Deceleration-stage Rayleigh–Taylor growth in a background magnetic field studied in cylindrical and Cartesian geometries

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ABSTRACT

Experiments have identified the Rayleigh–Taylor (RT) instability as one of the greatest obstacles to achieving inertial confinement fusion. Consequently, mitigation strategies to reduce RT growth and fuel–ablomer mixing in the hotspot during the deceleration phase of the implosion are of great interest. In this work, the effect of seed magnetic fields on deceleration-phase RT growth are studied in planar and cylindrical geometries under conditions relevant to the National Ignition Facility (NIF) and Omega experiments. The magnetohydrodynamic (MHD) and resistive-MHD capabilities of the FLASH code are used to model imploding cylinders and planar blast-wave-driven targets. Realistic target and laser parameters are presented that suggest the occurrence of morphological differences in late-time RT evolution in the cylindrical NIF case and a measurable difference in spike height of single-mode growth in the planar NIF case. The results of this study indicate the need for target designs to utilize an RT-unstable foam–foam interface in order to achieve sufficient magnetic field amplification to alter RT evolution. Benchmarked FLASH simulations are used to study these magnetic field effects in both resistive and ideal MHD.

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I. INTRODUCTION

Pre-magnetization of inertial confinement fusion (ICF) targets has been proposed as a means to achieve high energy gain due to the reduced ignition threshold and increased yield.1,2 One of the instabilities identified as a primary contributor to degradation of ICF implosions3,4 is the Rayleigh–Taylor (RT) instability.5,6 The presence of the RT instability in an ICF capsule disrupts convergence, which in turn can reduce the hotspot temperatures necessary for ignition. Although RT spikes are predicted to generate magnetic fields in the hotspot, they do not significantly alter the hydrodynamics (HD) or thermal conduction.7–9

Mitigation of the growth of the RT instability10–12 and fuel–ablomer mixing13–16 in ICF implosions is pivotal to improving capsule performance. One scheme aimed at achieving this is the use of strong pre-seeded magnetic fields.17 RT instability in the ablative acceleration phase of ICF implosion has been extensively studied both computationally and experimentally, but it is deceleration-phase RT instability that has a direct effect on the hotspot. The deceleration phase occurs when the low-density, high-pressure interior begins pushing back on the higher-density, lower-pressure imploding liner. Some theoretical work18,19 has been performed, and experimental efforts20–24 are beginning to probe...
cylindrical implosions in unmagnetized targets specifically to study deceleration-phase RT instability in a converging geometry. Additionally, a great deal of work has been done on planar blast-wave-driven RT instability growth, particularly in an astrophysical context, though most of the magnetization taken into consideration has been explored in the context of self-generated magnetic fields.\textsuperscript{13–14}

Magneto-RT (MRT) instabilities are known to occur in the cylindrical geometry of imploding liners in pulsed-power magnetohydrodynamic fusion experiments such as Magnetized Liner Inertial Fusion (MagLIF).\textsuperscript{4,7} Experiments have measured MRT growth on the Z facility and have compared it with MRT theory in cylindrical geometry.\textsuperscript{7} The presence of seeded axial magnetic fields in combination with the azimuthal magnetic fields that occur in a Z pinch could significantly affect RT instability growth and development in MagLIF.\textsuperscript{28,39} Hence, investigating the effect of magnetic fields on the development of RT instability in cylindrical geometry can play a significant role in mitigating the growth of the instability in laser- and pulsed-power-driven fusion concepts.

The standard evolution of the RT instability is generally understood via the classical description of two fluids with differing densities $\rho_1$ and $\rho_2$ (with $\rho_2 > \rho_1$) subject to a constant acceleration $g$ opposing the density gradient. A perturbation at the interface with wavenumber $k = 2\pi/\lambda$ results in a growth rate of $\gamma^2 = kgA_1$, where $A_1 = (\rho_2 - \rho_1)/(\rho_2 + \rho_1)$ is the Atwood number. In the presence of a magnetic field, the growth rate becomes\textsuperscript{40,41}
\begin{equation}
\gamma^2 = kgA_1 - \frac{2B^2k^2\cos^2 \theta}{\rho_0(\rho_2 - \rho_1)},
\end{equation}
where $\theta$ is the angle between the magnetic field and the wave vector $k$. The immediate effect of the magnetic field on RT instability can be seen from the existence of a critical wavelength $\lambda_c = 4\pi B^2 \cos^2 \theta /[\mu_0 \rho_0 (\rho_2 - \rho_1)]$ such that perturbations with a wavelength smaller than $\lambda_c$ are stabilized.

A magnetic field inside an ICF implosion will be amplified by magnetic flux compression.\textsuperscript{1,4} Owing to this amplification, magnetic fields are predicted to affect the RT spike morphology and subsequent evolution of the Kelvin–Helmholtz (KH) instability.\textsuperscript{4,5} The level of field amplification is characterized by the magnetic Reynolds number $R_m$, which is a measure of the ratio of fluid advection to magnetic diffusion. When $R_m \gg 1$, the fluid is highly conducting, and a seeded magnetic field is approximately frozen-in. Plasma conditions in the hotspot produce an $R_m$ of $\sim 10^4$, suggesting amplification factors of several hundred.\textsuperscript{1} Under these conditions, an appropriately applied seed magnetic field may help reduce RT growth and mixing in the hotspot, improving the efficiency of the implosion.

Deceleration-phase RT instability has the potential to truly disrupt convergence of ICF implosions by mixing the cold ablator with the hot fuel. The use of appropriately aligned seeded magnetic fields can produce conditions in which the RT instability could be mitigated with sufficient amplification ($R_m \gg 1$). Additionally, the ratio of dynamic pressure to magnetic pressure, $\beta = 2\mu_0 n_i B^2$, characterizes the level to which the magnetic field can alter hydrodynamic evolution. Hydrodynamic systems with a low beta ($\beta \lesssim 1$) will be greatly affected by a magnetic field. Recent computational and experimental work\textsuperscript{11} suggests that morphological effects in deceleration-phase RT evolution begin to occur at $\beta \lesssim 100$.

The work presented here studies the effect of magnetic fields on the RT instability in planar and cylindrical geometries. Planar geometry is relatively simple to diagnose, while cylinders allow diagnostic access and incorporate the effects of geometric convergence. Cylinders have been used to study hydrodynamic instabilities for many years,\textsuperscript{2,3,44} and the Los Alamos National Laboratory has recently revitalized such a platform.\textsuperscript{21–23} Both the planar target and the cylinder consist of a high-density pusher layer that is accelerated into a lower-density foam via laser direct drive. This work considers targets designed for both Omega\textsuperscript{45} and the National Ignition Facility (NIF).\textsuperscript{46} With additional development, seeded background magnetic fields of $\sim 30$ T may become accessible on NIF and Omega, and so a solid-density Omega-scale cylindrical configuration and a foam configuration for Omega-scale planar and NIF-scale cylindrical and planar targets are simulated.

Understanding the potential effects of a seed magnetic field on RT instability growth is the primary motivation for this work. A large magnetic Reynolds number is required to access the regimes where magnetic stabilization can occur, but this requires sufficiently high temperatures. This is evident in the standard Spitzer resistivity model, where the resistive diffusion of the magnetic field scales inversely with temperature. The standard model of using resistivity for an ICF implosion requires that the resistivity be sufficiently small that diffusive effects are limited. The work presented here focuses on simulations performed using radiation hydrodynamics only (HD), ideal-magnetohydrodynamics (MHD), or resistive MHD models in cylindrical and planar geometries.

The remainder of the paper is structured as follows. Section II presents code descriptions for FLASH. Section III presents the results of simulations using a cylindrical design at Omega and the NIF, and Sec. IV presents the results of simulations of experiments on Omega and the NIF using a planar platform. Conclusions are presented in Sec. V.

The key contributions of this paper are as follows. First, this work compares the expected results for a magnetized solid-density ICF target with those of a novel foam target design. Second, it predicts relevant parameters necessary to achieve the desired temperatures and magnetic Reynolds numbers under which a magnetized ICF experiment will see the mitigating effects of an externally applied magnetic field.

II. NUMERICAL MODEL

The models and numerical methods used are briefly outlined in this section. FLASH is an Eulerian multiphysics radiation-hydrodynamics code developed by the FLASH Center, now located at the University of Rochester,\textsuperscript{47} with adaptive mesh refinement capabilities, which are used to solve hyperbolic and stiff parabolic systems. The ICF configurations presented are modeled with the Euler equations, the ideal-MHD equations, and the resistive-MHD equations from FLASH.\textsuperscript{48} The specific Euler equations used in this study are given as\textsuperscript{49}
\begin{align*}
\frac{\partial \mathbf{u}}{\partial t} + \nabla \cdot (\rho \mathbf{u}) &= 0, \\
\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{u}) &= \rho g, \\
\frac{\partial \rho E}{\partial t} + \nabla \cdot [(\rho E + P)\mathbf{u}] &= \rho \mathbf{u} \cdot \nabla. 
\end{align*}
where $\rho$, $\mathbf{u}$, and $P$ are the fluid density, velocity, and pressure, respectively, $E$ is the sum of the internal energies, $g$ is acceleration, and $t$ is the time coordinate. For the MHD systems, FLASH solves

$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{u}) = 0,$$

(5)

$$\frac{\partial \rho \mathbf{u}}{\partial t} + \nabla \cdot [(\rho \mathbf{u} - \mathbf{B}) \cdot \mathbf{B}] + \nabla p = \rho g,$$

(6)

$$\frac{\partial \rho E}{\partial t} + \nabla \cdot [\mathbf{u}(\rho E + p) - \mathbf{B} \cdot \mathbf{B}] = \rho g \cdot \mathbf{u} + \nabla \cdot \left( \sigma \nabla T + \nabla \cdot [\eta \nabla \times \mathbf{B}] \right),$$

(7)

$$\frac{\partial \mathbf{B}}{\partial t} + \nabla \cdot (\mathbf{u} \mathbf{B} - \mathbf{B} \mathbf{B}) = -\nabla \times (\eta \nabla \times \mathbf{B}),$$

(8)

where

$$p^e = p + \frac{B^2}{2},$$

(9)

$$E = \frac{1}{2} \mathbf{u}^2 + \epsilon + \frac{1}{2} \frac{B^2}{\rho},$$

(10)

$T$ is the temperature, $\mathbf{B}$ is the magnetic field, $p$ is the thermal pressure, $\sigma$ is the heat conductivity, and $\eta$ is the resistivity. FLASH uses a tabulated equation of state (EOS) to close the system. For the ideal-MHD cases, resistivity is neglected in Eqs. (7) and (8). In all equations, the internal energy $\epsilon$ is calculated separately in FLASH using

$$\frac{\partial \rho \epsilon}{\partial t} + \nabla \cdot [\rho \mathbf{u} \epsilon - \eta \nabla \times \mathbf{B}] = 0.$$

(11)

The resistive-MHD cases present use a Spitzer form of resistivity in the FLASH code given by

$$\eta_e = \frac{m_{ele}}{e^2 n_{ele} \tau_{ele}},$$

(12)

$$\eta_i = \frac{\eta_e}{1.96},$$

(13)

where $m_{ele}$, $e$, $n_{ele}$, and $\tau_{ele}$ are the mass, charge, number density, and collision time of the electrons, respectively. $\eta_e$ and $\eta_i$ are the resistivities perpendicular and parallel to the magnetic field, of which $\eta_i$ is used in the simulations because the Hall parameter is much less than 1. The magnetic Reynolds number is defined as

$$R_m = \frac{UL}{D},$$

(14)

where $U$ is the fluid velocity, $L$ is the perturbation wavelength, and $D$ is the diffusivity. For the resistive-MHD cases, $D$ in Eq. (14) is equal to the diffusivity $\eta_i / \rho \sigma$; however, for the ideal-MHD cases, $D$ is estimated with

$$\eta_{est} = 3.3 \times 10^{-2} \frac{Z_i \ln \Lambda}{\sqrt{\epsilon}}.$$  

(15)

where $\ln \Lambda$ is estimated to be 2 (in FLASH, the minimum value is set to 1), $Z_i$ is the local average ionization, and $T_e$ is the local temperature in eV.

III. CYLINDRICAL CONFIGURATIONS

A. Cylindrical model tuning

The parameters used for the cylindrical simulations, performed by modeling targets in two dimensions in the radial and axial ($r$–$z$) frame of reference, are derived from an experiment performed using the Omega laser facility. In particular, the configuration derived for the verification of FLASH can been seen in Fig. 1. Using a laser drive of 18 kJ over 1 ns, 2D FLASH simulations are verified against experimental data from Omega shots whose configuration can be found in Ref. 23. FLASH calculations of the radial shock location are shown to agree well with experimental data collected over a series of four shots; see Fig. 2. As can be seen from this comparison, FLASH shows very reasonable agreement with the shock trajectories extracted from the available experimental data. This provides confidence in FLASH’s ability to simulate the bulk hydrodynamic motion in an $r$–$z$ geometry that dictates RT instability growth during the deceleration phase.
B. Cylindrical RT instability on Omega

The simulations to address magnetic field effects on cylindrical RT instability are based on a recent design study\(^2\) where the density of the low-density foam is decreased to 0.06 g cm\(^{-3}\). A lower laser drive of 8 kJ is used in this work. A perturbation along the \(z\) direction with \(\lambda = 40 \mu m\) and a sinusoidal amplitude of 5 \(\mu m\) is added to the interior aluminum tracer surface. These simulations are performed using FLASH’s HD, ideal-MHD, and resistive-MHD schemes. The seed background magnetic field for the MHD cases oriented parallel to the perturbation vector are 10, 25, and 50 T. The configuration was deliberately chosen so that the perturbation wavelength would be larger than \(\lambda_c\). The values of \(\lambda_c\) for the three cases presented are 0.03, 0.17, and 0.7 \(\mu m\), corresponding to magnetic fields of 10, 25, and 50 T, respectively. Distinct RT instability growth is noted on the interior of the shell during the deceleration phase of the implosion when modeled using the HD scheme; see Fig. 3.

Figure 4 illustrates this solid-density configuration modeled using the ideal-MHD and resistive-MHD schemes 5.4 ns into the implosion at 10, 25, and 50 T. The ideal-MHD density plots show that the nonlinear evolution modeled in these simulations produces stronger reduction in growth at higher seed magnetic field strengths. The ideal-MHD simulations at 10 T show little difference in morphology when compared with the HD case, while the 25 T case illustrates how the RT bubble morphology is reduced in the ideal-MHD case compared with the HD case. At 50 T, the overall morphology and growth of the RT spikes are more significantly affected by the reduced growth in the ideal-MHD simulation than in the HD simulation. While the ideal-MHD results show progressively clearer and notable reductions in RT spike growth and morphology, in the resistive-MHD simulations, the addition of the diffusive effects of resistivity to Eq. (8) reduces the magnetic field amplification during the implosion. This in turn reduces the effect of the magnetic fields on RT spike growth.

The magnetic fields that are presently achievable and those that are expected to be achievable in the next generation of coil designs have little impact on the RT spike growth when a resistive-MHD model is used. This can clearly be seen in Fig. 5, which shows the measurements over the course of the implosion of the RT spike growth from the top of the RT instability bubble (the peak) to the lowest point between RT spikes (the valley). As such, it predicts that the ideal-MHD regime provides an up to 40 \(\mu m\) measurable reduction in RT spike growth, whereas the HD and resistive-MHD schemes present an RT spike growth difference of the order of only a few micrometers. This suggests that in the case of solid-density shells, with small seed background fields, the HD case would capture the expected RT instability growth and morphology that a resistive-MHD scheme would predict. This is notable, given that in the resistive-MHD cases, the magnetic field amplification is of the order of three times the seeded field in the surrounding plasma for 50, 25, and 10 T seed fields in comparison with 400, 300, and 200 T, respectively, for the ideal-MHD cases corresponding to the same seed fields. Figure 6 reveals significant amplification of the magnetic field in the ideal-MHD and resistive-MHD cases; however, the resistive-MHD amplification is located in the shock front, whereas the ideal-MHD amplification occurs in the region where the RT instability grows behind the shock. Additionally, the resistive-MHD magnetic field only exceeds the

FIG. 3. Density plot of cylindrical Omega-based experimental configuration from HD simulation, predicting deceleration-stage RT instability growth after 5.4 ns.

FIG. 4. RT instability growth during deceleration using cylindrical Omega experimental parameters, modeled using ideal-MHD and resistive-MHD schemes with 10, 25, and 50 T background fields.
ideal-MHD one when peak compression occurs, which is likely due to the peak magnetic field being located in the shock front in the resistive-MHD cases and reaching the central axis of the cylinder earlier in time than in the ideal-MHD cases. As a result of the large magnetic field amplification that is occurring, the field exceeds other magnetic fields, such as the self-generated Biermann battery magnetic field. The lower temperatures and magnetic Reynolds numbers associated with these solid-density cylindrical implosions are responsible for the reduced effect of the magnetic fields on the growth of RT instability.

The ideal-MHD cases produce temperatures in and around the unstable interface of the order of 25 and 16 eV within the RT bubbles and spikes, respectively. These low temperatures correspond to low estimated magnetic Reynolds numbers of $\sim 3$ near the interface. By comparison, the resistive-MHD cases produce comparable plasma temperatures and magnetic Reynolds numbers of $\sim 6$, giving a clear indication that field amplification is insufficient to produce fields strong enough to alter RT evolution in a measurable way. To achieve higher magnetic Reynolds numbers, the laser drive should be increased and the pusher density reduced to increase the temperatures near the unstable interface.

C. Cylindrical RT instability on the NIF

The cylindrical NIF configuration is based on a set of NIF-scaled Omega parameters, which leads to a direct-drive NIF laser energy of 226 kJ. A modification is made to the cylindrical target that switches the solid-density Al marker for a nickel-doped foam, motivated by planar target designs that will be discussed subsequently. The cylindrical target for NIF is illustrated in Fig. 7, where the pusher has been adjusted to be a high-density nickel-doped foam. A perturbation with $\lambda = 120 \mu m$ and a sinusoidal amplitude of 40 $\mu m$ is added to the nickel-doped foam at the interface with the low-density target foam. This configuration is simulated with only a 30 T magnetic field, comparable to those previously achieved on the NIF.

The difference in RT spike size and morphology between the HD and ideal-MHD cases is again notable, as can be seen from Fig. 8. However, unlike in the previously discussed Omega configuration, which uses a solid-density Al marker, Fig. 8 shows that the resistive-MHD model also predicts a difference in the RT bubble compared with the HD model. Differences between the resistive-MHD simulation on the one hand and the HD and ideal-MHD simulations on the other are seen in the RT morphology of the bubble and spike. As can be seen below in Fig. 11, however, the overall spike growth does...
not different significantly between the HD and resistive-MHD cases, until late in time. All three models show the RT spikes developing well behind the shock front, which is the region where the highest temperatures are reached. Consequently, the plasma in and around the RT spikes reaches temperatures of the order of 60 eV.

The magnetic Reynolds numbers, shown in Fig. 9, only reach $\sim 5$ in the bubble and $\sim 10$ in front of the RT spikes. These low magnetic Reynolds numbers are in part due to the temperature and decreasing velocities of the plasma during the deceleration. The low magnetic Reynolds numbers result in low magnetic field amplification. Figure 10 shows the plasma $\beta$ values reaching several thousand at the center of the RT instability bubbles and dropping rapidly to $\sim 50$ at the front of the RT spike growth. At these $\beta$ levels, the system is only beginning to approach the regime where morphological magnetic field effects may be expected.

Despite the RT instability morphology being different in the resistive-MHD case, the resistive-MHD simulations with a 30 T seed magnetic field reveal little reduction in RT spike size, as can be seen in Fig. 11. Specifically, secondary features seen growing at the top of the RT instability bubbles in the HD case are reduced in size, as shown in Fig. 8. The late-time difference in spike size between the HD and resistive-MHD cases from Fig. 11 reaches 50 $\mu$m when, optimistically, the secondary features growing on top of the spikes in the HD case are incorporated; this may be measurable experimentally with axial radiographs. The detailed morphology of these small-scale secondary features would be significantly more difficult to measure in an experiment than a simple reduction in spike size.

Tables I and II provide approximate values for important plasma parameters for all the configurations at locations within the RT spikes where the material is 90% pusher and 90% low-density foam, respectively. Note that for the Omega cylindrical configuration, the temperature, Hall parameter $\chi$, and $R_m$ are substantially smaller than for the NIF cylindrical configuration, whereas the Reynolds number...
Re and Péclet number $Pe_L$ are larger in the Omega cases than in the NIF cases. Additionally, the difference between the pusher-dominant region (Table I) and the low-density foam-dominant region (Table II) of the RT instability lies primarily in the temperature and plasma $\beta$, with small differences between the regions in $R_m$ but substantial differences in $Re$ and $Pe_L$. The planar configurations discussed in Sec. IV achieve notably higher temperatures and $R_m$, while maintaining small Hall parameter values along with large Reynolds and Péclet numbers.

IV. PLANAR CONFIGURATIONS

Given the solid densities used in the Omega cylindrical configuration and the primarily morphological effects of the seed magnetic field in the NIF cylindrical configuration, an effort is made to explore planar foam targets on Omega and NIF-scale powers.

A. Planar RT instability on Omega

Additional configurations are designed to study blast-wave-driven deceleration-stage growth of RT instability, utilizing a laser to drive the implosion of a planar target in which a high-density pusher foam is machined with a sinusoidal perturbation and is driven into a low-density foam, as illustrated in Fig. 12. A seed background magnetic field of 12 T is applied in the ideal-MHD simulation. This target is then directly driven with a 2350 J laser drive for 2 ns, comparable to an Omega-EP experimental drive.

The RT instability growth is prominent during the deceleration stage, as can be seen from the density plots in Fig. 13. Distinct small-scale features are present in the HD cases, but are damped in the ideal-MHD cases, alongside an overall reduction in RT spike size. Additionally, the temperatures observed in these simulations are of the order of 40–45 eV in and around the RT instability, which is twice as hot as in the previously discussed cylindrical Omega-scale target simulations. This increased temperature does result in an estimated magnetic Reynolds number that is higher in both the HD and ideal-MHD cases, as can be seen from Fig. 14; however, it is still only of the order of 5–8, and thus is still too small for the effect of the 12 T seeded background magnetic field to be measurable in a resistive-MHD case. Consequently, shifting again to a NIF-like regime allows high laser drives, which would result in higher temperatures and higher magnetic Reynolds numbers. This then increases the likelihood that a resistive-MHD simulation would lead to an RT spike growth that differs from the growth found in HD simulations.

B. Planar RT instability on the NIF

The planar configuration explored here is based on experimental parameters that are the design point for a direct-drive NIF campaign and consist of a $30 \mu m$ thick CH ablator of density $1.0 \text{ g cm}^{-3}$, a $400 \mu m$ thick CH foam of density $0.215 \text{ g cm}^{-3}$, and a $400 \mu m$ thick nickel-doped foam of density $0.235 \text{ g cm}^{-3}$. The target CH foam has a density of $0.02 \text{ g cm}^{-3}$ and a thickness of $3500 \mu m$. The laser drive of this system is $\sim 260 \text{ kJ}$. These HD, ideal-MHD, and resistive-MHD simulations are performed until a time of 16 ns, with a sinusoidal perturbation with wavelength $\lambda = 120 \mu m$ and amplitude $20 \mu m$. The ideal-MHD and resistive-MHD cases are simulated with a seed background magnetic field of 30 T.
FLASH results for the planar NIF design at 12 ns with a 30 T seed field are shown in Fig. 15. The differences in RT morphology and spike growth between the ideal-MHD and HD cases are clearly seen. The resistive-MHD case also exhibits differences in RT spike growth and morphology compared with the HD and ideal-MHD cases. Additionally, the temperature around the RT spikes is of the order of 80 eV for the HD, ideal-MHD, and resistive-MHD cases, giving an estimated magnetic Reynolds number of 40 in the HD and ideal-MHD cases, compared with an actual magnetic Reynolds number of 47 in the resistive-MHD case, as can be seen from Fig. 16. Such large magnetic Reynolds numbers indicate that the magnetic field amplification is substantial, and the plasma $\beta$ suggests whether these conditions lend themselves to a regime where the RT spikes will be damped. The plasma $\beta$ values achieved can be seen in Fig. 17, where the plasma $\beta$ in the RT spikes is high, but is of the order of 100 in front of the spikes. This suggests that for configurations that achieve similarly high temperatures and velocities, the resistive-MHD scheme best captures the effects that a background magnetic field will have on RT spike growth and morphology.

The differences between the HD, ideal-MHD, and resistive-MHD models can be seen from the peak-to-valley measurements of RT spike growth in Fig. 18. The resistive-MHD spike growth (blue dotted line) and the HD spike growth (black solid line) reveal a 50 $\mu$m difference in RT spike size by 14 ns, and this continues to increase given additional time to grow. Experiments to confirm this measurable difference in RT instability growth are currently under way at NIF, in an effort to validate these simulation predictions.

V. CONCLUSIONS

The primary focus of this work has been on the growth of the RT instability during the deceleration stage of ICF-relevant implosions, particularly the effect, or lack thereof, of a seed magnetic field on this growth. These RT instability configurations have been studied using FLASH, first to solve the Euler equations and then extended to ideal MHD in the presence of seed background magnetic fields of varying magnitudes. Finally, with the addition of the Spitzer resistivity model, FLASH has been used to perform simulations using a more accurate resistive-MHD model. This introduces a diffusive effect into the domain, thereby providing a more realistic representation of what would be observed in an experiment. It is worth noting that although the Spitzer resistivity has been used for the resistive-MHD simulations performed here, further studies might use more accurate resistivity models for the materials and regimes considered here.

Following a comparison of the results from FLASH's HD model with experimental data from the Omega laser, Omega configurations

<table>
<thead>
<tr>
<th>Configuration</th>
<th>$T$ (eV)</th>
<th>$R_m$</th>
<th>$\beta$</th>
<th>$\chi$</th>
<th>$P_{\epsilon L}$</th>
<th>$Re$</th>
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<tr>
<td>Omega cylindrical, resistive-MHD, 25 T</td>
<td>18.7</td>
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<td>2607</td>
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<td>67 035</td>
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<td>0.02</td>
<td>757</td>
<td>86 392</td>
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<td>Omega cylindrical, HD, 0 T</td>
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<td>⋮</td>
<td>⋮</td>
<td>720</td>
<td>71 601</td>
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<td>NIF cylindrical, resistive-MHD, 30 T</td>
<td>53.1</td>
<td>7.5</td>
<td>328</td>
<td>0.06</td>
<td>130</td>
<td>6 350</td>
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<td>NIF cylindrical, ideal-MHD, 30 T</td>
<td>52.9</td>
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<td>38</td>
<td>0.15</td>
<td>107</td>
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<td>⋮</td>
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<td>NIF planar, resistive-MHD, 30 T</td>
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<td>NIF planar, HD, 0 T</td>
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<th>$\beta$</th>
<th>$\chi$</th>
<th>$P_{\epsilon L}$</th>
<th>$Re$</th>
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<tbody>
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<td>Omega cylindrical, resistive-MHD, 25 T</td>
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<td>NIF cylindrical, resistive-MHD, 30 T</td>
<td>56.4</td>
<td>14.7</td>
<td>166</td>
<td>0.09</td>
<td>106</td>
<td>4265</td>
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<tr>
<td>NIF cylindrical, ideal-MHD, 30 T</td>
<td>56.1</td>
<td>12.5</td>
<td>41</td>
<td>0.15</td>
<td>97</td>
<td>3942</td>
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<td>NIF cylindrical, HD, 0 T</td>
<td>59.8</td>
<td>15.7</td>
<td>⋮</td>
<td>⋮</td>
<td>94</td>
<td>3699</td>
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<td>NIF planar, resistive-MHD, 30 T</td>
<td>80.9</td>
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<td>99</td>
<td>0.21</td>
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<td>3995</td>
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<td>NIF planar, ideal-MHD, 30 T</td>
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<td>52</td>
<td>0.39</td>
<td>105</td>
<td>3883</td>
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<td>45.1</td>
<td>⋮</td>
<td>⋮</td>
<td>121</td>
<td>4204</td>
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in both cylindrical and Cartesian coordinate systems have been simulated with a single mode. In both configurations, the HD model predicts significant RT spike growth on the interior interface during deceleration. With the addition of seed background magnetic fields of 10, 25, and 50 T to the cylindrical system, there is a significant reduction in RT spike size in the ideal-MHD cases. However, in the presence of resistivity, there is little observable effect on the RT spikes in comparison with the HD case, regardless of the strength of the initial magnetic field. This is also observed in the foam–foam planar Omega configuration, where low temperatures and subsequent magnetic Reynolds numbers reached during deceleration indicate that there will be no measurable difference in RT spike size between the resistive-MHD and HD cases. Thus, similar configurations of laser power and density would benefit little from the added effort involved in use of the resistive-MHD model when the HD model provides the same results with less computational cost.

On shifting to a NIF configuration, in which a higher laser power, larger targets, and high-density pusher foam configurations are possible, increases are noted in both temperature and magnetic Reynolds number. However, the latter increase is not significant enough in the cylindrical foam–foam configuration to produce a sufficiently large magnetic Reynolds number. Thus, a significant

FIG. 12. Schematic of the general configuration used for directly driven planar targets on Omega. These targets consist of a high-density nickel-doped foam with a sinusoidal perturbation with wavelength $\lambda = 80 \mu m$ and an amplitude of $20 \mu m$ incident on a low-density CH foam.

FIG. 13. Density plots of Omega-scale planar targets. The RT instability growth is shown at 7 ns during deceleration simulated in HD and ideal-MHD schemes with a 12 T background magnetic field.

FIG. 14. Magnetic Reynolds number of the Omega-scale planar target at 7 ns during deceleration in HD and 12 T ideal-MHD simulations. Note the magnetic Reynolds numbers in the 5–8 range for both models.

FIG. 15. Density plots of RT instability growth during deceleration using planar NIF experimental parameters, modeled using HD, ideal-MHD, and resistive MHD schemes, the latter two with 30 T background field, 12 ns into the implosion. There are clear differences in RT spike height and morphology between the different models, with the ideal-MHD model predicting significantly damped RT spike growth.
reduction in RT spike size is not seen in resistive-MHD simulations compared with HD simulation, and only small features in the RT morphology of this cylindrical foam–foam case are damped. The damping of these small secondary features may be experimentally measurable with axial radiographs, although the larger RT spikes are not predicted to show much of a size difference. Owing to the limited space for growth before peak convergence in the cylindrical configuration, the RT instability does not grow sufficiently for the damping of the larger RT spikes to be measurable.

In the planar NIF configurations, the damping effect of a 30 T magnetic field is observable within the RT spikes for both the ideal-MHD and resistive-MHD cases. Temperatures of the order of 80–90 eV are observed and magnetic Reynolds numbers on the scale of 40–50 are seen in and around the RT spikes. As can be seen in Fig. 18, there is a measurable difference of ~50 μm in the RT spikes. For configurations driven with sufficiently increased laser power and reaching temperatures of the order of 80 eV and magnetic Reynolds numbers of ≤40, the use of the resistive-MHD model is essential for accurately simulating the effect of a magnetic field on RT spike growth. Experimental measurements of the effect of background magnetic fields on the growth of the RT instability are currently being pursued. Should these effects be replicated experimentally, the use of magnetic fields in Z pinches and concepts such as MagLIF, as well as the addition of magnetic fields in ICF experiments, could contribute to mitigating the growth of RT instability in these contexts.

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AUTHOR DECLARATIONS

Conflict of Interest

The authors have no conflicts of interest to declare.

DATA AVAILABILITY

The data that support the findings of this study are available from the corresponding author upon reasonable request.
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