Fuel-ion diffusion in shock-driven inertial confinement fusion implosions

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ABSTRACT

The impact of fuel-ion diffusion in inertial confinement fusion implosions is assessed using nuclear reaction yield ratios and reaction histories. In T^{3} He-gas-filled (with trace D) shock-driven implosions, the observed TT/T^{3} He yield ratio is ~2× lower than expected from temperature scaling. In D³He-gas-filled (with trace T) shock-driven implosions, the timing of the D³He reaction history is ~50 ps earlier than those of the DT reaction histories, and average-ion hydrodynamic simulations cannot reconcile this timing difference. Both experimental observations are consistent with reduced T ions in the burn region as predicted by multi-ion diffusion theory and particle-in-cell simulations.

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I. INTRODUCTION

In inertial confinement fusion (ICF),¹ a spherical target filled with fusion fuel is compressed to reach fusion temperature and density. Conventionally, ICF implosion simulations and modeling rely heavily on average-ion hydrodynamic codes. Understanding the roles of ion kinetics and diffusion has become more important since the start of the National Ignition Campaign² in 2009, as highlighted by recent theoretical,^{3,4} simulation,^{5–7} and experimental^{8–12} studies. However, most experimental work has focused on time-integrated measurements, which average over the implosion burn duration and obscure these important effects.

In a hot-spot ignition design, strong shocks are launched into the gas, and the convergence and rebound of these shocks are thought to set up the initial conditions for hot spot formation. These shocks distribute energy to particles proportional to their masses, creating a temperature disequilibrium between the ions and electrons. Because the electrons are more mobile than the ions, they stream ahead and preheat the upstream material. This separation between ions and electrons also creates strong electric fields across the shock front, in addition to the sharp pressure and density gradients. These self-generated electric fields have been observed in ICF implosions,^{1,3} as well as in planar shock-tube^{1,4} experiments. Recent ICF implosion experiments suggest that kinetic and multi-ion-fluid effects can impact performance in ways not captured by standard hydrodynamic codes such as DUED.¹⁵ These experimentally observed effects include reduced yield,⁸ temperature difference between ion species,⁹ unexpected yield scaling,¹² ion diffusion,¹⁰ and ion species separation.¹¹ To address these experimental results, hydrodynamic codes with reduced ion kinetic models⁵ and kinetic-ion codes¹⁶ have been used to better capture these multi-ion and kinetic physics in ICF implosions.

In this paper, the impact of ion diffusion in T^3 He-gas-filled (with trace D) shock-driven implosions and D³He-gas-filled (with trace T) shock-driven implosions is discussed. Section II will outline the experiment and observables. Section III will interpret these data in the context of multi-ion diffusion theory, average-ion hydrodynamic simulations, and particle-in-cell (PIC) simulations. Section IV will discuss future directions and potential implications of these findings.

II. SHOCK-DRIVEN IMPLOSION EXPERIMENTS

The OMEGA experiments in this work use shock-driven implosions¹⁷ as an experimental platform to probe kinetic and multi-ion effects during shock propagation and rebound in ICF implosions. A shock-driven implosion is one where the bulk of fusion reactions occur from shock heating of the fuel. These simple implosions have been invaluable for studying ICF implosion dynamics because they are low-convergence, 1D in nature, and insensitive to drive asymmetry and hydrodynamic mix.¹⁰ The two sets of implosions described in this work are T³He-gas-filled (with trace D) shock-driven implosions and D³He-gas-filled (with trace T) shock-driven implosions. The spherical targets have an outer diameter of 860 μ m with a ~2.3- μ m-thick SiO₂ shell. All 60 laser beams¹⁸ (351 nm, ~14 kJ total, 0.6 ns square pulse shape) are used to illuminate the target. 2D smoothing by spectral dispersion, polarization smoothing, and phase plates are used to improve laser uniformity.

These implosions are hydrodynamiclike, with Knudsen number $N_K \sim 0.3$, estimated here as the ratio of the burn-averaged ion mean free path λ_{ii} and the fuel radius R_{burn} at peak nuclear burn. For the D³He-gas-filled (with trace T) implosions, the primary observables are the D³He-p and the DT-n. For the T³He-gas-filled (with trace D) implosions, the primary observables are the T³He-d and the TT-n. The relevant DT, D³He, TT, and T³He nuclear reactions are

$$D + T \rightarrow \alpha (3.5 \text{ MeV}) + \mathbf{n} (\mathbf{14.1 MeV}), \tag{1}$$

$$D+^{3}He \rightarrow \alpha(3.6 \text{ MeV}) + \mathbf{p(14.7 MeV)}, \qquad (2)$$

$$T + T \rightarrow \alpha (\leq 6.6 \text{ MeV}) + 2n (\leq 10.6 \text{ MeV}), \qquad (3)$$

$$T+^{3}He \rightarrow \alpha (4.8 \text{ MeV}) + d(9.5 \text{ MeV}) (BR \sim 43\%).$$
 (4)

Strong shock heating can potentially cause differences between the ion density profiles (ion diffusion) and/or between the ion temperature profiles (ion thermal decoupling). For example, the T and ³He ion temperatures are expected to be higher than the D ion temperature immediately post shock because of their higher masses. To isolate the mechanism and impact of ion diffusion as far as is reasonably possible, these experiments focus on relatively high gas fill density implosions (>2 mg/cm³), corresponding to a short ion-ion thermalization time (~30 ps) during the shock burn as compared with the burn duration (~100 ps). The second key step taken to reduce the impact of different ion temperatures is to consider reaction pairs where the reactants have the same masses, since collisional shock heating is expected to partition energy to ions according to their masses. For D³He-gas-filled (with trace T) implosions, the reaction pairs DT and D³He are considered. For T³He-gas-filled (with trace D) implosions, the reaction pairs TT and T³He are considered. As an example, for two Maxwellian ion populations with two different ion temperatures, the effective fusion temperatures T_{fusion} (for DT and $D^{3}He$) are given by

$$T_{\rm fusion,D^{3}He} = \frac{m_{\rm D}T_{\rm i,^{3}He} + m_{^{3}He}T_{\rm i,D}}{m_{\rm D} + m_{^{3}He}},$$
(5)

$$T_{\rm fusion,DT} = \frac{m_{\rm D}T_{\rm i,T} + m_{\rm T}T_{\rm i,D}}{m_{\rm D} + m_{\rm T}}.$$
 (6)

As Eqs. (5) and (6) show, the higher temperatures of ³He and T (resulting from their higher masses) affect the D^{3} He and DT fusion temperatures in the same way. In general, the fusion reaction yield integrated over the implosion duration for reactants 1 and 2 is given by

$$Y_{12} = \int \frac{f_1 f_2}{1 + \delta_{12}} n_i^2 \langle \sigma v \rangle_{12} \ dV \, dt,$$
(7)

where *f* is the ion species fraction of reactants 1 and 2, n_i is the ion number density, $\langle \sigma v \rangle$ is the Maxwellian-averaged fusion reactivity, and δ_{12} is the Kronecker delta function. The fusion yield ratio can be approximated as

$$\frac{Y_{11}}{Y_{12}} \approx \frac{1}{2} \frac{f_1}{f_2} \frac{\langle \sigma \nu \rangle_{11}}{\langle \sigma \nu \rangle_{12}}.$$
(8)

A summary of the main experimental observables is provided in Table I. A suite of optical, nuclear, and X-ray diagnostics are used to diagnose these implosions. For the main experimental observables, the D³He-p and T³He-d yields are measured by wedge-range-filter spectrometers¹⁹ and charged-particle spectrometers.²⁰ The DT-n yield, the DT temperature, and the TT-n yield are measured by neutron time-of-flight detectors.²¹ The nuclear peak emission time (bang time) is measured by the neutron temporal diagnostic.²²

In Table I, the observed TT/T^{3} He and DT/D^{3} He yield ratios have been corrected for the branching ratio in the T^{3} He reaction, and for the fact that two neutrons are produced per TT reaction. The expected TT/T^{3} He and DT/D^{3} He yield ratios are calculated using the fuel fraction and fusion reactivity [Eq. (8)]. The reactivity ratio is a strong function of the ion temperature, and the corresponding expected yield ratio is different for each shot because different ion temperatures are measured on each shot.

Experimentally, the observed yield differences between shots are most likely to have been caused by differences in target shell thickness. For example, shot 86 208 has the thickest shell, latest bang time, highest T^{3} He-d yield, and lowest observed TT/T^{3} He yield ratio. Laser parameters (total energy and pulse shape) are repeatable to within 3% and are not expected to cause this level of difference. Hydrodynamic simulations also confirm that shell thickness rather than shell diameter has the most direct impact on implosion observables. For both the TT/T^{3} He and DT/D^{3} He reaction pairs, the observed yield ratios are lower than the expected yield ratios based on temperature scaling, and interpretations of this observation will be discussed in Sec. III.

In the D³He-gas-filled (with trace T) implosions, DT and D³He reaction histories are also simultaneously measured with high relative precision (± 10 ps) using the particle X-ray temporal diagnostic (PXTD),²³ as shown in Fig. 1. The timing of the D³He reaction history is ~50 ps earlier than that of the DT reaction history, and this timing differential is much larger than that predicted by average-ion DUED hydrodynamic simulations (~10 ps). As will be discussed in Sec. III, both the observed yield ratios and reaction histories are consistent with the D and ³He ions ahead of the shock front relative to the T ions during shock propagation.

III. DATA INTEPRETATION

Ion species separation in a multicomponent plasma is driven by sharp pressure and temperature gradients at the shock front and depends on both local plasma conditions (pressure and temperature) and differences in charge and mass between the different ion species.⁴ This is a hydrodynamic treatment of multi-ion-species diffusion, which is strictly valid only when the ion-ion mean free path is small compared with the gradient scale lengths. However, as long as the

TABLE I. Summary of primary experimental observables. The uncertainty in the absolute bang time is \pm 50 ps. The uncertainties in the TT-n, T³He-d, DT-n, and D³He-p yields are \pm 10%, \pm 20%, \pm 5%, and \pm 20%, respectively. The uncertainty in the DT T_i is \pm 0.5 keV.

T ³ He-gas-filled (with trace D) implosions												
Shot	Outer diameter (µm)	SiO ₂ thickness (µm)	ρ (mg/cm ³)	Fraction D	Fraction ³ He	Fraction T	Bang time (ps)	TT-n yield	T ³ He-d yield	DT T _i (keV)	TT/T ³ He (observed)	TT/T ³ He (expected)
86 193	854	2.3	2.8	0.004	0.50	0.49	780	$5.3 imes10^{10}$	$1.4 imes 10^9$	11.7	8.0	20.0
86 194	853	2.4	2.8	0.004	0.50	0.50	781	$8.2 imes 10^{10}$	$1.4 imes 10^{9}$	11.4	11.8	15.5
86 195	856	2.2	2.9	0.004	0.51	0.49	766	$7.1 imes 10^{10}$	$1.4 imes 10^{9}$	11.3	10.7	22.0
86 208	863	2.5	3.0	0.004	0.53	0.46	837	$6.5 imes 10^{10}$	2.1×10^{9}	10.5	6.5	20.0
				D	³ He-gas-fi	lled (with	trace T) im	plosions				
	Outer	SiO ₂										
	diameter	thickness	ρ	Fraction	Fraction	Fraction	Bang		D ³ He-p	DT T_i	DT/D ³ He	DT/D ³ He
Shot	(µm)	(µm)	(mg/cm^3)	D	³ He	Т	time (ps)	DT-n yield	yield	(keV)	(observed)	(expected)
82 614	889	2.7	2.0	0.50	0.49	0.007	841	$2.0 imes 10^{11}$	$5.0 imes 10^{10}$	11.6	4.0	5.0
82 615	855	2.7	2.0	0.50	0.50	0.007	831	$1.9 imes 10^{11}$	$5.0 imes 10^{10}$	10.5	3.8	6.2

plasma is not very kinetic, this treatment does produce qualitatively correct behaviors.

In particular, two diffusion mechanisms play important roles in the interactions between D, ³He, and T ions at the shock front, and these mechanisms are driven by the differences in the ion charges and masses. The first mechanism is baro-diffusion, relating to the ion pressure gradient.³ Baro-diffusion accelerates lighter ions ahead of heavier ions, and will accelerate D ions ahead of T ions. The second mechanism is electro-diffusion, related to the electric potential gradient (the electric field).⁴ Electro-diffusion accelerates ions with a higher charge-to-mass ratio ahead of ions with a lower charge-tomass ratio, and will accelerate ³He ions ahead of T ions. In both scenarios, the T ions are behind the D ions and ³He ions as the shock propagates inward.

This qualitative picture provided by multi-ion diffusion theory is supported by kinetic-ion PIC LSP¹⁶ simulations, which, in contrast to average-ion hydrodynamic codes, do treat the different ion species separately. In the LSP simulation, the fuel ion species are treated kinetically, while the electrons are treated as a fluid with a flux limiter of 0.06. The choice of flux limiter has been shown to minimally impact LSP results. The simulation uses a 1D spherical geometry with reflecting boundary conditions, with 2000 cells covering a radial distance of 1000 μ m (excluding the origin to avoid numerical



FIG. 1. D^{3} He (red) and DT (black) reaction histories measured on the PXTD in D^{3} He-gas-filled (with trace T) implosions.

stability). The simulation is initialized with 5000 particles per ion species per cell. More information on the PIC simulation setup and collision operators is given in Ref. 7.

Figure 2 illustrates shock propagation in a kinetic-ion LSP simulation that treats the ion populations separately. This simulation is for a D³He-gas-filled (with trace T) implosion. In Fig. 2, as the shock is propagating inward at t = 0.63 ns, the D and ³He ions are racing ahead. The T ions are notably lagging behind the shock front. This ion species separation at t = 0.63 ns during shock convergence developed in a triton depletion in the burn region during shock rebound at t = 0.73 ns (when the shock yields are being produced). As expected from the low convergence, mixing of the SiO₂ ions into the fuel plasma is negligible in the LSP simulation.



FIG. 2. Density profiles from an LSP simulation of a D^{3} He-gas-filled (with trace T) implosion at t = 0.63 ns and t = 0.73 ns, during shock convergence and shock rebound, respectively. The ion density profiles for D, T, and ³He are in blue, gold, and red, respectively.



FIG. 3. (a) DUED-simulated and (b) LSP-simulated $D^{3}He$ (red) and DT (black) reaction histories for a $D^{3}He$ (with trace T) shock-driven implosion.

These differences between the ion density profiles in the kinetic simulation and those in an average-ion-fluid simulation in turn translate to differences in the timing of the simulated reaction histories, which are shown in Fig. 3. In the DUED simulations, the D^3 He and DT bang times (the times of peak thermonuclear production) are nearly simultaneous (within 10 ps), which is very different from the measured timing difference and well outside the measurement uncertainty. In contrast, the simulated peak timing difference between the D^3 He and DT reaction histories in the kinetic-ion LSP simulation (~50 ps) is in much closer agreement with measurements.

In simulations, the absolute timing and amplitude of the reaction histories (relative to the start of the laser pulse) are strongly affected by many factors (laser energy, absorption, equations of state, flux limiter, etc.). However, the relative timing between the reaction histories is a much more robust and insensitive quantity in the simulation. In the kinetic-ion simulation, the absolute nuclear yield is quite a bit lower than measured, because the laser drive is truncated when the kineticion calculations begin. This has been shown to not affect the relative timing of the simulated reaction histories.

IV. DISCUSSION AND CONCLUSION

The impact of ion diffusion during the shock phase of ICF implosions has been investigated using both time-integrated and time-resolved nuclear observables. The lower-than-expected TT/T^{3} He yield ratios (in T^{3} He-gas-filled implosions with trace D) and lower-than-expected DT/D^{3} He yield ratios (in D^{3} He-gas-filled implosions with trace T) are consistent with tritium depletion in the burn region during shock rebound. At the same time, the observed earlier D^{3} He reaction history timing relative to that of DT measured using the PXTD and comparison with kinetic-ion simulations provide additional indications that this tritium depletion is related to fuel-ion-species separation that developed during shock propagation into the fuel.

These experimental observations provide new insights into kinetic and multi-ion physics not modeled in average-ion hydrodynamic codes. The experiments here focused on the shock phase of ICF implosions. Using both time-integrated and time-resolved nuclear observables, future experiments will explore these kinetic and multi-ion physics as implosion plasma conditions become increasingly more collisional. Future work will also begin probing how these kinetic and multi-ion effects that developed during the shock phase propagate into and affect hot spot formation during the later compression phase.

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