

Kinetic study of transverse electron-scale interface instability in relativistic shear flows

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ABSTRACT

Interfacial magnetic field structures induced by transverse electron-scale shear instability (mushroom instability) are found to be strongly associated with electron and ion dynamics, which in turn will influence the development of the instability itself. We find that high-frequency electron oscillations are excited normal to the shear interface. Also, on a larger time scale, the bulk of the ions are gradually separated under the influence of local magnetic fields, eventually reaching an equilibrium related to the initial shear conditions. We present a theoretical model of this behavior. Such separation on the scale of the electron skin depth will prevent different ions from mixing and will thereafter restrain the growth of higher-order instabilities. We also analyze the role of electron thermal motion in the generation of the magnetic field, and we find an increase in the instability growth rate with increasing plasma temperature. These results have potential for providing a more realistic description of relativistic plasma flows.

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I. INTRODUCTION

Plasma shear instabilities play an important role in a wide range of laboratory and astrophysical plasma flows^{1–3} and in inertial confinement fusion.^{4–7} They are closely related to dissipation of plasma kinetic energy into thermal or electromagnetic field energy,^{8–10} and have been shown to be strongly coupled with other hydrodynamic instabilities such as Rayleigh–Taylor instability (RTI) and Richtmyer–Meshkov instability (RMI),¹¹ often followed by transition to turbulence in highly nonlinear regimes.⁴ In astrophysical scenarios such as supernovae and gamma-ray bursts, plasma shear instability has been proposed as a candidate mechanism for strong magnetic field generation along the shear interface,^{12,13} which cannot be clearly explained by magnetohydrodynamic (MHD) simulations.¹⁴ The coupling of such interfacial electromagnetic fields and charged particles could significantly affect the particle velocity distribution,¹⁵ transport processes within or among species,¹⁶ and the development of instability itself.^{17,18}

On the basis of the results of multidimensional particle-in-cell (PIC) simulations, Grismayer *et al.*¹⁹ proposed an electron-scale (i.e., scale size comparable to the electron skin depth), purely kinetic instability [electron-scale Kelvin–Helmholtz instability (ESKHI)], which is capable of generating large-scale dc magnetic field structures in unmagnetized collisionless shear. Subsequent work by Alves *et al.*²⁰ found another electron-scale surface wave, which was unstable in the transverse plane of a shear flow in the relativistic regime and which also contributed to interfacial magnetic field structures with a similar kinetic mechanism. Mushroom-like electron density structures were found to emerge in the nonlinear phase of the instability, and hence the instability was named mushroom instability (MI). However, further investigation regarding the influence of such large-scale magnetic fields on particle dynamics, especially ion dynamics is still lacking. The microscopic magnetic field structures could be

relevant to particle acceleration, radiation emission, and various possible subsequent macroscopic processes.^{3,21,22}

In this paper, via 2D3V (two-dimensional in space, three-dimensional in velocity space) PIC simulations, we investigate plasma dynamics in the plane transverse to the shearing flows for various time-scales and initial parameters. The basic mechanism for the generation of the interfacial magnetic field through electron thermal motion is explored. Multiple simulations are then performed to fully clarify the electron dynamics, i.e., the electron oscillations and the separation of ions caused by the interfacial magnetic field. Saturation and the relevant physical processes are also investigated.

II. SIMULATION SETUP AND BASIC PARAMETERS

For charged-particle shear flows as occur in a plasma, the development and evolution of instabilities differ from those in ordinary fluids owing to the generation of strong self-induced electromagnetic fields, which usually occurs at various interfaces. These field structures dramatically affect the particle velocity distributions, which deviate from the Maxwell–Boltzmann distribution. Therefore, when studying an electron-scale plasma instability like the MI, kinetic simulations provide much more detailed information on particle dynamics than can be obtained from traditional (magneto)hydrodynamic simulations, and they also give a better description of the formation of local field structures.

The 2D3V PIC code ASCENT is applied to simulate the evolution of the fields and their influence on particle dynamics during the development of MI in the plane perpendicular to the initial velocity profile.^{23,24} In the simulation box, the shearing plasmas have a spatial distribution in the x - y plane and are uniform in the z direction. The simulated domain has dimensions $L_x \times L_y = 30 \times 10 (c/\omega_{pe})^2$, where L_x and L_y are the physical side lengths of the simulation box, c is the speed of light, and ω_{pe} is the electron plasma frequency, defined as $\omega_{pe} = \sqrt{4\pi n_e e^2/m_e}$, where n_e is the electron density, and m_e and e are the electron mass and charge, respectively. The initial velocity condition of the plasma shear flows is set as $\mathbf{v}_0 = -0.5c\mathbf{e}_z$ for the $x < L_x/2$ half and as $\mathbf{v}_0 = 0.5c\mathbf{e}_z$ for the $x > L_x/2$ half to create a symmetric shearing configuration. The simulations allocate 49 particles per cell for both electrons and protons, and meshed 100 cells per c/ω_{pe} . The time step of the simulations is set to meet the Courant condition. The initial velocity and density profiles of both ions and electrons in each of the flows are set to be identical to ensure charge and current neutrality. For both particles and fields, periodic boundary conditions are imposed in every direction.

Coulomb collisions are considered negligible in all our simulations. The first type of collisions, caused by particle thermal motion, has $\tau_{ee} \propto T_e^{3/2}$, where τ_{ee} is the electron–electron Coulomb collision time and T_e is the electron temperature for a Maxwellian distribution.²⁵ The parameters that we choose in our simulations indicate that $\tau_{ee}\omega_{pe}$ varies within the range 3×10^1 – 10^4 and that all particles have an identical initial temperature so that the “collisionless” assumption holds. The other type of collisions, caused by the very high relative velocity $v_{rel} \sim 0.8c$ of particles between the two shearing flows, is also neglected, with $\tau_{ee} \propto v_{rel}^3$,²⁵ which means that such collisions are extremely unlikely to occur within the simulation time.

III. EVOLUTION OF THE INTERFACIAL MAGNETIC FIELD

A. Single-mode perturbation growth

In the cold shear scenario, the magnetic field along the shear interface is generated purely by the development of the initial perturbation. We first simulate the evolution of MI with a single unstable mode in a fully ionized electron–proton ($m_i/m_e = 1836$) shear flow. An initial harmonic perturbation $\delta\mathbf{v}_x = \delta v_{x0} \cos(ky) \mathbf{e}_x$ in the electron velocity field, with $\delta v_{x0} = 1.5 \times 10^{-4}c$ and $k = 4\pi/L_y$, is introduced to seed the mode of the instability. To ensure the growth of a single mode, both electron and ion temperatures are initially set to 10^{-4} eV. Therefore, the typical thermal velocity of electrons will be $1.4 \times 10^{-5}c$, which can be considered to have little impact compared with the velocity perturbation.

The formation of the out-of-plane current imbalance and the induced in-plane magnetic fields are presented in Fig. 1(a). The generation of the interfacial magnetic field can be described qualitatively as follows.²⁰ The shearing flows are charge- and current-neutral at the very beginning. The initial velocity perturbation $\delta\mathbf{v}_x$ transports electrons across the shear interface, instantly producing a current imbalance $\delta\mathbf{J}_z$ due to the sharp transition in the shearing velocity field, as is shown in Fig. 1. The current imbalance then induces in-plane magnetic fields ($\delta\mathbf{B}_x, \delta\mathbf{B}_y$) on one side of the interface, which in turn enhances the velocity perturbation $\delta\mathbf{v}_x$ via the Lorentz force $\mathbf{v}_0 \times \delta\mathbf{B}_y$. In the linear stage, the characteristic strength of the interfacial magnetic field structure is estimated as $\mu_0 en_0 v_0 \delta v_x t$.¹⁹ The enhanced velocity perturbation then leads to further electron transport across the velocity shear gradient in a feedback loop process, which acts as the basis for the MI growth in the linear stage.

The MI eventually enters a nonlinear stage when the growing magnetic fields become strong enough to significantly displace the electrons and distort the shear interface.²⁰ Such nonlinear distortion of the shear interface leads to the formation of electron surface current filament structures, which eventually induce a strong magnetic field structure extending around the entire interface, as can be seen in Fig. 1(a).

B. Thermally induced instability growth

Considering a more universal physical picture, we remove the artificial perturbation of the velocity profile and set the initial temperature of the shear flows to 1 eV with a Maxwell–Boltzmann distribution so that the growth and saturation of thermally induced MI can be observed during the simulation time. The electron thermal velocity is slightly larger than the amplitude of the perturbation in the previous simulation. In this case, electron thermal expansion is expected to be the main mechanism responsible for electron transport across the interface and for formation of the current imbalance required to induce the dc magnetic field.

Magnetic field generation through thermal expansion is a similar physical process to the single-mode perturbation growth discussed in Subsection III A, which can be considered as a multimode development of the MI. Note that the direction of the interfacial magnetic field is not relevant to the modes of the perturbation, but depends only on the initial shearing settings, for which the possibility of multiple modes would not suppress the generation of the dc magnetic field from extending along one direction. However, the possibility of multiple modes suppresses the expansion of the mushroom-like structures, and thus limits the width of the interfacial magnetic field structure compared with the single-mode case with proper

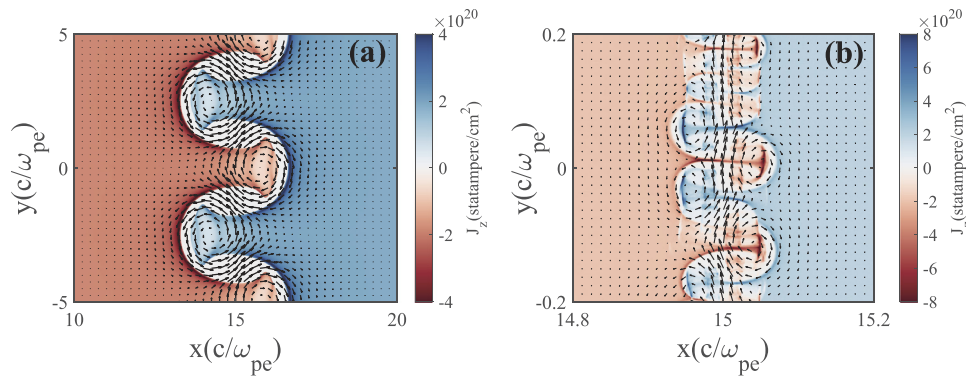


FIG. 1. Out-of-plane electron current density J_z and in-plane self-generated magnetic field (vector plot) at $t = 28 (1/\omega_{pe})$. In (a), a single-mode sinusoidal perturbation is added to the electron velocity field in initially cold shear flows; in (b), the plasma temperature is set to 1 eV, and there are no artificial velocity perturbations. The size of the plot region in (b) is zoomed in to illustrate the finer current structures caused by electron thermal motion.

perturbation wave number k . In this situation, the early electron density protuberances generated from the thermal motion of electrons around the interface expand and start to interact magnetically with their neighborhoods. Small-scale current filaments are formed and subsequently merge into larger finger-like structures. The simulation results shown in Fig. 1(b) reveal excitation of the current filaments on either side of the shear interface and their merger into larger current structures as the instability grows. B_y is the dominant component of the interfacial magnetic field, while the averaged B_x and B_z components contribute little of the total field energy, namely, about 10^{-2} and 10^{-3} , respectively, at the moment presented in Fig. 1(b).

The growth of instability can be illustrated by the temporal evolution of the ratio between energy restored in the self-generated magnetic field and the total energy in the simulation box, as is shown in Fig. 2(a). The energy in the simulation box is strictly conserved, with a deviation less than 10^{-8} . At the very beginning, the system is unmagnetized and current-neutral. The growth of instability is accompanied by an increase in the self-generated magnetic field. The

magnetic field energy (and similarly the electric field energy) subsequently reaches a sufficiently large amplitude and saturates owing to the effect of magnetic trapping,²⁶ which makes it difficult to transport more electrons across the shear to form further current imbalance.³ Figure 2(b) reveals that the growth rate of the MI increases with increasing initial plasma temperature and reaches a turning point where the induced electric and magnetic fields are comparable to the plasma thermal pressure. This conclusion is valid for a temperature range no higher than 3 keV for our simulation configurations. By contrast, in the ultra-hot regime ($T_e > 50$ keV), according to Alves *et al.*,²⁰ who took account of relativistic thermal effects and used an extension of the Jüttner distribution, an increase in the initial plasma temperature will cause a decrease in the MI growth rate. The great difference in parameter space (and thus in particle distribution) could lead to very different conclusions, and the transition between these two types of system is a topic that we are interested in for future study.

In another simulation, if a sinusoidal perturbation (like that in Sec. III A) is introduced into a warm shearing system with

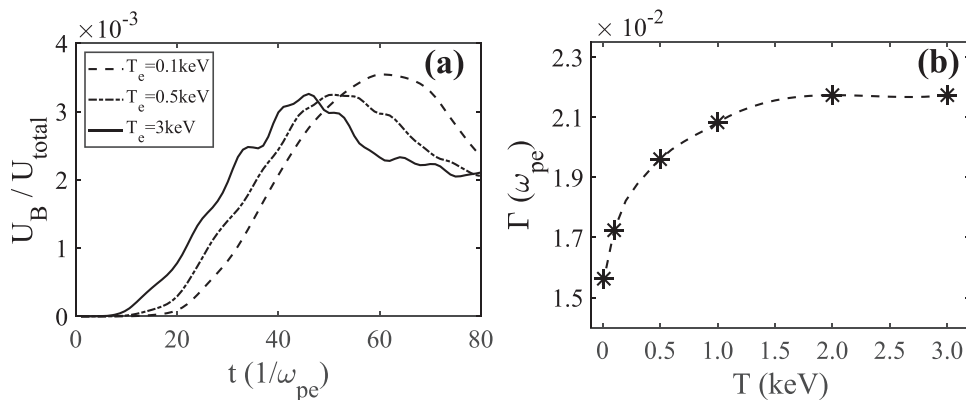


FIG. 2. (a) Temporal evolution of the ratio between magnetic field energy and total energy in the simulation box (U_B/U_{total}) with three different initial plasma temperatures. The MI growth rate increases with increasing initial plasma temperature and undergoes earlier saturation and faster energy drop in low-temperature plasma shear flows. (b) Finite-temperature effect on MI growth rate with several PIC simulation results. A reduced mass ratio $m_i/m_e = 100$ is used in these simulations, but simulations using the authentic mass ratio give similar results.

$T_e = 0.1$ keV, then growth of the seed perturbation will be accelerated owing to the existence of a thermally induced magnetic field that saturates much more rapidly. Interestingly, the mode of the added velocity perturbation will still determine the mode that eventually develops at later times. This coincides with what was found by Miller and Rogers,²⁷ who presented analytical results to show that the growth of MI is not sensitive to particle thermal dynamics in the MHD framework.

IV. INFLUENCE OF THE MAGNETIC FIELD ON PARTICLE DYNAMICS

A. Oscillation of electrons

The thermally induced magnetic field in relativistic shear flows can extend all along the shear interface in our simulations and last long enough to cause a variety of electron and ion behaviors. To shorten the saturation time of the thermally induced magnetic field by a moderate amount and to better investigate the subsequent processes, we increase the initial plasma temperature to 0.1 keV while leaving the other parameters unchanged. The simulation results show that the generation of a strong interfacial field structure will first drive

the electrons to move across the interface, forming a counter-streaming current sheet parallel to the initial interface. On the time scale of the electron response, the protons remain immobile, and thus an electrostatic field is formed by charge separation, as shown in Fig. 3(a). The electrostatic field and the Lorentz force (from the interfacial magnetic field) act as a restoring force on the electrons, which leads to the emergence of upper hybrid (UH) oscillation.²⁵ The dispersion relation for the electron oscillation in this scenario of unmagnetized, collisionless plasmas can be written as

$$\omega^2 = \omega_{ce}^2 + \omega_{pe}^2 + k^2 v_{th}^2, \quad (1)$$

where $\omega_{ce} = eB/m_e c$ is the electron cyclotron frequency in a magnetic field \mathbf{B} , and v_{th} is the typical electron thermal velocity. In our specific simulation setup, it can be estimated that $\omega_{pe} \approx 3.5 \times 10^{14}$ rad/s and $\omega_{ce} \approx 1.0 \times 10^{14}$ rad/s, with a characteristic magnetic field strength of 6×10^6 G, which leads to $\Omega_{UH} = \sqrt{\omega_{pe}^2 + \omega_{ce}^2} \approx 3.7 \times 10^{14}$ rad/s. The sampling rate is then determined to be 2.6×10^{15} Hz based on the Nyquist–Shannon sampling theorem. The results of a frequency analysis of the electron density evolution of our PIC simulation are shown in Fig. 4 and are in general agreement with the theoretical analysis.

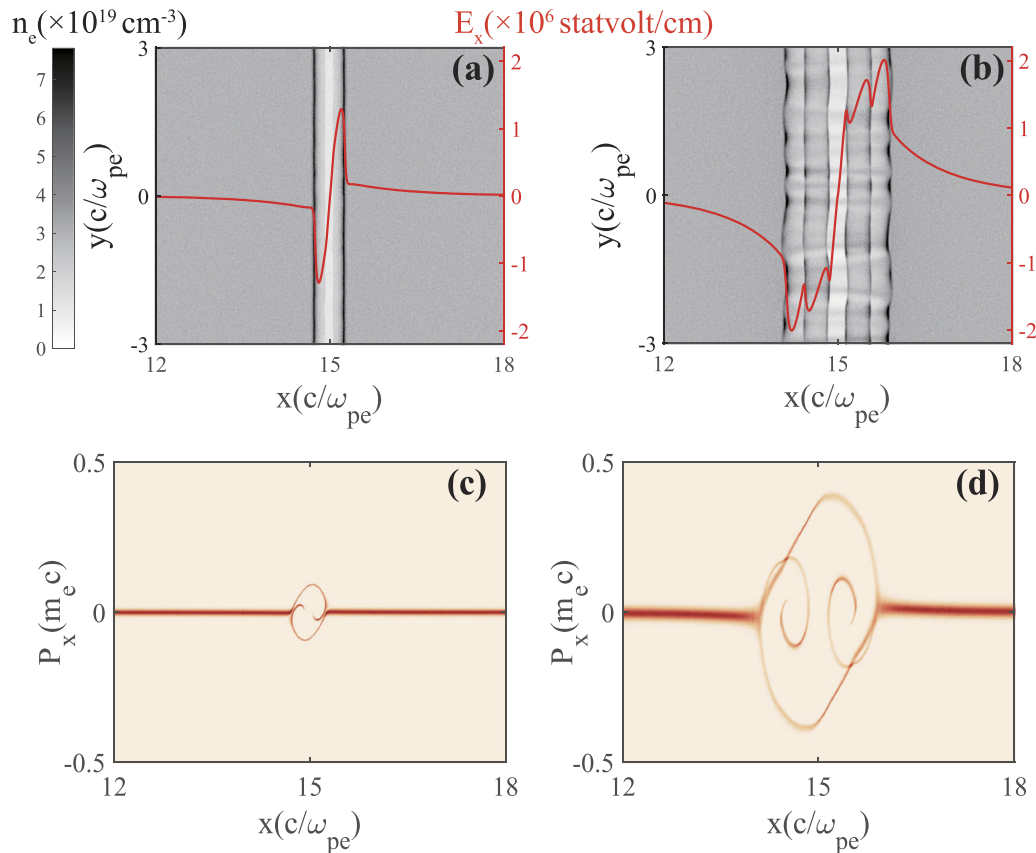


FIG. 3. Evolution of the electron oscillation induced by magnetic–thermal pressure imbalance at the shear interface, with the initial plasma temperature set to 0.1 keV: (a) and (b) electron density and averaged electric field strength E_x (red solid lines) due to charge separation at $t = 12 (1/\omega_{pe})$ and $20 (1/\omega_{pe})$, respectively; (c) and (d) 2D phase-space (x – P_x) distribution plots of electrons at the corresponding times, illustrating the magnetic trapping process.

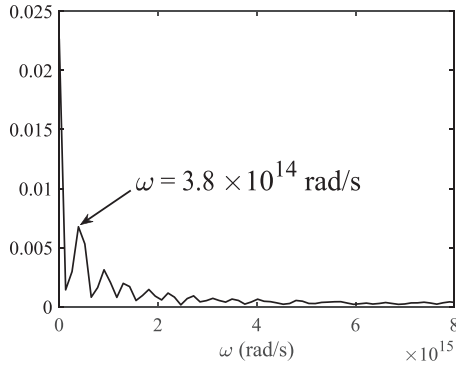


FIG. 4. Frequency spectrum of the oscillating electrons near the shear interface in PIC simulations. The spectrum is obtained by sampling the time variation of the electron density peaks inside the trapping region from $6 (1/\omega_{pe})$ to $20 (1/\omega_{pe})$. The upper hybrid oscillation contributes the largest proportion of electron oscillations.

B. Separation of ions

The characteristic strength of the dc magnetic field along the shear interface in plasmas of 0.1 keV saturated at 1.2×10^7 G will be strong enough to affect proton dynamics within the simulation time, and thus ion mobility can no longer be neglected. Protons on both sides of the initial shear interface will be pushed apart by magnetic pressure, causing pileup of ions on either side of a gap. Note that we define the two borders of the separation gap as being where the averaged ion number density falls to one-half of the initial plasma density. We define the width between these borders as the separation width.

From Fig. 5(a), it can be seen that the separation process lags the development of the interfacial magnetic field in time, which can be explained by the fact that the separation can start to grow only when the interfacial magnetic pressure has become strong enough to overcome the ion thermal pressure. The simulation result shows that although the ions around the shear interface are slightly heated over time, their velocity distribution function deviates little from a drifting-Maxwellian distribution, and thus it is possible to obtain an ion “temperature” by

statistical methods. By the time separation of ions begins to be observable, the effect of the ion thermal pressure gradient is negligible compared with that of the Lorentz force. Figure 6 illustrates two characteristic moments: one at which the magnetic field is dominant and the two shearing flows are expelled owing to magnetic pressure and the growth of the separation width is in the acceleration phase [Fig. 6(a)] and one at which the electric field has a greater impact on the ions, tending to prevent them from separating, and the growth of the separation width is in the deceleration phase [Fig. 6(b)]. Both of these moments and the corresponding separation states can be seen clearly in Fig. 5(a).

The separated ions will form a strong charge separation field and drag the trapped electrons from the region of strongest magnetic field, whereas the magnetic trapping will impede cross-interface transport of the electrons and thus saturate the magnetic field, which indicates that the broadening of the magnetic field structure and the separation of the ions have opposite effects on electron transport normal to the shear interface. The saturation of the interfacial magnetic field will be delayed if the mobility of the ions is taken into consideration.

The evolution of the ion separation process is caused mainly by the general effect of the interfacial magnetic field due to growth of instability, the electric field generated by charge separation, and the gradient in thermal pressure due to density pileup. From an MHD point of view, for one particular ionic fluid element on the boundary surface of the gap, the equation of motion can be written as

$$m_i n_i \frac{dv_i}{dt} = n_i e \left(\mathbf{E} + \frac{\mathbf{v}_i \times \mathbf{B}}{c} \right) - \nabla P_i, \quad (2)$$

$$\nabla \cdot \mathbf{E} = 4\pi e (n_i - n_e), \quad (3)$$

$$\mathbf{B} = B_{\text{sat}} \mathbf{e}_y, \quad (4)$$

where B_{sat} is the saturated central magnetic field strength given by $1.3\beta_0 \sqrt{\gamma_0} (m_e \omega_{pe} c/e)$. Here, we adopt the $\beta_0 \sqrt{\gamma_0}$ scaling given by Grismayer *et al.*,¹⁹ and set the best-fit coefficient to 1.3 for 2D warm MI simulations with an initial shear velocity between $0.3c$ and $0.8c$. It is reasonable to assume that the magnetic field is space- and

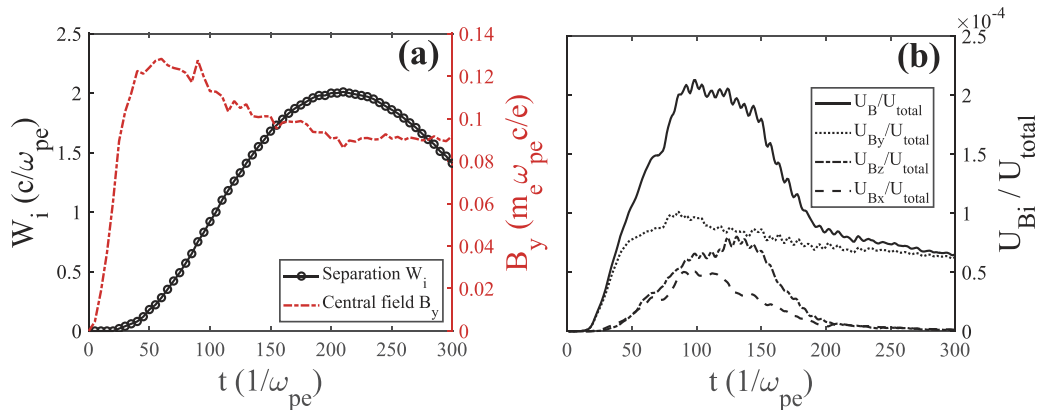


FIG. 5. (a) Temporal evolution of the separation width and the averaged interfacial dc magnetic field strength. (b) Evolution of the ratio U_B/U_{total} between magnetic field energy and total energy in the simulation box and of the corresponding ratios for the three components of the magnetic field. The plasma temperature is set to 0.1 keV and the authentic ion mass ratio $m/m_e = 1836$ is used.

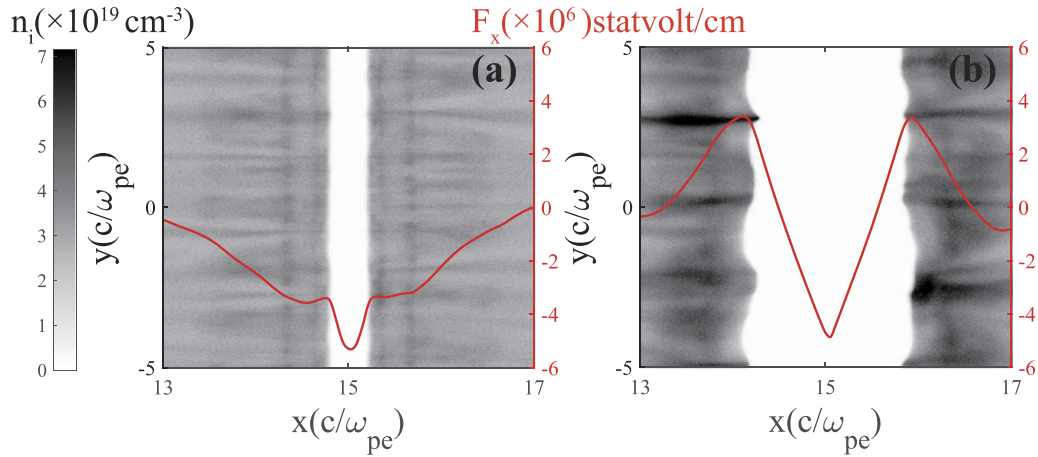


FIG. 6. Ion density evolution ion-electron shear flows at (a) $t = 70(1/\omega_{pe})$ and (b) $t = 150(1/\omega_{pe})$. The red solid line represents the general strength of the electric and magnetic force in x axis $F_x = |E_x| - |v_z B_y/c|$. When the line goes below zero, magnetic field is dominant and the two shearing flows would be expelled apart from the center; when the line goes above zero, electric field has a greater impact on ions, which tends to prevent the ions from separating. For ions on the boundary of the separation gap, magnetic field is dominant in (a) and the separation width growth is in the acceleration phase; while the electric field is in charge in (b) and the separation width growth is in the deceleration phase.

time-independent in the equations above, since the separation happens on a space scale sufficiently small compared with the characteristic width of the dc magnetic field and on a time scale where the dc magnetic field has already reached saturation.

Another important assumption is made to further simplify the situation. The electrons are assumed to be fully trapped by the magnetic field. For a typical field strength of 10^7 G in our 0.5c simulation, $\omega_{ce}/\omega_{pe} = 0.58$ and the electron Larmor radius is two orders of magnitude smaller than the electron inertial length c/ω_{pe} , which is also the characteristic length of the separation width in our simulations. As was shown in Sec. IV A, the high-frequency oscillation of the electrons inside the magnetic field structure means that it is reasonable to neglect the variation in electron density when considering ion-scale separation behavior.

By solving the equation of motion in x from a Lagrangian point of view, we can derive the equation that describes the separation behavior (adiabaticity and a linear density ramp are assumed):

$$\frac{d^2 W}{dt^2} = -\frac{\gamma_i T_i}{m_i} W^{-1} - \frac{3}{4} \omega_{pi}^2 W + u_0 \omega_{ci}, \quad (5)$$

where W is half of the separation width defined previously, $\gamma_i = 3$ is the one-dimensional adiabatic exponent, $\omega_{pi} = \sqrt{4\pi n_0 e^2/m_i}$ is the ion plasma frequency, and $\omega_{ci} = eB_{sat}/m_i c$ is the ion gyration frequency at B_{sat} . This equation is simplified when the ion thermal pressure term can be neglected, which is acceptable when the ion temperature remains below a few keV. Equation (5) can then be solved to give

$$W = \frac{4}{3} \frac{u_0 \omega_{ci}}{\omega_{pi}^2} + [\psi_1 \exp(i\omega_{pi} t) + \psi_2 \exp(-i\omega_{pi} t)], \quad (6)$$

where ψ_1 and ψ_2 are determined by the initial conditions. It can be seen that this solution consists of an equilibrium term and an oscillating term, the former of which is time-independent and can be used to examine the reliability of the model. In fact, it is more convenient to get the equilibrium term by simply setting the left-hand side of Eq. (5) to zero:

$$W_{eq} = \frac{2}{3} \frac{(u_0 \omega_{ci} + \sqrt{u_0^2 \omega_{ci}^2 - 3(\gamma_i T_i/m_i) \omega_{pi}^2})}{\omega_{pi}^2}. \quad (7)$$

This reduces to the first term on the right-hand side of Eq. (6) when the thermal pressure term is sufficiently small. Given the symmetry of the problem, the estimated separation width at equilibrium should be

$$W_{eq} \approx \frac{8}{3} \frac{u_0 \omega_{ci}}{\omega_{pi}^2} = 1.75 \times 10^{13} \beta_0^2 \sqrt{\gamma_0 n_0^{1/2}} \quad (\mu\text{m}) \quad (8)$$

where n_0 is in m^{-3} . The theoretical results at different initial shearing velocities are compared with the 2D PIC results in Fig. 7.

The theoretical results are slightly higher than the 2D PIC simulation ones, the main reason being the existence of a shear gradient layer (instead of the Heaviside function used earlier) between

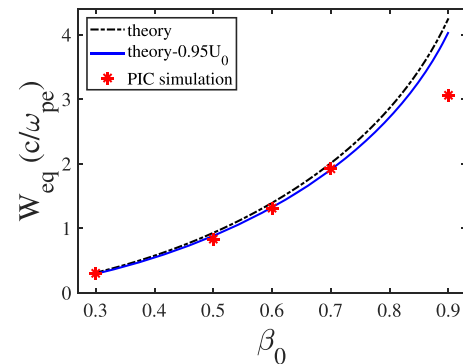


FIG. 7. Comparison between the theoretical separation width at equilibrium W_{eq} and 2D PIC simulation results with different initial shear velocities. The dashed line represents the theoretical model given by Eq. (7) with a shear velocity $u = u_0 = \beta_0 c$; the solid line represents the modified model with a shear velocity $u = 0.95u_0$, which is in better agreement with simulation results. A clear deviation emerges at $\beta_0 = 0.9$.

TABLE I. Comparison of the critical length L_g^{\max} and the equilibrium separation width W_{eq} for different initial shear velocities.

β_0	$L_g^{\max} (c/\omega_{pe})$	$W_{\text{eq}} (c/\omega_{pe})$	L_g^{\max}/W_{eq}
0.3	0.20	0.29	0.69
0.5	0.72	0.88	0.81
0.7	2.27	1.91	1.19

the two bulk plasmas on the ion time scale, which means the actual shear velocity of a fluid element is smaller than that in the initial situation. The formation of this shear gradient layer could be a combined effect of grad- B drift, $E \times B$ drift, and the noncontact frictional force due to electromagnetic instabilities.^{25,28} Based on the simulation results, we can expect to obtain better agreement by altering the shear velocity to $0.95u_0$, as can be seen in Fig. 7. The model breaks down in highly relativistic situations ($\beta_0 > 0.8$ in our initial configurations), where the theoretical prediction of the magnetic field strength we adopted no longer matches. The lower limit ($\sim 0.2c$) of the model is determined by competition between ESKHI and MI,¹⁹ since the latter is dominant only in relativistic regimes.

Alves *et al.*²⁰ have simulated the situation where the shearing flows are initially separated by a nanometer-scale vacuum gap and the situation with a smooth shear gradient of a certain length. In both situations, they have found that the growth rate of MI decreases with the gap/gradient length and that there is a critical length (in the vacuum gap situation) beyond which the growth of MI is largely restrained. Ion separation would have the same effect on the development of subsequent instabilities as in the density-gradient case. The critical gap length given in their theory is estimated as $L_g^{\max} \approx 2(\gamma_0^2 - 1)\sqrt{v_0}(c/\omega_{pe})$, which is comparable to the equilibrium separation width W_{eq} as can be seen in Table I.

V. SUMMARY

2D3V PIC simulations have been performed at different time scales to investigate the evolution of the self-generated interfacial magnetic field of the MI and its impact on electron and ion dynamics. It has been found that the instability can be triggered by electron thermal motion and that its growth rate increases with rising initial plasma temperature, reaching a peak at an initial temperature of around 3 keV when the thermal pressure force is able to counteract the electric and magnetic forces that drive the unstable arrangement of the electron currents. In the case of a warm shearing configuration, the presence of the strong interfacial magnetic field will cause upper hybrid oscillation normal to the shear interface, as well as separation of ions on a longer time scale. A theoretical prediction of the equilibrium separation width has been presented and evaluated, and it has been found to match well with simulation results for initial shear velocities ranging from $0.2c$ to $0.8c$. Scaling of the growth of such electron-scale instability and particle dynamics in experimental situations remains unexplored, and the coupling with other macroscopic (magneto)hydrodynamic instabilities is also a topic that we shall be investigating in the future.

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