# A novel single－polarization single－mode photonic crystal fiber with circular and elliptical air－holes arrays＊ 

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#### Abstract

A novel single－polarization single－mode photonic crystal fiber（SPSM－PCF）with circular and elliptical air－holes is proposed．The characteristics of the proposed SPSM－PCF are investigated by using a full－vector finite element method （FEM）with perfect matched layer（PML）boundary conditions．The results show that the SPSM operation is achieved with wider band，and the total dispersion profile of the SPSM－PCF is dispersion－flattened from $1.193 \mu \mathrm{~m}$ to $1.384 \mu \mathrm{~m}$ ． This dispersion property makes the proposed SPSM－PCF useful for various applications，such as optical transmission and dispersion compensation for conventional fiber at long wavelength band with 500 nm negative dispersion region． It indicates that this is a good solution to realize broadband SPSM operation．


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Since the first photonic crystal fiber（PCF）was demon－ strated by Russell ${ }^{[1]}$ ，PCFs with design flexibility and incomparable advantages have been attracting much at－ tention and are extensively investigated ${ }^{[1-3]}$ ．PCFs can achieve single－polarization single－mode（SPSM）operat－ ion by designing proper PCF structure．The SPSM－PCFs can be applied in high power fiber lasers，sensing and optical communication systems，because it can eliminate both polarization mode coupling and polarization mode dispersion．Some groups have studied PCFs for SPSM operation ${ }^{[4-11]}$ ．The PCFs perform the SPSM operation with bandwidth of 55 nm in the 1550 nm band $^{[4]}, 220 \mathrm{~nm}$ in the 727 nm band $^{[5]}, 84.7 \mathrm{~nm}$ and 103.5 nm in the 1300 nm and 1550 nm band ${ }^{[6]}, 460 \mathrm{~nm}^{[7]}, 560 \mathrm{~nm}^{[8]}, 250 \mathrm{~nm}^{[9]}$ ， $120 \mathrm{~nm}^{[10]}$ ，and $600 \mathrm{~nm}^{[11]}$ ，respectively．In this paper，we propose a novel SPSM－PCF with circular and elliptical air－holes in order to achieve dispersion－flattened profile， wider bandwidth and negative dispersion for SPSM op－ eration．The characteristics of proposed SPSM－PCF are investigated by using the full－vector finite element method （FEM）with perfect matched layer（PML）boundary condi－ tions．

Fig． 1 shows the cross－section of the proposed SPSM－ PCF．The inner cladding of proposed PSM－PCF is square
lattice of circular air－holes，and the outer layer is com－ posed of three－rings hexagonal lattice of elliptical air－holes．The proposed PCF can perform SPSM opera－ tion because of the three－rings hexagonal lattice of ellip－ tical air－holes．The low dispersion is induced by the square lattice of circular air－holes．


Fig． 1 Cross－section of the proposed SPSM－PCF
The gray area denotes pure silica，the elliptical and circular areas represent air holes，and the rectangular

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areas at the edges represent PML boundary. The diameter of circular air holes is $a=0.45 \mu \mathrm{~m}$, and the spacing between the circular air holes is $\Lambda_{1}=1.00 \mu \mathrm{~m}$. The diameters of the elliptical air holes along the $x$-axis and $y$-axis are denoted as $a$ and $b$, respectively. The spacing between the elliptical air holes is $\Lambda_{2}=1.80 \mu \mathrm{~m}$, and the elliptical ratio is $\eta=b / a=2$, where $a=0.45 \mu \mathrm{~m}$, and $b=2 a$ $=0.90 \mu \mathrm{~m}$. The refractive indices of the silica regions and the air holes are 1.45 and 1 , respectively. The mode field characteristics can be modified by the shape and the spatial distribution of these air holes.

The Helmholtz equation can be obtained from Maxwell equations ${ }^{[10,11]}$

$$
\begin{equation*}
\nabla \times\left(\left[\mu_{\mathrm{r}}\right]^{-1} \nabla \times \boldsymbol{E}\right)-k_{0}^{2}\left[\varepsilon_{\mathrm{r}}\right] \boldsymbol{E}=0, \tag{1}
\end{equation*}
$$

where $k_{0}=2 \pi / \lambda$ is the free-space wave number, $\lambda$ is the wavelength of input light, $\boldsymbol{E}=E(x, y)^{\mathrm{j} \beta z}$ denotes the electric field, $\beta$ is propagation coefficient, $\left[\varepsilon_{\mathrm{r}}\right]$ and [ $\mu_{\mathrm{r}}$ ] are the relative dielectric permittivity and magnetic permeability tensors, respectively. According to the full-vector FEM, we can obtain complex effective index $n_{\text {eff }}$ from the eigenvalue equation of Eq.(1). The model birefringence $B$ of the proposed SPSM fiber is given by the difference between the effective indices of two orthogonal polarization modes ${ }^{[11-13]}$, and the beat length of model birefringence is defined by $L_{B}=\lambda / B$.

The confinement loss of the SPSM-PCF is defined by ${ }^{[11-14]}$

$$
\begin{equation*}
\alpha_{\mathrm{dB}}=1000 \times 40 \pi \times \operatorname{Im}\left(n_{\mathrm{eff}}\right) /(\operatorname{In}(10) \cdot \lambda) \quad(\mathrm{dB} / \mathrm{km}), \tag{2}
\end{equation*}
$$

where $\operatorname{Im}\left(n_{\text {eff }}\right)$ is the imaginary part of the effective index $n_{\text {eff. }}$ The dispersion, which is an important parameter of the fiber, includes the material dispersion and waveguide dispersion. The material dispersion can be obtained from the Sellmeier equation ${ }^{[11-15]}$

$$
\begin{equation*}
n^{2}=1+\sum_{j=1}^{m} \frac{B_{j} \cdot \lambda^{2}}{\lambda^{2}-\lambda_{j}^{2}} \tag{3}
\end{equation*}
$$

and group-velocity dispersion parameter equation ${ }^{[11-15]}$

$$
\begin{equation*}
D=-\frac{\lambda}{c} \cdot \frac{\mathrm{~d}^{2} n}{\mathrm{~d} \lambda^{2}} \tag{4}
\end{equation*}
$$

where $n$ is the refractive index of the medium, $\lambda$ is the input optical wavelength, $m=3, B_{1}=0.6961663, B_{2}=0.4079426$, $B_{3}=0.8974794, \lambda_{1}=0.0684043 \mu \mathrm{~m}, \lambda_{2}=0.1162414 \mu \mathrm{~m}, \lambda_{3}=$ $9.8961610 \mu \mathrm{~m}$, and $\lambda_{j}=2 \pi c / \omega_{j}$, where $\omega_{j}$ is the medium resonance radian frequency, and $c$ is the speed of light in vacuum. The group-velocity dispersion parameter $D$ is useful in practice. The waveguide dispersion is obtained from Eq.(4) and the variation of the real part of effective index $n_{\text {eff }}$ with the wavelength. The complex effective index and modal field distribution can be obtained from solving Eq.(1) by using the full-vector FEM. The confinement loss and dispersion can be obtained from Eq.(3) and (4), respectively.

We firstly calculate the confinement losses of a PCF with three-ring arrays of circular air holes by our full-vector FEM with PML boundary conditions. The calculation is well consistent with that of Ref.[16].

The electric field distributions of $x$-polarized and $y$ -

Optoelectron. Lett. Vol. 9 No. 2 • 0121 • polarized fundamental modes of the proposed SPSMPCF at the wavelength of $1.550 \mu \mathrm{~m}$ are shown in Fig.2. The horizontal arrow denotes $x$-polarized mode, and vertical one shows $y$-polarized mode. It can be obtained from Fig. 2 that the mode fields of $x$ - and $y$-polarized modes are basically symmetrical about $x$ - and $y$-axes. The electric field of $y$-polarized mode is more obviously extended to the cladding region than that of $x$-polarized one. The y-polarized confinement loss is much larger than that of $x$-polarized mode.


Fig. 2 Electric field distributions of (a) $x$-polarized and (b) $y$-polarized modes of the proposed SPSM-PCF at the wavelength of $1.550 \mu \mathrm{~m}$

The modal birefringence is $1.458 \times 10^{-2}$, and the beat length is 0.106 mm at the wavelength of $1.550 \mu \mathrm{~m}$. The confinement losses of $x$ - and $y$-polarized modes are $3.100 \times 10^{-4} \mathrm{~dB} / \mathrm{km}$ and $1.721 \mathrm{~dB} / \mathrm{km}$, respectively. It is assumed that the transmission span is 80 km , and transmitter power is 0 dBm according to general optical communication systems. After propagation over 80 km of the proposed SPSM-PCF, the powers of $x$ - and $y$-polarized modes are reduced to $-2.480 \times 10^{-3} \mathrm{dBm}$ and $-1.377 \times 10^{2} \mathrm{dBm}$, respectively. The experimental noise of a good detector (e.g. optical spectrum analyser AQ6319) is about -60 dBm . It shows that $y$-polarized mode is suppressed, and $x$-polarized mode can be detected and amplified in the systems. Thus, the SPSM operation is achieved by using the proposed PCF. The SPSM-PCF can be extensively applied in the field devices. The numerical aperture of the $x$-polarized mode is 0.447 , the effective mode area is $3.066 ~ \mu \mathrm{~m}^{2}$, and the nonlinear coefficient is $34.373 \mathrm{~W}^{-1} \cdot \mathrm{~km}^{-1}$ at the wavelength of 1.550
$\mu \mathrm{m}$.
Fig. 3 shows the effective index and the modal birefringence varying with input wavelength. It is obtained from Fig. 3 that the effective indices of $x$ - and $y$-polarized modes are increased with the decrease of the wavelength. The effective index of $x$-polarized mode increases from 1.284 to 1.413 with the decrease of the wavelength. The effective index of $y$-polarized mode decreases from 1.409 to 1.256 with the increase of the wavelength. The effective index of $y$-polarized mode is smaller than that of $x$-polarized mode for a given input wavelength. The modal birefringence of the proposed SPSM-PCF is almost linearly increased with the increase of the wavelength.


Fig. 3 Variations of (a) effective indices and (b) modal birefringence with input wavelength

Variations of confinement loss and confinement loss difference between $y$-polarized mode and $x$-polarized one with input wavelength are shown in Fig.4. The confinement losses of $x$ - and $y$-polarized fundamental modes are almost exponentially increased with the increase of the input wavelength. The confinement loss of $x$-polarized mode is increased from $3.854 \times 10^{-7} \mathrm{~dB} / \mathrm{km}$ to $1.757 \times 10^{4}$ $\mathrm{dB} / \mathrm{km}$ with the increase of the input wavelength. That of $y$-polarized one is increased from $8.951 \times 10^{-7} \mathrm{~dB} / \mathrm{km}$ to $1.806 \times 10^{7} \mathrm{~dB} / \mathrm{km}$. The confinement loss of $y$-polarized mode is much larger than that of $x$-polarized mode for a given input wavelength. The confinement loss difference between the $y$-polarized fundamental mode and the $x$-polarized one is rapidly increased approximately ex-
ponentially from $1.100 \mu \mathrm{~m}$ to $2.000 \mu \mathrm{~m}$. The confinement loss difference is increased from $5.097 \times 10^{-7} \mathrm{~dB} / \mathrm{km}$ at the wavelength of $1.100 \mu \mathrm{~m}$ to $1.804 \times 10^{7} \mathrm{~dB} / \mathrm{km}$ at the wavelength of $2.500 \mu \mathrm{~m}$. It shows that the confinement loss is increased with the increase of input wavelength. The diffraction effect of air holes is enhanced with the increase of input wavelength, while the effect of air holes for blocking the light into the cladding is weakened. According to the discussion on SPSM operation above, the PCF can perform SPSM operation with input wavelength from $1.550 \mu \mathrm{~m}$ to $2.500 \mu \mathrm{~m}$.


Fig. 4 Variations of (a) confinement loss and (b) the difference with input wavelength

Variations of the dispersion with input wavelength are illustrated in Fig.5. The dispersion flattened characteristic of optical communication systems is a hot spot. The material dispersion is gradually increased with the increase of wavelength. The waveguide dispersion is decreased with the increase of wavelength from $1.100 \mu \mathrm{~m}$ to $2.500 \mu \mathrm{~m}$. It results in that the total dispersion profile is convex and dispersion-flattened from $1.193 \mu \mathrm{~m}$ to $1.384 \mu \mathrm{~m}$. The dispersion parameters of the proposed PCF are $83.482 \mathrm{ps} /(\mathrm{km} \cdot \mathrm{nm})$ at the wavelength of 1.193 $\mu \mathrm{m}$ and $83.480 \mathrm{ps} /(\mathrm{km} \cdot \mathrm{nm})$ at the wavelength of 1.384 $\mu \mathrm{m}$, and the maximum dispersion parameter is 85.477 $\mathrm{ps} /(\mathrm{km} \cdot \mathrm{nm})$ at the wavelength of $1.286 \mu \mathrm{~m}$. The dispersion flatness of the proposed SPSM-PCF, which means subtracting minimum parameter from the maximum parameter in the range of the wavelength, is $2.039 \mathrm{ps} /$ $(\mathrm{km} \cdot \mathrm{nm})$. It is much better than the flatness $9.000 \mathrm{ps} /$
( $\mathrm{km} \cdot \mathrm{nm}$ ) from $0.830 \mu \mathrm{~m}$ to $1.020 \mu \mathrm{~m}^{[17]}$, and is slightly less than the flatness $1.800 \mathrm{ps} /(\mathrm{km} \cdot \mathrm{nm})$ from $1.480 \mu \mathrm{~m}$ to $1.620 \mu \mathrm{~m}^{[18]}$. The dispersion flattened region of the proposed SPSM-PCF is 191 nm , which is almost equal to the width of 190 nm in Ref.[17], and wider than the bandwidth of 140 nm in Ref.[18] and the width of 100 nm in Ref.[19]. This dispersion property makes the proposed SPSM-PCF useful for various applications. The total dispersion value is negative from $2.015 \mu \mathrm{~m}$ to 2.500 $\mu \mathrm{m}$. The dispersion is $-125.142 \mathrm{ps} /(\mathrm{km} \cdot \mathrm{nm})$ at the wavelength of $2.500 \mu \mathrm{~m}$. It shows that the PCF can be applied in dispersion compensation for conventional fiber in optical communication systems.


Fig. 5 Variations of dispersion with input wavelength
The modal birefringence is $1.458 \times 10^{-2}$, and the beat length is 0.106 mm at the wavelength of $1.550 \mu \mathrm{~m}$. The confinement losses of $x$ - and $y$-polarized modes are $3.100 \times 10^{-4} \mathrm{~dB} / \mathrm{km}$ and $1.721 \mathrm{~dB} / \mathrm{km}$, respectively. The proposed PCF can perform SPSM operation because of the suppression of $y$-polarized mode. The SPSM operation is achieved with wider band of 950 nm . The total dispersion profile of the SPSM-PCF is disper-sion-flattened from $1.193 \mu \mathrm{~m}$ to $1.384 \mu \mathrm{~m}$. This dispersion property makes the proposed SPSM- PCF useful for various applications. The SPSM-PCF can be applied in dispersion compensation of conventional fiber at long wavelength band with 500 nm negative dispersion region.

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