

# Wavelength-switchable vortex beams based on a polarization-dependent microknot resonator

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We experimentally demonstrated a method of generating continuously wavelength-switchable optical vortex beams (OVBs) in an all-fiber laser. A polarization-dependent microknot resonator (MKR) functions as comb filter and accounts for the narrow linewidth (0.018 nm) of multiwavelength channels. The wavelength interval corresponds to the free spectral range of the MKR. We exploit a fused SMF-FMF (single mode fiber-few mode fiber) mode coupler to obtain broadband mode conversion and successfully achieve multiwavelength switchable OVBs. As far as we know, this is the first report about identical multiwavelength vortex beams with topological charges of  $\pm 1$ . It has been verified that each channel of the vortex beams preserves the same orbital angular momentum (OAM) properties through their clear spiral interferograms. Multiwavelength vortex beams with identical OAM properties are desirable for multiplexing, exchanging, and routing to further improve the capacity of optical fiber transmission. ©2018 Chinese Laser Press

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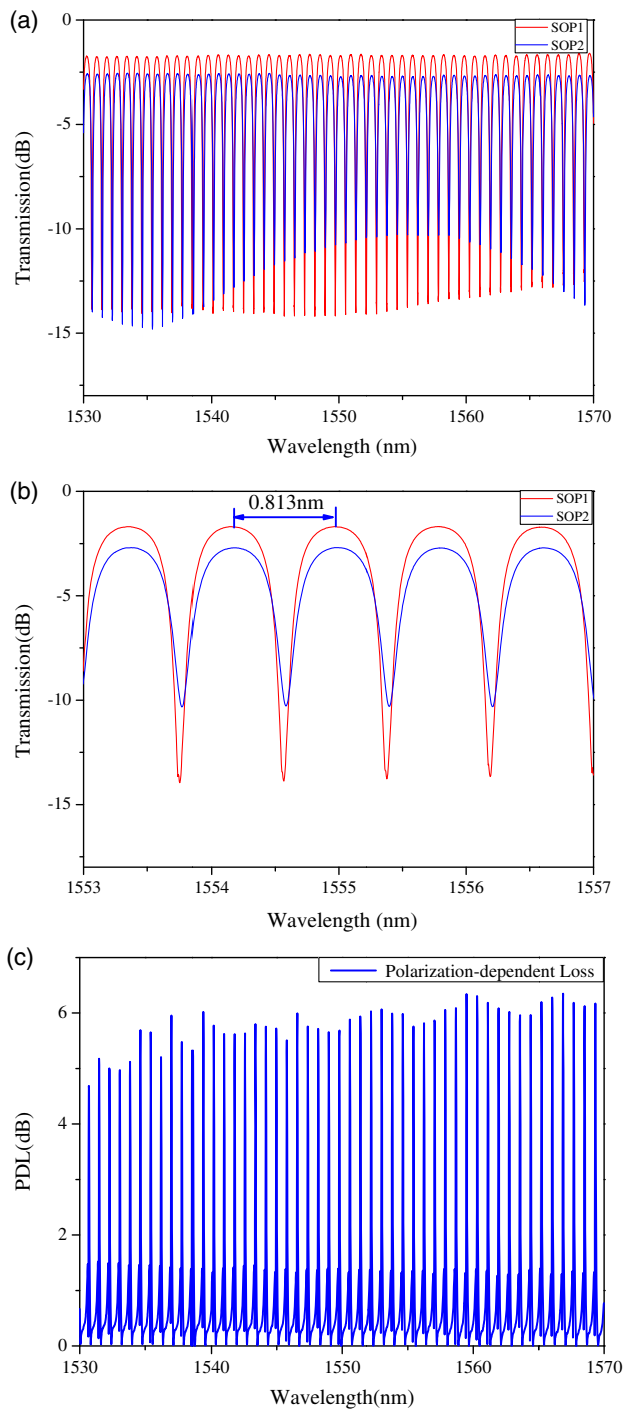
## 1. INTRODUCTION

Optical vortex beams (OVBs) are spatially structured beams with a helical phase front. Such beams are characterized by a topological charge (order), also called orbital angular momentum (OAM) beams. Vortex beams have a phase singularity at the center with a doughnut-shaped spatial intensity. Due to their polarization and amplitude symmetry, OVBs attract a lot of attention and have been investigated in many areas, such as high-resolution measurement [1], particle trapping [2], material processing [3], remote sensing [4], microscopy [5], and quantum information technology [6]. OAM recently has been used in applications in multidimensional multiplexing technologies in optical communications, such as wavelength-division multiplexing (WDM), mode-division multiplexing (MDM) [7], and all-optical processes [8]. A traditional method is used to convert a Gaussian beam to a vortex beam using phase elements, such as a  $q$ -plate [9], or computer-generated holograms created by a programmed spatial light modulator (SLM) [10]. Such phase elements are typically designed for a specific laser wavelength and this inherently constrains the wavelength versatility of the vortex laser sources. Optical vortex modes could be directly generated from a laser cavity by certain methods, such as the use of an annular pump beam for the laser

medium [11] and using an SLM as a cavity reflector [12]. Different kinds of vortex lasers based on fiber mode conversion devices have been proposed, such as few-mode fiber Bragg gratings (FBGs) [13–15]. Recently, nonlinear frequency conversion based on optical parametric oscillation [16], optical parametric amplification [17], or stimulated Raman scattering [18,19] is proven to be a valid approach to generate optical vortices in the new waveband. Single-pass optical parametric generation of a Yb-fiber laser was demonstrated to generate optical vortices in the mid-infrared region [20]. However, most of them have two disadvantages: high cost and low integration.

Multiwavelength switchable fiber lasers have the advantages of wavelength flexibility and high coherence. They have been considered excellent sources for optical WDM and sensing systems. Many methods have been proposed to obtain multiwavelength fiber lasers, such as using a Lyot-Sagnac filter [21], a Mach-Zehnder interferometer (MZI) [22], and a superimposed chirped fiber Bragg grating (CFBG) [23]. Zhan *et al.* reported a triple-wavelength switchable lasing laser with equal wavelength spacing of 2.6 nm by using cascaded long-period fiber grating (LPG) [24]. Luo *et al.* reported a wavelength-switchable femtosecond pulse fiber laser using a gold-nanorod saturable absorber (SA) [25].





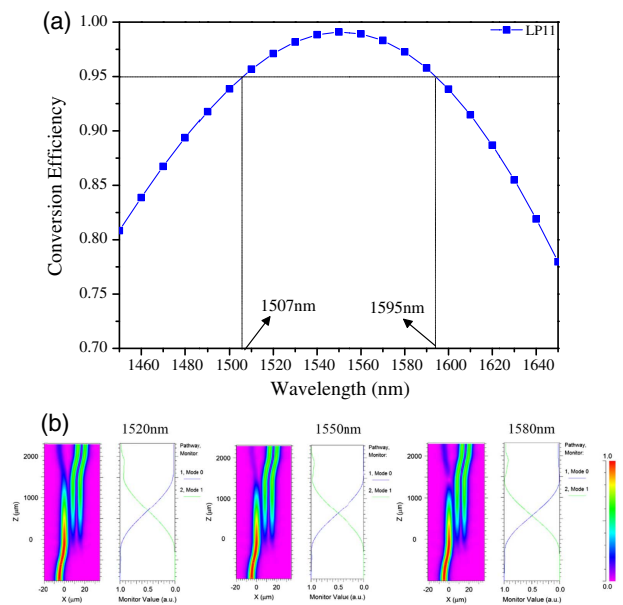
**Fig. 3.** Spectral response of MKR: (a) Transmission spectrum with different incident states of polarization (SOP); (b) transmission spectra from 1553 nm to 1557 nm; and (c) polarization-dependent loss of the MKR.

combining different vector modes  $HE_{2,1}^{\text{even}}$  ( $HE_{2,1}^{\text{odd}}$ ) and  $TE_{0,1}$  ( $TM_{0,1}$ ) when  $l = 1$ , or combining  $HE_{l+1,m}^{\text{even}}$  ( $HE_{l+1,m}^{\text{odd}}$ ) and  $EH_{l-1,m}^{\text{even}}$  ( $EH_{l-1,m}^{\text{odd}}$ ) when  $l > 1$  with a  $\pi/2$  phase shift, where  $l$  refers to the azimuthal index and  $m$  refers to the radial index [32]. Then a  $\pi/2$  phase shift between two vector modes is an indispensable part of generating OAM OVBS. A polarization

controller (PC4) is used to achieve a  $\pi/2$  phase shift between vector modes.

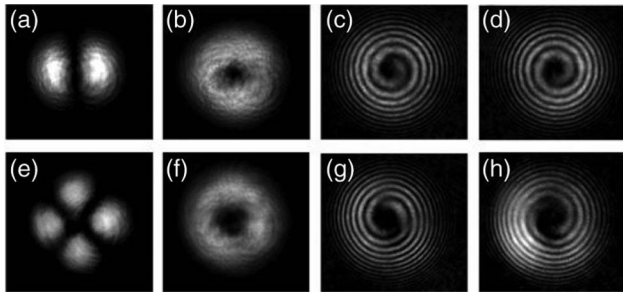
The commercial simulation software (Rsoft) is used to solve the modes propagating in the SMF–FMF couplers. The simulation results are shown in Fig. 4. SMF and FMF core diameters are set to 5.60  $\mu\text{m}$  and 10.90  $\mu\text{m}$ , respectively. The corresponding mode effective indices are 1.444. The coupling region length is set to 2300  $\mu\text{m}$ , and the core distance between the two fibers is set to 5  $\mu\text{m}$ . The conversion efficiency is the ratio of  $LP_{01}$  mode in SMF coupled to  $LP_{11}$  mode in FMF as a function of the wavelengths, as shown in Fig. 4(a). The coupling efficiency is more than 95% from 1507 nm to 1595 nm. Figure 4(b) shows the power exchange in the coupling region when  $LP_{01}$  mode from the SMF converts to  $LP_{11}$  mode in the FMF at the wavelengths of 1520, 1550, and 1580 nm, respectively.

Before the fusing process of the SMF–FMF fiber coupler, SMF (core/cladding diameter = 8/125  $\mu\text{m}$ ) is pre-tapered to the cladding diameter of around 85  $\mu\text{m}$ , while the core/cladding diameter of FMF fiber is 20/125  $\mu\text{m}$ . Then the pre-tapered SMF and FMF are twisted, stretched, and fused together using an oxyhydrogen flame so that their fiber core diameters are near to the phase-matching condition. Optimum taper diameters are determined after experimental fine tuning of pre-tapered SMF diameters [26]. The powers from the output SMF port and FMF port are carefully monitored. The coupling ratio (CR) is expressed by the ratio between the out power in FMF ( $P_2$ ) and the total output power of SMF ( $P_1$ ) and FMF ( $P_2$ ):  $CR = P_2/(P_1 + P_2)$ . When the desired coupling ratio is achieved, the automated fusing and pulling process is stopped. The change of the power coupling is observed during the fiber pulling and fusing process, and a different splitting ratio can be obtained by controlling the pulling length.



**Fig. 4.** Simulation results: (a) Coupling efficiency as a function of the wavelengths; and (b) power exchange in the coupling region when  $LP_{01}$  mode in SMF converts to  $LP_{11}$  mode in FMF.





**Fig. 5.** Output near-field intensity distribution from a mode selective coupler by inputting a femtosecond pulse. (a), (e) Intensity profiles of the  $LP_{11}$  and  $LP_{21}$  modes; (b), (f) donut-shaped OAM mode patterns when pressing the output FMF; (c) and (d), and (g) and (h) corresponding clockwise and anticlockwise spiral interferograms of  $OAM_{\pm 1}$  and  $OAM_{\pm 2}$ , respectively.

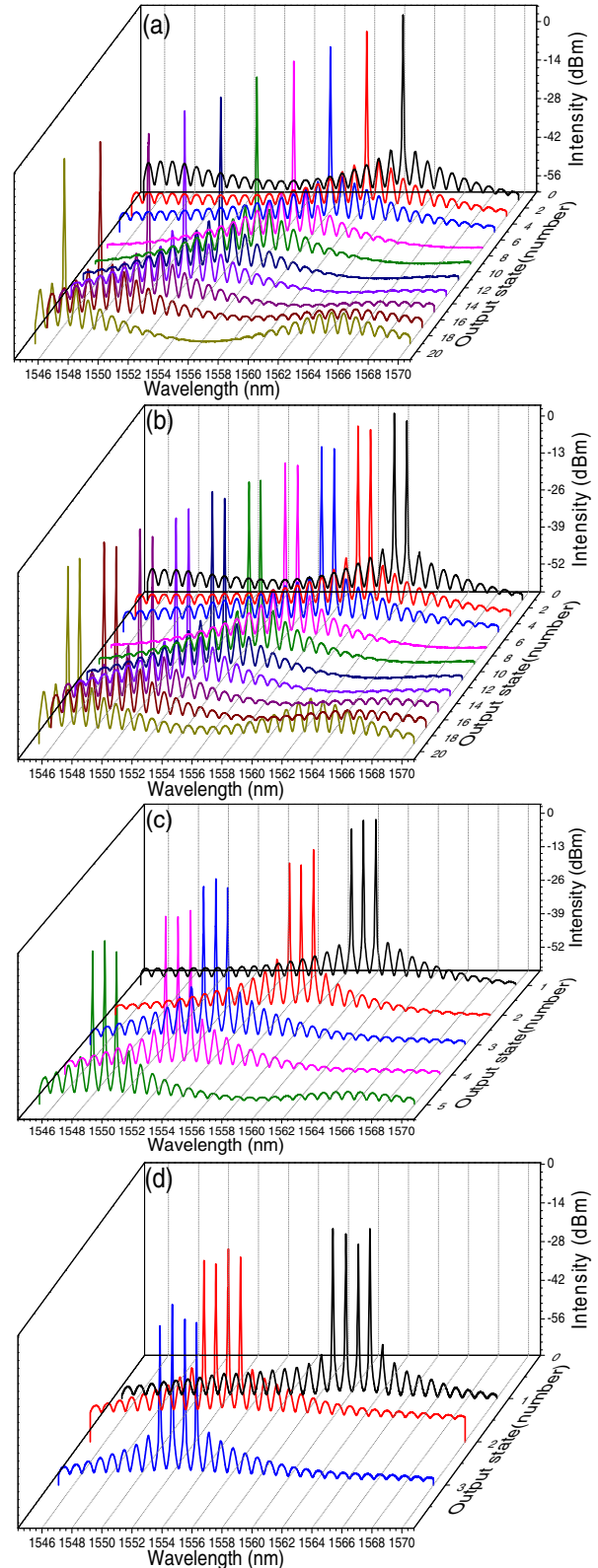
Fiber  $OAM_{\pm 1}$  modes can be obtained by combining vector modes  $HE_{2,1}^{even}$  ( $HE_{2,1}^{odd}$ ) and  $TE_{0,1}$  ( $TM_{0,1}$ ) with a  $\pi/2$  phase shift [32]. By rotating the PC4 on the output of FMF and adjusting the pressure appropriately, a  $\pi/2$  phase shift between vector modes can be achieved. The mode selective coupler with a broad bandwidth is further verified by inputting a femtosecond pulse with a spectrum bandwidth of 32 nm (centered at 1550 nm) and its pulse duration is around 150 fs. Femtosecond optical vortex beams are obtained from the FMF output port of the mode selective coupler, as shown in Fig. 5. The output high-order mode patterns and the corresponding interference patterns of  $OAM_{\pm 1}$ ,  $OAM_{\pm 2}$  modes are clearly seen, respectively, which indicate that the mode selective coupler can work as an efficient mode converter within a large bandwidth.

### 3. RESULTS AND DISCUSSION

The mechanism of wavelength-switchable fiber laser is easy to explain. The MKR comb filter exhibits a polarization-dependent transmission loss for different wavelengths, which leads to unequal cavity losses at the lasing wavelength channels. Due to the existence of mode competition in erbium-doped fiber, a small change of cavity loss can lead to the different lasing wavelengths. By adjusting the state of polarization of the PCs to change the transmission loss of the MKR cavity, it leads to unequal cavity losses at the lasing wavelength channels. The wavelength-switching operation can be obtained for different wavelengths. To extend the tuning range, a broadband HiBi-SLM filter is used. It is known that its reflective spectrum is a periodic sinusoidal curve, and the reflective bandwidth is inversely proportional to the PMF length. In fact, only the gain at the wavelengths near the center of the reflective profile of the HiBi-SLM filter can offset the cavity loss to generate the lasing. The PMF length is about 15 cm and its reflective bandwidth is about 30 nm. Moreover, the effective gain region can be tuned along with the reflective profile [33], which is first tuned by adjusting the PC1 and PC2 to the desired lasing band. Then the SOP of the MKR is adjusted to switch the lasing wavelengths continuously by using PC3.

Multiwavelength switchable lasing based on the MKR is demonstrated experimentally, as shown in Fig. 6. By adjusting

the PCs appropriately, adjacent single- and dual-wavelength outputs are successively tuned out in the lasing channels. The signal-to-noise ratio (SNR) of each channel keeps as higher

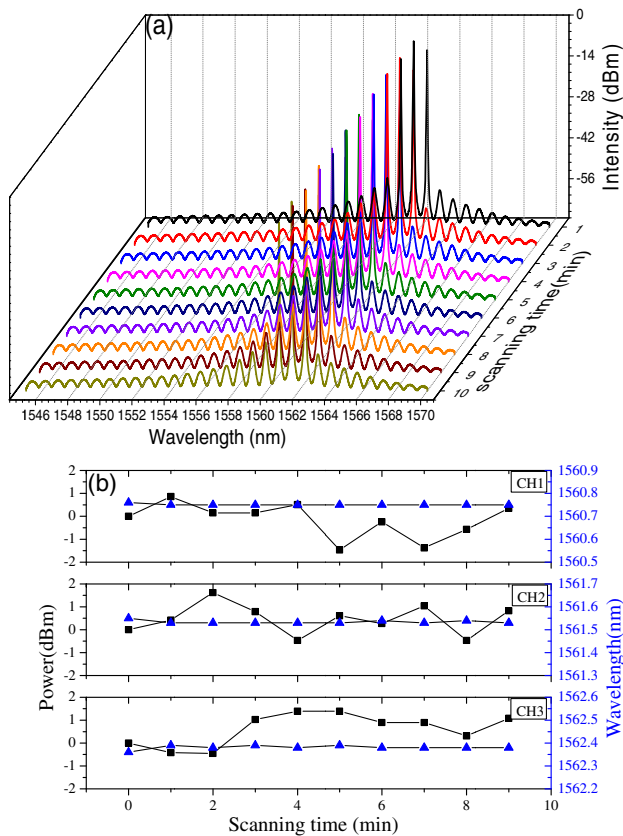


**Fig. 6.** Output spectra of successively tunable (a) single-, (b) dual-, (c) triple-, and (d) quadruple-wavelength lasing operations.

than 40 dB, which is mainly attributed to the high contrast of the comb spectrum of the MKR (Fig. 3). Moreover, the measured 3 dB linewidth of each channel reaches approximately 0.018 nm, limited by the measurement of OSA precision. Single-longitudinal-mode oscillation can be realized based on a fiber Fabry–Perot interferometer and the MKR in the state of single-wavelength lasing [34]. The wavelength interval is 0.813 nm, which is in agreement with the FSR of the MKR. As shown in Fig. 6(a), the single wavelength can be tuned from 1546.95 nm to 1562.29 nm, and continuous 19 wavelengths in total are generated. Then multiwavelength operation is achieved based on these wavelengths. The output spectra of more multiwavelength lasing are observed. As shown in Figs. 6(b)–6(d), stable adjacent dual-, triple- and quadruple-wavelength channels can also be tuned continuously through controlling the polarization state of light inside the HiBi-SLM filter, the MKR, and the fiber ring cavity.

The proposed multiwavelength switchable fiber laser exhibits some advantages. First, multiwavelength channels can be flexibly tuned with different number combinations of lasing channels, which cover versatile single-, dual-, triple-, and quadruple-wavelength lasing. Second, it is a compact and simple configuration of a polarization-dependent MKR and a HiBi-SLM filter, which offers comb filtering and polarization switching.

We also investigate the generation stability of multiwavelength lasing channels. The output triple-wavelength spectra

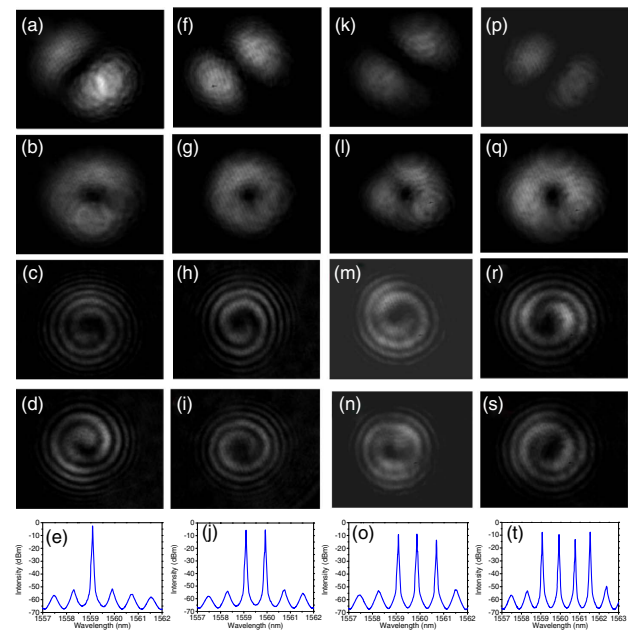


**Fig. 7.** Stability of triple-wavelength output spectrum. (a) Repeat scans of triple-wavelength output spectrum every minute. (b) Power fluctuation (black) and central wavelength (blue) of each channel in the triple-wavelength output every minute.

are repeatedly scanned every minute, as shown in Fig. 7(a). The output power can be increased by reducing the whole cavity loss or increasing the power of pump or even double pump configuration. Here, the output power of the vortex beams is about 2 mW. The fluctuation of output power is less than 2.5 dBm, and central wavelengths of different channels remain within 0.03 nm in 10 min, which show the stability of the output laser, as shown in Fig. 7(b).

We further exploit the polarization characteristics of multi-wavelength switchable outputs through a fused SMF–FMF coupler inserted in the cavity. The mode patterns from the FMF output of the broadband mode coupler are observed when the fiber laser is running at the state of switchable wavelengths. The fused SMF–FMF coupler has been verified effectively when acting as a mode selective converter. A polarizer is added before the CCD camera; by rotating the polarization direction, linearly polarized vortex beams are observed.

We show in Fig. 8 that four columns present the experimental near-field intensity patterns of the  $LP_{11}$  mode and the corresponding  $OAM_{\pm 1}$  of a single wavelength (1559.09 nm), dual wavelengths (1559.09 nm and 1559.90 nm), triple wavelengths (1559.09, 1559.90, and 1560.71 nm), and quadruple wavelengths (1559.09, 1559.90, 1560.71, and 1561.52 nm), respectively. Figures 8(a) and 8(b) are the experimental near-field patterns of  $LP_{11}$  mode and the donut-shaped mode pattern when adjusting the PC4 on the FMF output. Figures 8(c) and 8(d) are the corresponding clockwise and anticlockwise spiral interferograms. Figure 8(e) is the output spectrum of the single-wavelength lasing operation. Other columns present



**Fig. 8.** Near-field distribution of  $LP_{11}$  intensities, OAM patterns, spiral interferograms, and the out spectra of wavelength-switchable laser. Four columns present (a)–(e) single-, (f)–(j) dual-, (k)–(o) triple-, and (p)–(t) quadruple-wavelength lasing operations. First row,  $LP_{11}$  intensity profiles; second row, donut-shaped mode patterns of vortex beams; third and fourth rows, corresponding clockwise and anticlockwise spiral interferograms; and fifth row, the output spectra.

the experimental results of dual-, triple- and quadruple-wavelength lasing operations. The purities of the modes are estimated to be more than 95% using the tight bend approach [35].

The clockwise and counterclockwise spiral interference patterns indicate the vortex beams with  $OAM_{-1}$  and  $OAM_{+1}$ .  $LP_{11}$  and OAM mode intensities are preserved identically between the multiwavelength channels and keep the same polarization properties, which are due to the polarization switching of the MKR and HiBi-SLM filter. The near-field  $LP_{11}$  mode intensity patterns, the vortex patterns, and their corresponding spiral interferograms of adjacent single, dual, triple, and quad wavelengths are clearly observed without any distortion. It is concluded that each wavelength channel carries identical properties of  $OAM_{+1}$  or  $OAM_{-1}$ .

We successfully obtain multiwavelength vortex beams with identical OAM properties, which are desirable for multiplexing, exchanging, and routing to further improve the capacity of optical fiber transmission. The multiwavelength switchable lasing shows a potential application in mode-division multiplexing, OAM modes switching, and routing.

#### 4. CONCLUSION

In conclusion, we experimentally demonstrate a method to generate multiple-wavelength switchable OVBs in an all-fiber laser based on a polarization-dependent MKR. The tuning wavelengths range from 1546 nm to 1562 nm, and single-, dual-, triple-, and quadruple-wavelength channels can be switched. The wavelength interval is 0.813 nm, which is in agreement with the FSR of the MKR. Variable wavelength intervals can be acquired by just changing the diameter of the MKR. We use a fused SMF-FMF mode coupler to successfully obtain broadband mode conversion and achieve multiwavelength switchable OVBs. It also verifies that each wavelength channel preserves identical OAM properties through their clear spiral interferograms. The proposed wavelength-switchable and widely tunable OAM fiber laser may be useful in various fields, such as mode-division multiplexing, optical fiber communication, and material processing.

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