bypass window. This design is implemented in 40 nm CMOS technology. The conversion frequency of the ADC reaches up to 30 MS/s. The ADC achieves an SFDR of 85.35 dB and 11.12-bit ENOB with Nyquist input, consuming 380  $\mu$ W, down from 427  $\mu$ W without multiple adaptive bypass windows, at a 1.1 V supply, resulting in a figure of merit (FoM) of 5.69 fJ/conversion-step.

**Key words:** adaptive bypass window; number of oscillation cycles (NOC); offset; split-and-recombination redundancy; SAR ADC; VCO-based comparator

**Citation:** X X Pan, X Zhou, S Chang, Z M Ding, and Q Li, A 12-bit 30-MS/s VCO-based SAR ADC with NOC-assisted multiple adaptive bypass windows[J]. *J. Semicond.*, 2020, 41(11), 112401. <http://doi.org/10.1088/1674-4926/41/11/112401>

## 1. Introduction

Low power and high resolution analog-to-digital converters (ADCs) are widely used in mobile, wearable and implantable devices, the internet of things (IoT) and so on. Successive approximation register (SAR) ADC exhibits excellent energy efficiency and has attracted much attention due to its digital-like nature and adaptability to advanced CMOS technology. Much work is occurring to reduce the logic power consumption, such as a variety of switching schemes to save part of the energy of CDAC<sup>[1–6]</sup>. From a systematic perspective, the bypass logic shown in Fig. 1, can not only save energy from CDAC but also greatly reduce the energy from the comparator and digital logic<sup>[7]</sup>. When the input voltage is within the range called the bypass window, the intermediate bit cycles can be skipped completely and does not influence the correct output. However, the bypass window comes at the cost of two additional coarse comparators and an external reference, which increases design complexity and makes the precision partially dependent on the reference voltage.

The comparator is a fundamental consideration in SAR ADC, which is an indispensable but power-hungry block. The input-referred noise constrains the power consumed by the comparator. For a voltage-domain comparator such as a double-tail comparator or strong-arm comparator, whose noise reduction relies on brute-force analog scaling, it requires four times the power to halve the input-referred noise<sup>[8]</sup>. Alternatively, time-domain comparators, which show good potential in power efficiency and scalability, attract attention due to their digital nature and more choices for lower

noise such as VTC-based<sup>[9]</sup>, VCDL-based<sup>[10]</sup>, oscillator collapse-based<sup>[11]</sup> and VCO-based<sup>[12, 13]</sup>. The last type gains much favor under its noise-adaptive characteristic. It can generate output signal without oscillation if the input voltage is large. When the input voltage is small enough, it will oscillate until the decision is made. In other words, there is a relationship between the input voltage and the oscillation number, which shows that the oscillation number indicates an inherent coarse quantization.

Apart from making decisions and employing the decisions to reduce the comparator noise<sup>[14–16]</sup>, a VCO-based comparator offers extra information, known as the number of oscillation cycles (NOC)<sup>[17]</sup>, to detect whether the input signal of the comparator is in the vicinity of common-mode voltage. This information can be utilized to trigger bypass logic, which avoids the use of additional comparators and reference. It can be triggered at any bit as long as NOC reaches a specific number. Furthermore, multiple bypass windows can be constructed by NOC, which provide more power reduction and static performance improvement. The windows size can be adaptively adjusted to PVT variations on the basis of the NOC and window detection logic.

This design takes full advantage of the potential of a VCO-based comparator as a bypass detector served, which can be used for higher resolution (12 bit) and higher speed (30 MS/s) SAR ADC<sup>[18]</sup>. The structure of the VCO-based comparator and the consideration of the offset caused by different NOC are presented. The design of core digital circuits is described thoroughly. The benefits of bit cycles decrease, power reduction and static linearity improvement from adaptive multiple bypass windows are analyzed. For compensating the settling error from DAC and reference because of high resolution and speed, a 1-bit split-and-recombination re-

Correspondence to: Q Li, [qli@uestc.edu.cn](mailto:qli@uestc.edu.cn)

Received 22 JUNE 2020; Revised 15 JULY 2020.

©2020 Chinese Institute of Electronics

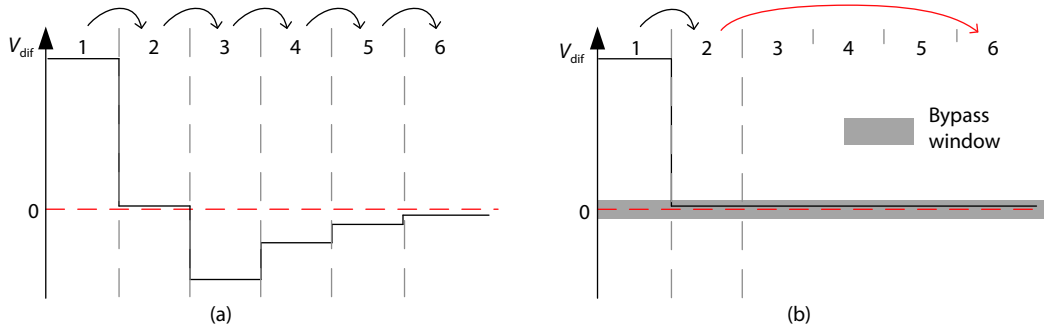


Fig. 1. Conversion process of 6-bit SAR ADC. (a) Conventional SAR ADC. (b) SAR ADC with bypass window.

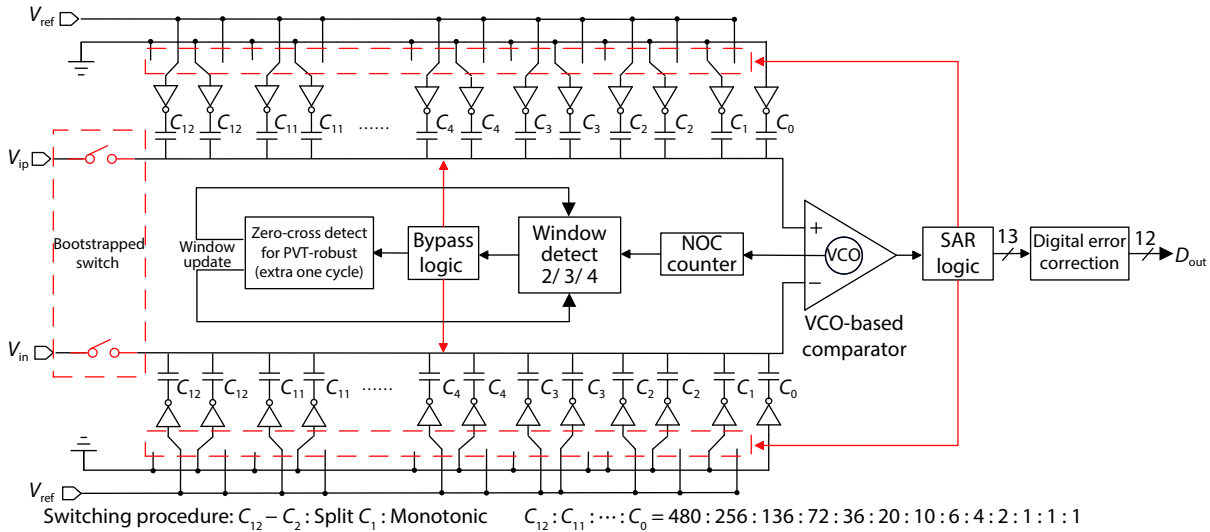


Fig. 2. Architecture of the proposed SAR ADC.

dundancy<sup>[19]</sup> and a general method to correct digital errors for bypass logic are proposed, which circumvents the use of complex or off-chip calibration circuits.

This paper is organized as follows. Section 2 describes the overall ADC architecture, operation principle and building blocks. Section 3 analyzes the bit cycle decrease, power reduction and static performances with multiple adaptive bypass windows, and derives the maximum DNL and INL of it, while section 4 explains split-and-recombination based redundancy and a general digital error correction method for bypass logic. Section 5 presents simulation results and comparison with the state-of-the-arts, and section 6 draws the conclusions.

## 2. Architecture and design considerations

The architecture of the proposed SAR ADC is shown in Fig. 2 including two bootstrapped sampling switches<sup>[20]</sup>, a differential capacitive DAC (with 1-bit redundancy), VCO-based comparator, NOC counter, SAR logic, bypass logic, window detection logic (three adaptive bypass windows), window update logic, and digital error correction logic.

### 2.1. Operation principle

During the sampling phase, the input differential voltage is sampled onto the top plates of CDAC by two bootstrapped switches. If the input signal is large enough, the comparator makes the decision directly without oscillation. Otherwise, if the input signal is relatively small (within several LSBs), VCO

will oscillate several times to increase the delay until the time difference between two VCO loops exceeds the dead zone of the phase detector. To take advantage of the oscillation information, three bypass windows  $W_2$ ,  $W_3$  and  $W_4$  are used for the standing of the oscillation numbers of 2, 3 and 4, respectively. For example, if the NOC is 4, the bypass window  $W_4$  is triggered for the first time and bit cycles will move to the LSB cycle. Due to the impact of noise and PVT variation, even if the same voltage inputs into the comparator, the oscillation number might be different. The signal must be detected to determine whether it can be digitized with the remaining capacitor weights in case the result is not convergent.

Window update logic, shown in Fig. 3, can implement the window-size detection.  $V_x$  and  $V_y$  are the differential inputs.  $V_B$  stands for the current bypass window size of  $W_4$ , and its initial value is 1 LSB. If differential signals cannot cross zero (common-mode voltage), the bypass window is too small and this process of the bypass is wrong<sup>[17]</sup>. The cycle must be back to where the bypass begins and  $W_4$  is updated. The next time when the NOC is 4, the conversion process will be bypassed to the cycle of  $LSB + 1$  and  $V_B$  will become the voltage of 2 LSB. This update process also applies to  $W_2$  and  $W_3$ . It is worth noting that the size of the bypass window is updated following the weights of CDAC and carried out in the background. So smaller low-weight capacitors achieves more precision bypass window sizes and the adaptive bypass windows are PVT-robust. Bypass logic cannot be triggered for more than one time in one conversion period under the con-

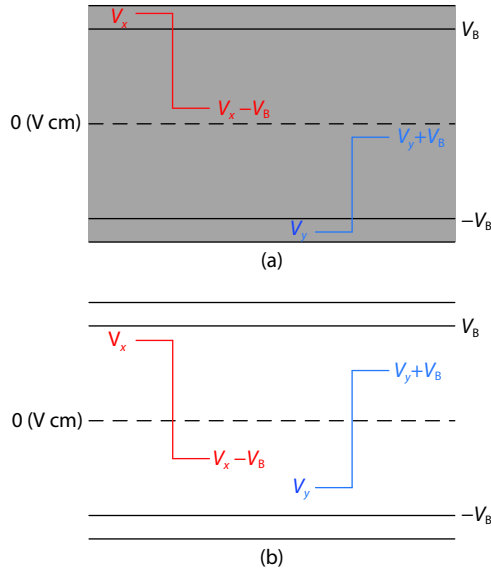


Fig. 3. Window update logic. (a) Not cross zero. (b) Cross zero.

sideration of conversion speed and complexity of the logic design.

## 2.2. VCO-based comparator design and offset consideration

Compared with voltage-domain comparator, whose input-referred noise is often dominated by sizes of input and tail transistors<sup>[21]</sup>, designing a low-noise VCO-based comparator is more flexible<sup>[17]</sup>. The more stages it uses, the lower input referred noise but lower speed for the large input voltage it possesses. For delay cells, the topologies, the sizes of transistors, the threshold voltages of transistors and filtering capacitors all influence the noise and speed<sup>[22]</sup>. It is a hard trade-off that influences the bypass window sizes. Two common differential delay cells are shown in Fig. 4. When input voltage is low, the pulling down of cell II will be slow. Compared with the delay cell II<sup>[12]</sup>, the inserted inverter in delay cell I increases the reset speed. The option is that four stages of the delay cell I are to be used in the proposed scheme for quicker comparison.

Some works<sup>[23, 24]</sup> utilized multiple comparators to achieve lower power consumption or higher speed<sup>[25, 26]</sup>. All these designs have the matching problem of different input-referred offset voltages, which can be solved well by the calibration method<sup>[27]</sup> or introducing redundant capacitors into the DAC<sup>[28]</sup>. Actually, a VCO-based comparator operates like multiple comparators as it oscillates for a different number of cycles while it does not need extra calibration circuit or redundant cycle. The offset problem must be analyzed very carefully.

The delay time of the unit delay stage is given by

$$t_d = \frac{C_L V_{dd}}{2I_{DS}}, \quad (1)$$

where  $C_L$  and  $I_{DS}$  are the load capacitance and average current of the current-starving stage, respectively. And the differential voltage-to-time gain of the VCO for one oscillation cycle is given by

$$G_{VCO\_1} = \frac{2C_L V_{dif} g_m}{I_{DS}^2}, \quad (2)$$

where  $g_m$  is the trans-conductance of the tail NMOS, and  $V_{dif}$

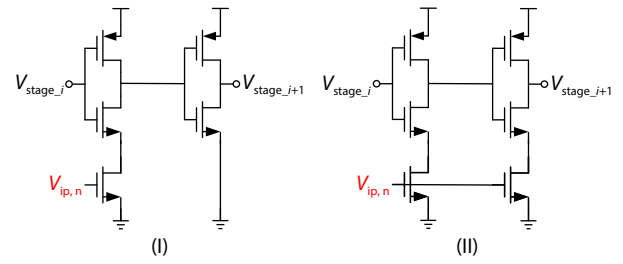


Fig. 4. Schematic of two common delay cells.

is the differential input voltage of the VCO comparator.

The dead zone of the PD ( $t_{dz}$ ) represents the minimum detectable delay difference. The difference input voltage has the following relationship with the number of oscillations  $n$ <sup>[17]</sup>,

$$|(n-1)G_{VCO\_1}V_{dif}| \leq t_{dz} < |nG_{VCO\_1}V_{dif}|. \quad (3)$$

According to Eq. (2), Eq. (3) can be rewritten as

$$\frac{t_{dz}^2 I_{DS}^2}{2ng_m C_L V_{DD}} < |V_{dif}| \leq \frac{t_{dz}^2 I_{DS}^2}{2(n-1)g_m C_L V_{DD}}. \quad (4)$$

Eq. (4) means that the number of oscillations is the coarse quantization of the input signal, i.e., each NOC value corresponds to an input range.

Since the current of the unbiased circuit is much larger than that of the biased transistor, the offset voltage caused by the unbiased circuit can be ignored. For one oscillation cycle, the VCO in Fig. 5 can be considered as a four-stage VCDL. Hence, according to Ref. [10], the standard deviation of the offset time due to one oscillation cycle can be written as

$$\Delta t_{dVCO\_1} = \frac{g_m \Delta V_{os} C_L V_{dd}}{I_{DS}^2}, \quad (5)$$

where  $\Delta V_{os}$  is the standard deviation of the input-referred offset voltage of one delay stage. And the standard deviation of the input-referred offset voltage induced by single oscillation becomes

$$\Delta V_{osVCO\_1} = \frac{\Delta t_{dVCO\_1}}{G_{VCO\_1}} = \frac{\Delta V_{os}}{2}. \quad (6)$$

No matter how many cycles are needed in the oscillation loop, signals oscillate in the same circuit paths. The offset delay time of a fabricated chip remains unchanged for each oscillation cycle. Hence, the standard deviation of the offset time caused by  $n$  oscillation cycles is  $n \cdot \Delta V_{osVCO\_n}$ . So the input-referred offset voltage for  $n$  oscillation cycles is

$$\Delta V_{osVCO\_n} = \frac{n \cdot \Delta t_{dVCO\_1}}{G_{VCO\_n}} = \frac{\Delta V_{os}}{2}. \quad (7)$$

Eqs. (6) and (7) show that the input-referred offset voltage of the VCO-based comparator for one oscillation cycle is the same as that of  $n$  oscillation cycles.

The NAND-based phase detector (PD) is shown in Fig. 5. Compared with the DFF-based PD in Ref. [12], it doesn't wait for a slower edge. Therefore, it increases the speed of the comparator. The size of the dead zone and bypass window can be tuned via load capacitors.

The dead zone of the PD can be derived as

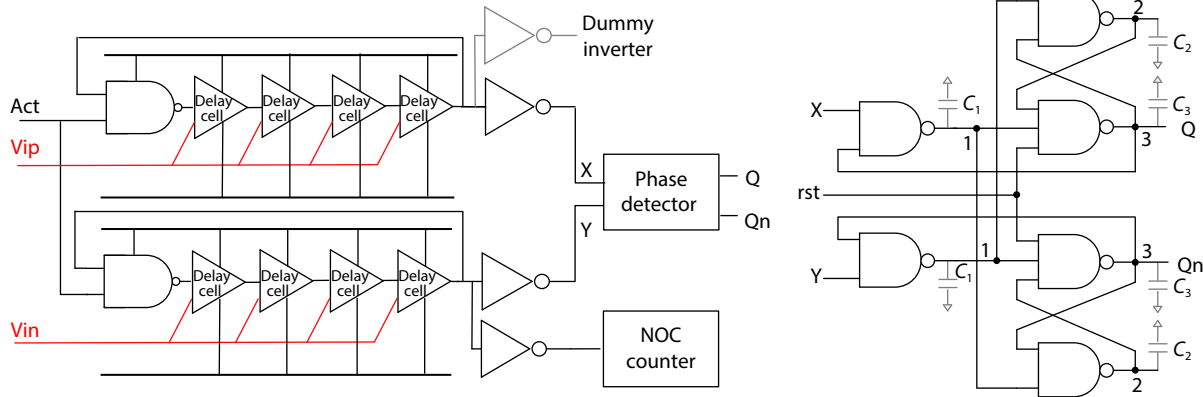


Fig. 5. Schematic of VCO-based comparator and phase detector.

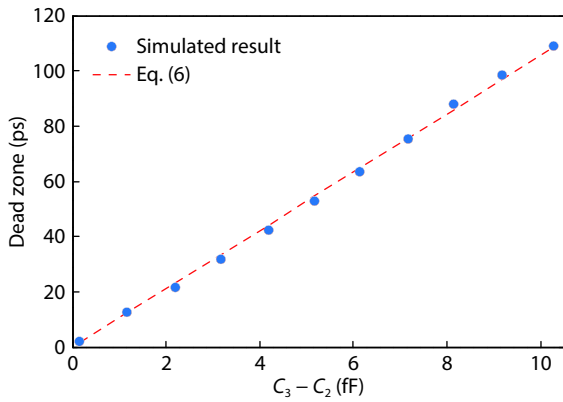


Fig. 6. Comparison of simulated result and Eq. (6) of the dead zone of PD.

$$t_{dz} = \frac{(C_3 - C_2)V_{dd}}{2I_{NAND}}, \quad (8)$$

where  $C_2$  and  $C_3$  are the load capacitors at the output terminals in PD,  $V_{dd}$  is the supply voltage and  $I_{NAND}$  is the average switching current of NAND. The simulated results of the dead zone of PD are shown in Fig. 6, which is accorded with Eq. (8).

### 2.3. Capacitive DAC

This work employs a split capacitor switching scheme<sup>[29]</sup> from MSB to LSB + 1. Compared with many other switching schemes, it not only keeps the input common-mode voltage of comparator stable, which avoids the deterioration of linearity of ADC, but also eliminates the need of extra common-mode voltage. For the LSB, the design uses the monotonic switching procedure<sup>[30]</sup>. It can halve the total capacitance with a fixed unit capacitor. Moreover, the change of common-mode voltage caused by it is negligible. To meet the requirements of  $KT/C$  noise and matching, this design chooses the unit capacitor as 1fF. The weight of the capacitor is shown in Fig. 1.

### 2.4. Bit-cycle control logic

In this design, the order of bit cycles is controlled by NOC. Bit cycles are not executed in the order of the conventional SAR ADC because of the bypass and window update logic. Registers should record the current cycle number, cycle number after bypass and the window size after window updating.

Fig. 7(a) shows the schematic and timing diagram of bit cycle control logic. It employs three window registers to record the sizes of three predefined bypass windows. Because of the relatively small size of the window, a 5-bit register can implement every window. **CLR** is the reset signal to reset window registers at power-up. The signal  $W\_flag$  consists of  $W_2\_flag$ ,  $W_3\_flag$ , and  $W_4\_flag$ . The rising edges of them mean that differential input voltage  $V_{dif}$  triggers the corresponding window. The bypass cycle register is utilized to record the bit cycle after the process of the bypass. The decision of the comparator is indicated by the signal **ready**, and **ready\_d** is the delay signal of **ready**. The normal cycle register is used to record the current bit cycle in the normal SA process. Enabling the bypass cycle register or normal cycle register is selected by the signal **SEL**. And **Samp\_n** is the inverted sampling signal and  $en < 12 : 1 >$  is used to control the state of CDAC.

Fig. 7(b) shows the timing diagram of the bit cycle control logic for two conversion periods. Initial **CLR** is low to reset the window registers. When **samp\_n** is low, both the bypass cycle register and the normal cycle register are reset. A low **SEL** means that normal cycle register is enabled. Cycle  $< 12 >$  is set high when the next **ready\_d** rises meaning that the 12th bit is being converted. If the bypass logic is not triggered, the SA cycle will convert the 11th cycle. However, the rising edge of  $W_4\_flag$  means that the bypass window  $W_4$  is triggered. A high **SEL** enables the bypass cycle register and disables the normal cycle register. At the same time, the high **SEL** makes cycle  $< 6 : 1 >$  connect to **byps**  $< 6 : 1 >$ , and it is set to high. Cycle  $< 1 >$  becomes high on the next rising edge, meaning that the conversion from the 11th to the 2nd bit cycle is skipped and the conversion of the 1st bit starts. The rising edge of **error** indicates that  $V_{dif}$  is outside the bypass window *i.g.* and the window  $W_4$  is too small. So the value of the window register increases by one. Then **SEL** is set to low to disable the bypass cycle register and enable the normal cycle register. At the same time, cycle  $< 12 : 1 >$  is reconnected to **norm**  $< 12 : 1 >$ . Therefore, the bit cycles previously bypassed is reconverted, and the 11th bit will be converted in the next cycle.

At the beginning of next sampling period, **SEL** is low and it is a conventional SA process. The rising edge of  $W_4\_flag$  triggers the bypass logic. Since  $W_4 < 5 : 1 >$  has increased from '00000' to '00001'. Then the cycles from the 11th to the 3rd are bypassed. Missing the window size error detection during this cycle, cycle  $< 1 >$  is set to high on the next rising edge of

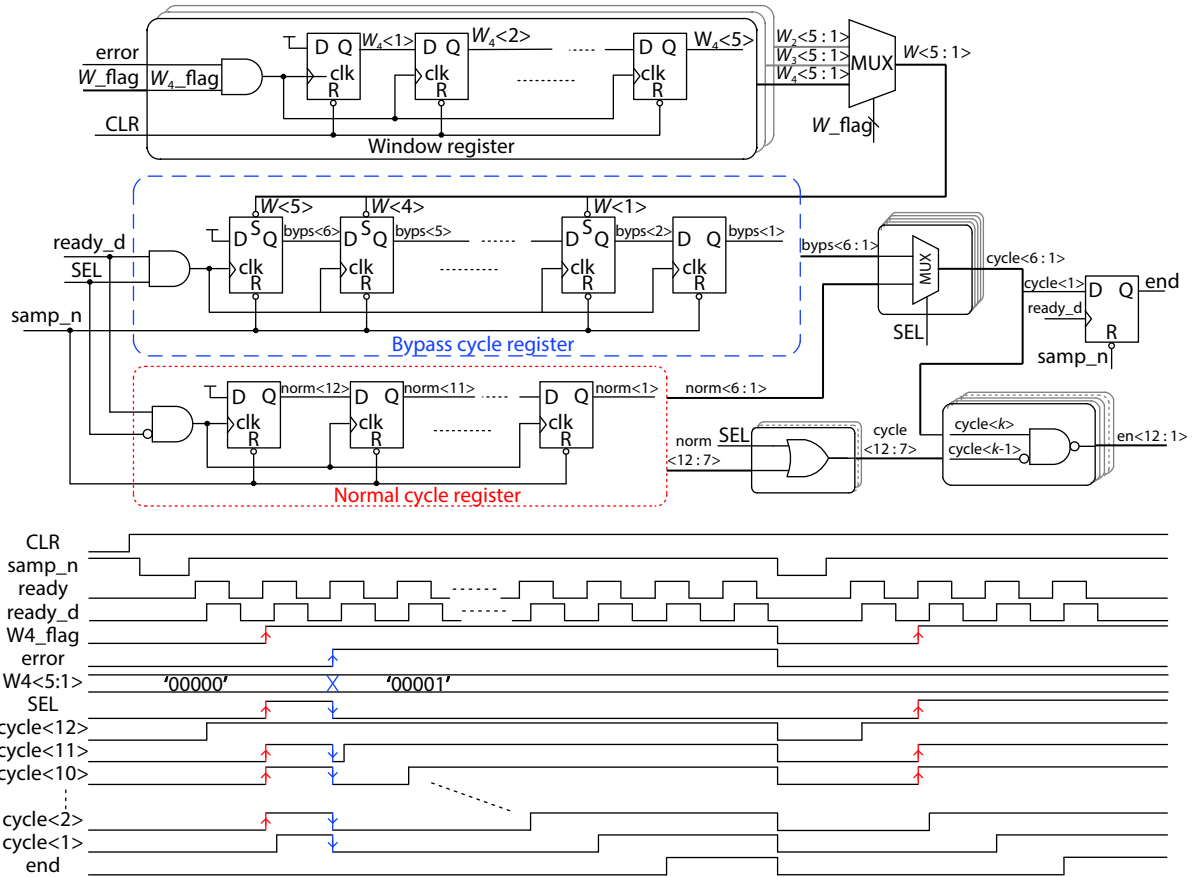


Fig. 7. Bit cycle control circuits. (a) Schematic. (b) Timing diagram.

ready\_d.

## 2.5. CDAC driving circuits

In this design, the CDAC needs to be recovered after the detection of the wrong window size sometimes. The driving circuits of CDAC are shown in Fig. 8. Data\_d and Datan\_d are delay signals of the comparator output.  $\overline{Dp}$  and  $\overline{Dn}$  are inverted signals of Dp and Dn, respectively. When rst is low, Dn is set to high and Dp is set to low. If en is high, high data\_d can set Dp to high and low  $\overline{Dp}$  can lock all outputs until the next effective rst. Similarly, if en is high, high data\_d can set Dn to high and low  $\overline{Dn}$  can lock all outputs until the next effective rst.

In the upper block in Fig. 8(a), samp\_n can be used as a reset signal to reset this block in the sampling phase. Cycle < 6 : 1 > can work as the reset signal in the lower block to recover the wrong switches due to the wrong bypass window size. For example, in Fig. 7, in the first sampling period, after the rising edge of W4\_flag, the output of the comparator is locked in Dp < 1 > and Dn < 1 >. At this moment, the window size is wrong. So the rising edge of error set cycle < 1 > to low, so Dp < 1 > and Dn < 1 > are reset directly. Therefore, these circuits do not need extra blocks to complete the recovery from the wrong switches in CDAC.

## 3. Multiple adaptive bypass windows

The NOC of the VCO-based comparator can be used to construct multiple bypass windows without additional references and comparators. The power reduction and static performances with multiple bypass windows are discussed in detail.

### 3.1. Power reduction with multiple adaptive bypass windows

Fig. 9 shows two conversion periods of a 6-bit SAR ADC without and with different bypass windows, respectively. In Fig. 9(a), 6 SA cycles are needed in every conversion period for conventional SAR ADC no matter how much the input signal is. For the SAR ADC with a wide bypass window, shown in Fig. 9(b), the differential signal is likely located in the range of the bypass window. But the bypass logic can only bypass a few SA cycles, and hence the power efficiency improvement is limited. For the SAR ADC with a narrow bypass window, shown in Fig. 9(c),  $V_{dif}$  has fewer opportunities to be detected within the bypass window. However, the bypass logic can bypass more numbers of SA cycles for the detected signal. The conversion process in Fig. 9(d) shows that the SAR ADC with multiple adaptive bypass windows will improve conversion efficiency extremely.

For general signals with uniform input, Fig. 10 shows the number of SA cycles per sample of a 12-bit SAR ADC with different bypass windows. The voltage range of a single wide or narrow bypass windows is  $\pm 16$  LSB or  $\pm 1$  LSB, respectively. For the wide bypass window, the bypass logic can reduce the number of SA cycles within a large input signal range, which achieves 11.06 SA cycles per sample on average. For the narrow bypass window, though the bypass logic can be employed to deal with the smaller input signal range, it can reduce more SA cycles for the signal meeting the size of the bypass window (indicated by the red line in Fig. 10), leading to 11.69 SA cycles per sample on average.

For the SAR ADC with multiple adaptive bypass windows,



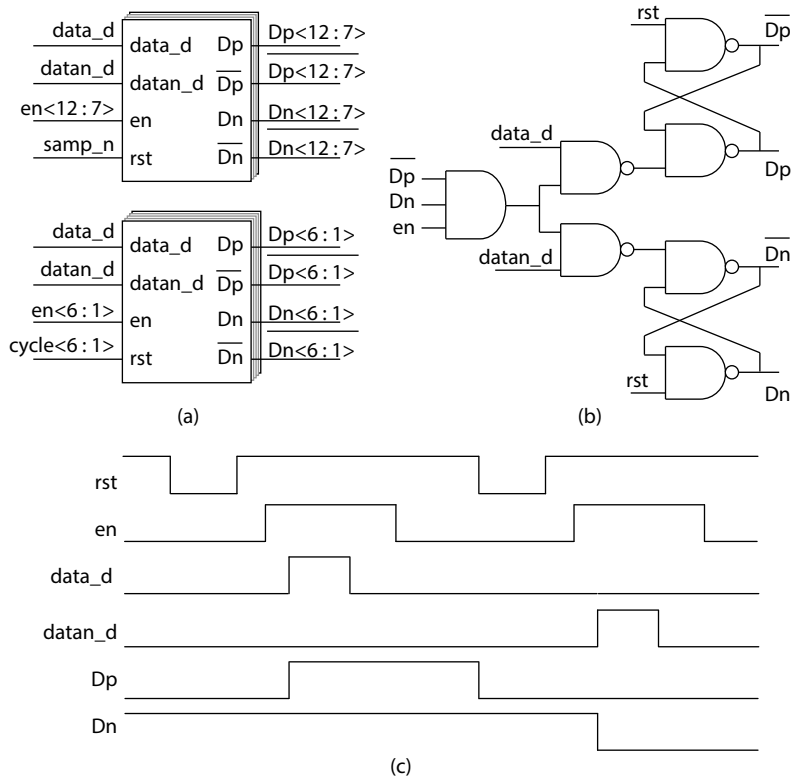


Fig. 8. CDAC driving circuits. (a) Blocks. (b) Schematic. (c) Timing diagram.

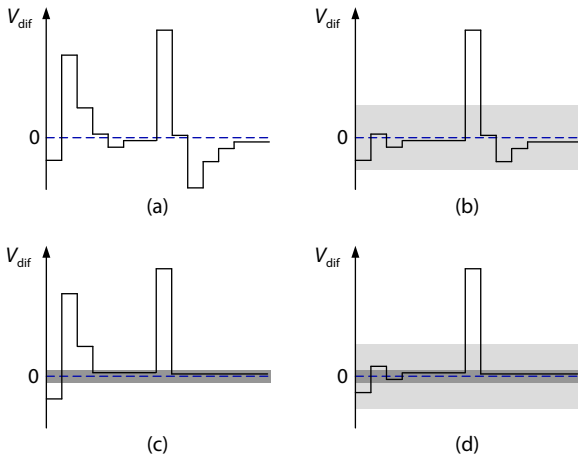


Fig. 9. Conversion processes of 6-b SAR ADCs. (a) Without bypass window. (b) Wide bypass window. (c) Narrow bypass window. (d) Multiple adaptive bypass windows.

this design uses three bypass windows. The simulation result shows that the SAR ADC with multiple adaptive bypass windows responds to large input signal range. Additionally, for small input voltage, the bypass logic can save more SA cycles. In other words, the SAR ADC with multiple adaptive bypass windows takes advantage of both the wide and narrow bypass windows. The size of the three bypass windows is initialized to 1 LSB, when the circuit starts to work. The window size has a correction process, and the three windows corresponding to NOC = 2, 3 and 4 will eventually stabilize on a certain size<sup>[17]</sup>. The convergence results are related to the design of the VCO comparator. In this design, the sizes of the three windows converge to  $\pm 16$  LSB,  $\pm 4$  LSB and  $\pm 2$  LSB. And the SAR ADC with three bypass windows achieves 10.75 cycles per sample on average. The power consumption of the SAR

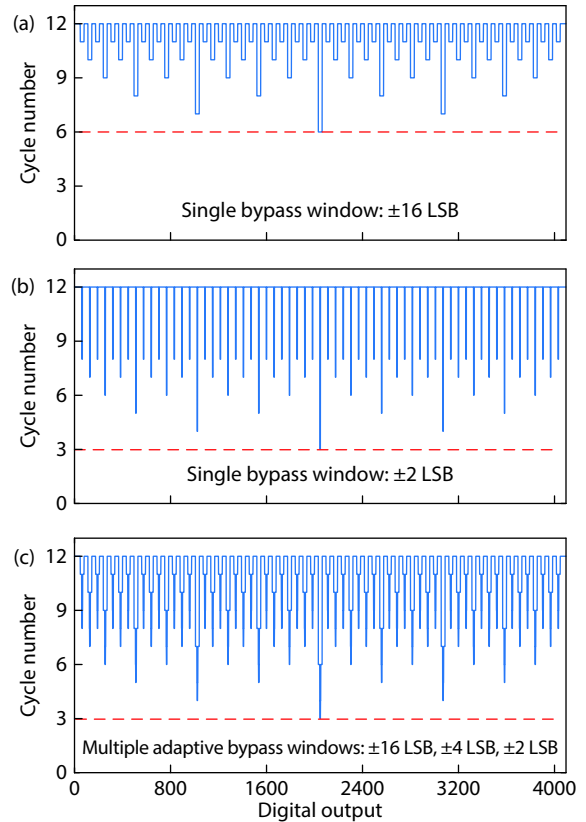


Fig. 10. (Color online) SA cycles per sample. (a) Wide bypass window. (b) Narrow bypass window. (c) Multiple adaptive bypass windows.

ADC mainly consists of the power of DAC, comparator and control logic. Reducing the SA cycle can reduce the power of the DAC, comparator and control logic at the same time. There is a case worth mentioning: where the clock cycles should be

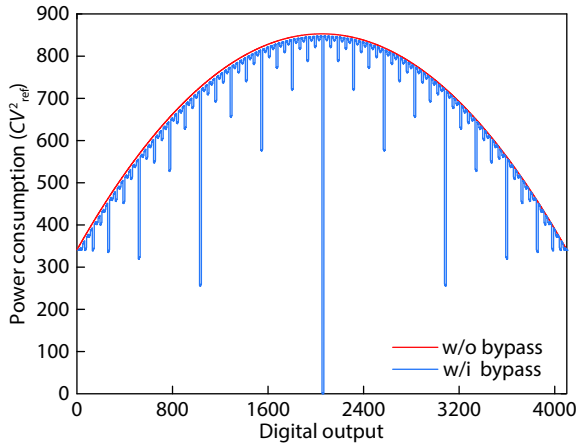


Fig. 11. Switching power consumption with/without bypass logic.

beyond 12 when the size of bypass window is wrong. However, because the change of window size is mainly caused by PVT change, the correct bypass window can be used in subsequent ADC conversion, without the need to detect the wrong bypass window every cycle and waste power. Consequently, the SAR ADC with multiple adaptive bypass windows can save more power than that with a single bypass window.

When three bypass windows sizes are assumed as  $\pm 16$  LSB,  $\pm 4$  LSB and  $\pm 2$  LSB respectively, and the probability density function of the output code is assumed as a uniform distribution, Fig. 11 shows the power consumption by switching with and without bypass logic. The average switching energy with bypass logic is  $602.92 CV_{ref}^2$  which is 11.62% lower than the switching energy without bypass logic ( $682.17 CV_{ref}^2$ ). If there is only one bypass window used, the switching energy is 605.89, 654.89 and 666.63  $CV_{ref}^2$  for  $W_2$ ,  $W_3$ , and  $W_4$ , respectively.

It is worth noting that the narrow window like  $W_4$  failing to decrease too much bit cycles and switching power comes as no surprise. This is because the input signal is assumed as uniform here and the power efficiency of bypass logic is tied to the characteristics of signals. For many biomedical signals concentrating on the adjacent of common-mode voltage, this shows small variations in magnitude can save much power with bypass logic<sup>[7, 31]</sup>. In contrast with the single bypass window of prior works, the technique of multiple adaptive bypass windows is more versatile for different characteristics of input signals.

### 3.2. Static performance analysis of SAR ADC with multiple adaptive bypass windows

The state of capacitors in a split capacitor array is illustrated in Fig. 12. When the control code is changed from 'X' to '1',  $C_{up}$  is switched; when the control code is changed from 'X' to '0',  $C_{dn}$  is switched. Considering the mismatch of capacitors, different error voltages are introduced into the system by  $C_{up}$  and  $C_{dn}$  if the control codes are different.

The output voltage of the proposed SAR ADC is given by

$$V(S) = \frac{\sum_{i=1}^{N-1} (C_{up_i} b_{up_i} - C_{dn_i} b_{dn_i}) + C_0 b_{up_0}}{C_{total}} V_{ref}, \quad (9)$$

$$DNL = \left[ C_{dn_{N-1}} - \sum_{i=M+1}^{N-2} C_{up_i} - (C_{up_M} + C_{dn_M}) + (C_{up_{M-1}} + C_{dn_{M-1}}) - \sum_{i=j}^{M-2} (C_{up_i} + C_{dn_i}) - C_0 \right] \cdot \frac{V_{ref}}{C_{total}}. \quad (10)$$

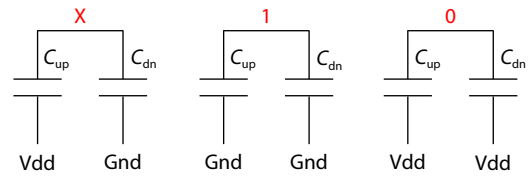


Fig. 12. The state of capacitors in split capacitor array.

If the control code of the DAC  $S[j] = 1$ ,  $b_{up_j} = 1$  and  $b_{dn_j} = 0$ ; if  $S[j] = 0$ ,  $b_{up_j} = 0$  and  $b_{dn_j} = 1$ ; if  $S[j] = X$ ,  $b_{up_j} = 0$  and  $b_{dn_j} = 0$ .  $C_{up_j}$  and  $C_{dn_j}$  are the actual values (with mismatch errors) of the corresponding capacitors.  $C_0$  is the unit capacitance. Since the mismatch errors of high-weighted capacitors influence the conversion results, much more greatly than that of the low-weighted capacitors, the maximum DNL occurs at the minimum code with the largest bypass window. Assuming the maximum bypass window  $W_2 = 5$  ( $\pm 16$  LSB), the maximum DNL will occur at  $S = 'XXXXXX010000'$ , which can be decoded into the standard binary code as  $D_{out} = '01111110000'$  by the state of capacitor array. The control code for  $D_{out} = '01111110000' - '1'$  is  $S = '011111101111'$ . So the voltage difference can be written as

$$DNL = V(XXXXXX010000) - V(011111101111). \quad (11)$$

Assuming  $\sigma_0$  is the standard deviation of the random error of a unit capacitor, from Eqs. (9) and (11), the DNL can be written in LSB as  $\sqrt{1040}\sigma_0/C_0$ . If  $W_2 = M$  and the resolution is  $N$ -bit, Eq. (10) can be derived. So the maximum DNL can be calculated in LSB as

$$DNL_{max} \approx \frac{\sigma_0 \sqrt{2^{N-2} + 2^{M-1}}}{C_0}. \quad (12)$$

Fig. 13 illustrates the DNL performance of a conventional SAR ADC with split capacitor array and the proposed ADC with multiple adaptive bypass windows. The DNL curves are the root-mean-square (RMS) value of 10 000 simulations and each unit capacitor cell has a Gaussian random error with a standard deviation of 1%. The simulation shows the ADC with multiple adaptive bypass windows achieves a better DNL performance than the conventional one.

The definition of INL at bin  $k$  is often defined as  $INL(k) = V(k) - V_{ideal}(k)$ . However, in actual applications,  $V(0)$  is used as the starting point of INL to eliminate the error caused by offset. So the formula of INL is

$$INL(k) = V(k) - V(0) - V_{ideal}(k). \quad (13)$$

If the minimum bypass window  $W_4 = 2$  ( $\pm 2$  LSB), the control code at  $D_{out} = '01111111111'$  is  $S = 'XXXXXXXXX01'$ . The INL at  $D_{out} = '01111111111'$  is

$$INL = V(XXXXXXXXX01) - V(00000000000) - V_{ideal}. \quad (14)$$

So the INL at  $D_{out} = '01111111111'$  can be calculated in LSB as  $32\sigma_0/C_0$ . Similarly, if the minimum bypass window  $W_4 = K$ , the INL at  $D_{out} = '01111111111'$  is

$$INL = \left[ \sum_{i=K+1}^{N-1} C_{dn_i} + \sum_{i=1}^{K-1} (C_{up_i} + C_{dn_i}) + C_0 \right] \frac{V_{ref}}{C_{total}} - V_{ideal}. \quad (15)$$

Since  $C_{up_i}$  and  $C_{dn_i}$  are different in split capacitor array be-

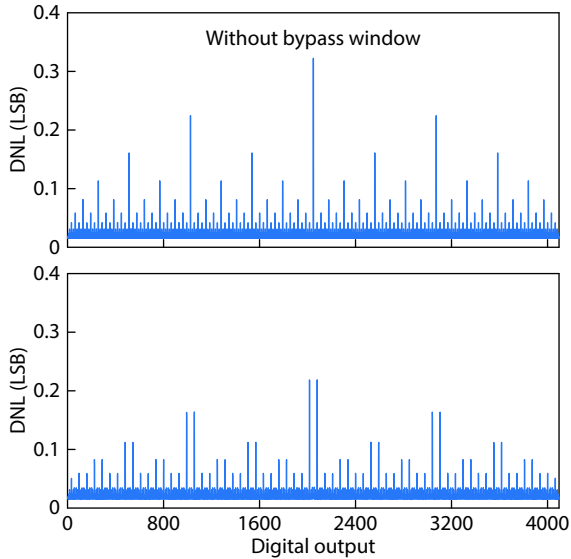


Fig. 13. (Color online) DNL performances of SAR ADC without bypass window and with multiple adaptive bypass windows.

cause of mismatch, Eq. (14) cannot be simplified. So the maximum INL can be calculated in LSB as

$$INL_{max} \approx \frac{\sigma_0 \sqrt{2^{N-2}}}{C_0}, \quad (16)$$

which shows that the maximum INL is independent of the bypass window parameter  $K$ . The INL performance of the SAR ADC with multiple bypass windows (the standard deviation of the Gaussian error of the unit capacitor is 1%) is shown in Fig. 14, and it is the same with the INL performance of a conventional SAR ADC with the split capacitor array<sup>[29]</sup>.

#### 4. Split-and-recombination-based redundancy with adaptive bypass windows

In a high-resolution ADC with relatively high speed, variations on reference voltage lead to wrong decisions. The design avoids the large-area on-chip decoupling capacitor for stabilizing the reference by redundancy. The solution corrects the errors, and it is also favorable for the speed because the requirement for DAC settling is relaxed. Although the bypass logic offers redundancy since there are multiple output presentations for one identical input voltage<sup>[7]</sup>, it is not enough for a 12-bit 30 M/s SAR ADC.

Compared with the binary-scaled error compensation redundancy<sup>[32]</sup>, the split-and-recombination redundancy<sup>[19]</sup> does not need extra compensation capacitors and the sampling capacitance and input range remains unchanged. The main idea of split-and-recombination redundancy is to split MSB into two groups and make the smaller group recombine with LSB capacitors. The most critical point is that each capacitor is not larger than the sum of capacitors smaller than it so that multiple output codes are assigned to one same input signal. A split-and-recombination method (1-bit) shown in Fig. 15 is chosen under the consideration of speed. For designing the digital error correction circuit, it is necessary to derive the expression of  $D_{out}$  first.

##### 4.1. Without bypass logic

If the bypass logic is not applied, the  $D_{out}$  can be written

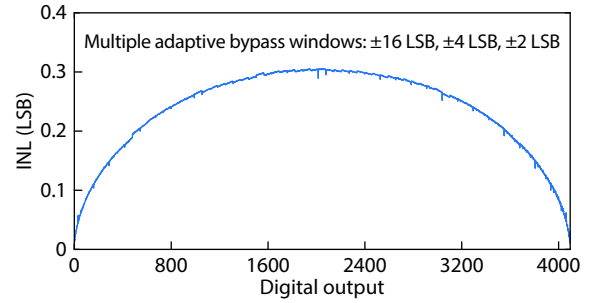


Fig. 14. INL performance of SAR ADC with multiple adaptive bypass windows.

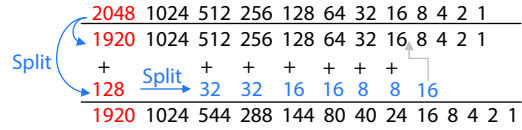


Fig. 15. Split-and-recombination method.

$$\begin{aligned}
 & 2^{10} + 2^9 + 2^8 + 2^7 \\
 & \quad \quad \quad \parallel \\
 D_{out} = & B_{12} \times (2^{11} - 2^7) + B_{11} \times 2^{10} + B_{10} \times (2^9 + 2^5) \\
 & + B_9 \times (2^8 + 2^5) + B_8 \times (2^7 + 2^4) + B_7 \times (2^6 + 2^4) \\
 & + B_6 \times (2^5 + 2^3) + B_5 \times (2^4 + 2^3) + B_4 \times 2^4 + B_3 \times 2^3 \\
 & + B_2 \times 2^2 + B_1 \times 2^1 + B_0 \times 2^0 \\
 = & 2^{10} \times (B_{12} + B_{11}) + 2^9 \times (B_{12} + B_{10}) + 2^8 \times (B_{12} + B_9) \\
 & + 2^7 \times (B_{12} + B_8) + 2^6 \times B_7 + 2^5 \times (B_{10} + B_9 + B_8) \\
 & + 2^4 \times (B_8 + B_7 + B_5 + B_4) + 2^3 \times (B_6 + B_5 + B_3) \\
 & + 2^2 \times B_2 + 2^1 \times B_1 + 2^0 \times B_0
 \end{aligned}$$

Fig. 16. Expression of  $D_{out}$  without bypass logic.

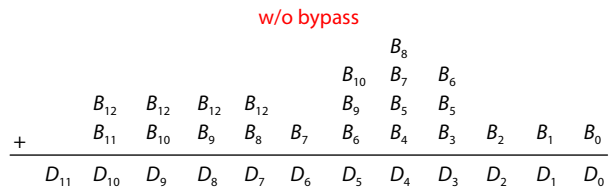


Fig. 17. Expression of  $D_{out}$  without bypass logic.

as Fig. 16. And  $D_{out}$  also can be expressed as Fig. 17. The digital error correction logic can be designed according to this expression similar to the implementation in Ref. [19].

##### 4.2. With bypass logic

The proposed bypass logic requires us to know the weights of the bypassed cycles. For example, it needs to search four times without bypass logic for  $V_{in} = 8$  as shown in Fig. 18. The weight of every bit is 8, 4, 2 and 1, respectively. So the output is obtained by  $8 \times 1 + 4 \times 0 + 2 \times 0 + 1 \times 0 = 8$ . For  $V_{in} = 8$  with bypass logic, the first and second cycles are bypassed. So  $V_{in}$  must be located in areas I and II. The third and fourth comparison results are 1 and 0, respectively. So the output is  $XX10$  ( $X$  stands for the bit bypassed). In this way, the output can be expressed as  $4 \times 1 + 2 \times 1 + 2 \times 1 + 1 \times 0 = 8$ .

In short, bypassing one bit requires the addition of half weight of this bit to the output regardless of binary or non-binary weight. In accordance with this general conclusion for bypass logic, the  $D_{out}$  can be expressed as shown in Fig. 19 and





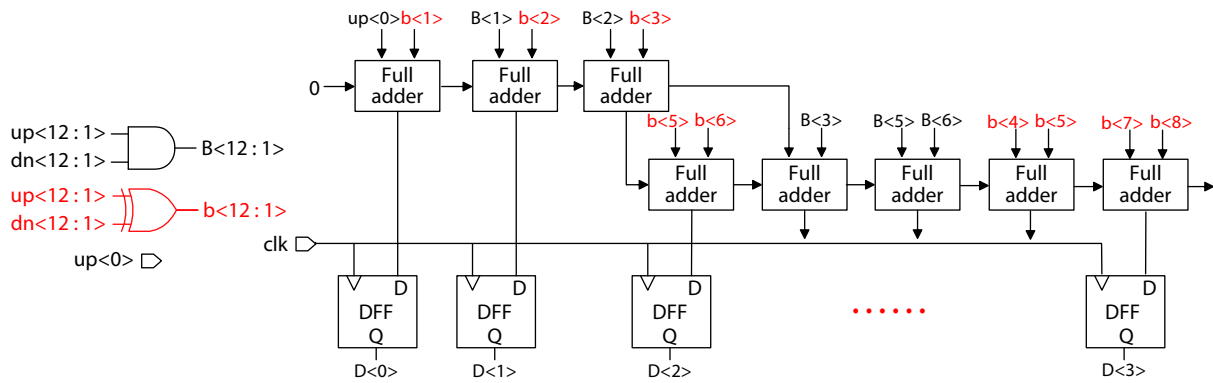


Fig. 20. Part of implementation of digital error correction logic.

Table 1. Performance comparison of SAR ADCS with time-domain comparators.

Parameter	JSSC 2011 <sup>[10]</sup>	TCAS-I 2013 <sup>[33]</sup>	JSSC 2014 <sup>[34]</sup>	ESSCIRC 2014 <sup>[12]</sup>	JSSC 2016 <sup>[24]</sup>	JSSC 2017 <sup>[11]</sup>	JSSC 2019 <sup>[17]</sup>	This Work
Technology (nm)	180	130	180	65	90	65	40	40
Comparator type	VCDL	VCDL	VCDL hybrid	VCO	TDC hybrid	Edge-pursuit	VCO	VCO
Calibration	No	Yes	No	Yes	Yes	Yes	No	No
Supply voltage (V)	0.6	0.5	0.6	0.85	0.7	N/A	1.1	1.1
Conversion rate (MS/s)	0.1	0.01	0.1	1.024	4	0.02	10	30
Resolution (bit)	10	11	10	13	10	15	10	12
SFDR (dB)	64	78	64.2	85.2	71.5	95.1	68.84	85.35
SNDR (dB)	57.5	61.6	56.5	66.4	54.8	74.12	58.57	68.72
ENOB (bit)	9.3	9.93	9.2	10.4	8.81	12.02	9.44	11.12
Power (μW)	1.3	0.73	0.39	45.2	9.25	1.17	47.6	380
FoM (fJ/Conv.-step)	21	74.8	6.7	33	5.16	14.06	6.85	5.69

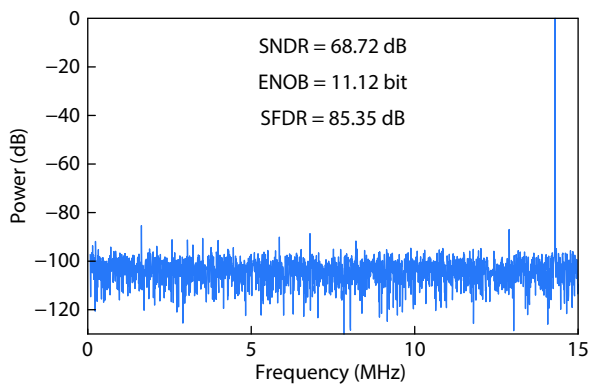


Fig. 21. (Color online) FFT plot with Nyquist input at 30 MS/s.

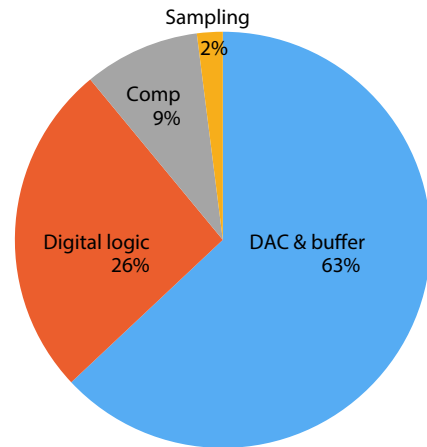


Fig. 23. (Color online) Power breakdown at Nyquist frequency.

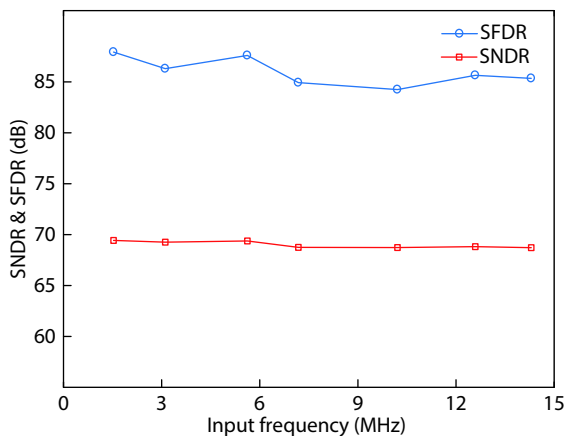


Fig. 22. Dynamic performance versus input frequency.

### Acknowledgements

This work was supported by the National Natural Science Foundation of China under Grant 61534002 and Grant 61761136015.

### References

- [1] Zhu Y, Chan C, Chio U, et al. A 10-bit 100-MS/s reference-free SAR ADC in 90 nm CMOS. *IEEE J Solid-State Circuits*, 2010, 45(6), 1111
- [2] Lin J, Hsieh C. A 0.3 V 10-bit 1.17 f SAR ADC with merge and split switching in 90 nm CMOS. *IEEE Trans Circuits Syst I*, 2015, 62(1), 70
- [3] Sun L, Li B, Wong A K Y, et al. A charge recycling SAR ADC with a

- LSB-down switching scheme. *IEEE Trans Circuits Syst I*, 2015, 62(2), 356
- [4] Lin J, Hsieh C. A 0.3 V 10-bit SAR ADC with first 2-bit guess in 90-nm CMOS. *IEEE Trans Circuits Syst I*, 2017, 64(3), 562
- [5] Pang W, Wang C, Chang Y, et al. A 10-bit 500-kS/s low power SAR ADC with splitting comparator for bio-medical applications. 2009 IEEE Asian Solid-State Circuits Conference, 2009, 149
- [6] Zhu Z, Liang Y. A 0.6-V 38-nW 9.4-ENOB 20-kS/s SAR ADC in 0.18- $\mu$ m CMOS for medical implant devices. *IEEE Trans Circuits Syst I*, 2015, 62(9), 2167
- [7] Huang G, Chang S, Liu C, et al. A 1- $\mu$ W 10-bit 200-kS/s SAR ADC with a bypass window for biomedical applications. *IEEE J Solid-State Circuits*, 2012, 47(11), 2783
- [8] Nuzzo P, De Bernardinis F, Terreni P, et al. Noise analysis of regenerative comparators for reconfigurable ADC architectures. *IEEE Trans Circuits Syst I*, 2008, 55(6), 1441
- [9] Agnes A, Bonizzoni E, Malcovati P, et al. A 9.4-ENOB 1 V 3.8- $\mu$ W 100 kS/s SAR ADC with time-domain comparator. 2008 IEEE International Solid-State Circuits Conference, 2018, 246
- [10] Lee S, Park S, Park H, et al. A 21 fJ/conversion-step 100 kS/s 10-bit ADC with a low-noise time-domain comparator for low-power sensor interface. *IEEE J Solid-State Circuits*, 2011, 46(3), 651
- [11] Shim M, Jeong S, Myers P D, et al. Edge-pursuit comparator: An energy-scalable oscillator collapse-based comparator with application in a 74.1 dB SNDR and 20 kS/s 15 b SAR ADC. *IEEE J Solid-State Circuits*, 2017, 52(4), 1077
- [12] Yoshioka K, Ishikuro H. A 13b SAR ADC with eye-opening VCO based comparator. ESSCIRC 2014: 40th European Solid State Circuits Conference (ESSCIRC), 2014, 411
- [13] Kao C, Hsieh S, Hsieh C. A 0.5 V 12-bit AR ADC using adaptive timedomain comparator with noise optimization. 2017 IEEE Asian Solid-State Circuits Conference (A-SSCC), 2017, 213
- [14] Harpe P, Cantatore E, van Roermund A. A 10b/12b 40 kS/s SAR ADC with data-driven noise reduction achieving up to 10.1b ENOB at 2.2 fJ/conversion-step. *IEEE J Solid-State Circuits*, 2013, 48(12), 3011
- [15] Ahmadi M, Namgoong W. A 3.3fJ/conversion-step 250 kS/s 10b SAR ADC using optimized vote allocation. Proceedings of the IEEE 2013 Custom Integrated Circuits Conference, 2013, 1
- [16] Chen L, Tang X, Sanyal A, et al. A 0.7-V 0.6- $\mu$ W 100-kS/s low-power SAR ADC with statistical estimation-based noise reduction. *IEEE J Solid-State Circuits*, 2017, 52(5), 1388
- [17] Ding Z, Zhou X, Li Q. A 0.5–1.1-V adaptive bypassing SAR ADC utilizing the oscillation-cycle information of a VCO-based comparator. *IEEE J Solid-State Circuits*, 2019, 54(4), 968
- [18] Chang S, Zhou X, Ding Z, et al. A 12-bit 30 MS/s SAR ADC with VCO-based comparator and split-and-recombination redundancy for bypass logic. 2019 IEEE International Symposium on Circuits and Systems (ISCAS), 2019, 1
- [19] Liu C, Kuo C, Lin Y. A 10 bit 320 MS/s low-cost SAR ADC for IEEE 802.11ac applications in 20 nm CMOS. *IEEE J Solid-State Circuits*, 2015, 50(11), 2645
- [20] Abo A M, Gray P R. A 1.5 V, 10-bit, 14 MS/s CMOS pipeline analog-to-digital converter. 1998 Symposium on VLSI Circuits, 1998, 166
- [21] Kim J, Leibowitz B S, Ren J, et al. Simulation and analysis of random decision errors in clocked comparators. *IEEE Trans Circuits Syst I*, 2009, 56(8), 1844
- [22] Abidi A A. Phase noise and jitter in CMOS ring oscillators. *IEEE J Solid-State Circuits*, 2006, 41(8), 1803
- [23] Tai H, Hu Y, Chen H, et al. 11.2 A 0.85fJ/conversion-step 10b 200 kS/s subranging SAR ADC in 40 nm CMOS. 2014 IEEE International Solid-State Circuits Conference, 2014, 196
- [24] Chen Y, Chang K, Hsieh C. A 2.02–5.16 fJ/conversion step 10 bit hybrid coarse-fine SAR ADC with time-domain quantizer in 90 nm CMOS. *IEEE J Solid-State Circuits*, 2016, 51(2), 357
- [25] Chan C, Zhu Y, Ho I, et al. 16.4 a 5 mW 7b 2.4 GS/s 1-then-2b/cycle SAR ADC with background offset calibration. 2017 IEEE International Solid-State Circuits Conference (ISSCC), 2017, 282
- [26] Yoshioka K, Shikata A, Sekimoto R, et al. An 8 bit 0.35–0.8 V 0.5–30 MS/s 2 bit/step SAR ADC with wide range threshold configuring comparator. 2012 Proceedings of the ESSCIRC (ESSCIRC), 2012, 381
- [27] Ragab K, Sun N. A 1.4 mW 8b 350 MS/s loop-unrolled SAR ADC with background offset calibration in 40 nm CMOS. ESSCIRC Conference 2016: 42nd European Solid-State Circuits Conference, 2016, 417
- [28] Chang A H, Lee H, Boning D. A 12b 50 MS/s 2.1 mw SAR ADC with redundancy and digital background calibration. 2013 Proceedings of the ESSCIRC (ESSCIRC), 2013, 109
- [29] Ginsburg B P, Chandrakasan A P. 500-MS/s 5-bit ADC in 65-nm CMOS with split capacitor array DAC. *IEEE J Solid-State Circuits*, 2007, 42(4), 739
- [30] Liu C, Chang S, Huang G, et al. A 10-bit 50-MS/s SAR ADC with a monotonic capacitor switching procedure. *IEEE J Solid-State Circuits*, 2010, 45(4), 731
- [31] Wang T, Li H, Ma Z, et al. A bypass-switching SAR ADC with a dynamic proximity comparator for biomedical applications. *IEEE J Solid-State Circuits*, 2018, 53(6), 1743
- [32] Liu C, Chang S, Huang G, et al. A 10b 100 MS/s 1.13 mW SAR ADC with binary-scaled error compensation. 2010 IEEE International Solid-State Circuits Conference (ISSCC), 2010, 386
- [33] Um J, Kim Y, Song E, et al. A digital-domain calibration of split-capacitor DAC for a differential SAR ADC without additional analog circuits. *IEEE Trans Circuits Syst I*, 2013, 60(11), 2845
- [34] Jin J, Gao Y, Sánchez-Sinencio E. An energy-efficient time-domain asynchronous 2 b/step SAR ADC with a hybrid r-2r/c-3c DAC structure. *IEEE J Solid-State Circuits*, 2014, 49(6), 1383