# Human localization technology based on the pyroelectric infrared sensors 

WU Qin－Qin ${ }^{1}$ ，LI Xi－Cai ${ }^{1}$ ，WANG Yuan－Qing ${ }^{1,2^{2}}$ ，REN Shu－Ping ${ }^{3}$<br>（1．School of Electronic Science and Engineering，Nanjing University，Nanjing 210023，China；<br>2．Key Laboratory of Intelligent Optical Sensing and Manipulation，Ministry of Education， Nanjing University，Nanjing 210023，China；<br>3．JiangXi Academy of Sciences，Nanchang 330000，China．）


#### Abstract

A field of views of pyroelectric infrared sensors modulation strategy is proposed．The strategy can im－ prove the human localization resolution，and it will not reduce the detection distance of pyroelectric infrared sen－ sor．For the strategy，the field of views of pyroelectric infrared sensors are modulated by a mask．And the modu－ lated field of views overlap and interleave with each other to form some sampling areas．In order to verify the pro－ posed field of views modulation strategy，the human localization node which includes nine pyroelectric infrared sensors is fabricated．The modulated degree of the field of views of each pyroelectric infrared sensor is $36^{\circ}$ ．The degree of each sampling area is $4^{\circ}$ ．If the human moves in a sampling area，the corresponding pyroelectric infra－ red sensors will be triggered．The human position can be localized by using at least two nodes．According to the states of the pyroelectric infrared sensors，the human position can be estimated．In the experiment，two nodes are set in a $600 \mathrm{~cm} \times 600 \mathrm{~cm}$ square area，the theoretical error is analyzed by using least square estimation．The theo－ retical maximum error of the two nodes human localization equipment in a $600 \mathrm{~cm} \times 600 \mathrm{~cm}$ square area is about 70 cm ．Eight human positions are estimated in experiments，and the estimation route is formed by connecting all the estimated positions．The estimation route is close to the predefined route．The minimum and maximum estimation errors are about 4.42 cm and 16.91 cm respectively．


Key words：pyroelectric infrared sensor，human position localization，least square estimation PACS：07．60．－j，42．79．－e

# 基于热释电红外探测器的人体定位技术 

吴勤勤 ${ }^{1}$ ，李希才 ${ }^{1}$ ，王元庆 ${ }^{1,2^{*}}$ ，任舒平 ${ }^{3}$<br>（1．南京大学 电子科学与工程学院，江苏 南京 210023；<br>2．南京大学 智能光感知与调控技术教育部重点实验室，江苏 南京 210023； 3．江西省科学院，江西南昌 330000）


#### Abstract

摘要：提出了一种热释电红外探测器视场调制策略。此策略能够提高人体定位分辨率，并且不会降低探测器的探测距离。对于此策略，热释电红外探测器的视场被遮光板调制，且调制后的探测器视场相互重叠交错形成一些采样区域。为了验证此策略，制作了包含九个热释电红外探测器的人体定位节点，节点中所有调制后的探测器视场角均为 $36^{\circ}$ ，每一个采样区域的角度均为 $4^{\circ}$ 。如果受测者在一个采样区域中运动，对应的热释电红外探测器将被触发，至少需要两个人体定位节点才能实现人体定位。根据节点中热释电红外探测器的状态，能够估计人体的位置。实验中，在 $600 \mathrm{~cm} \times 600 \mathrm{~cm}$ 的方形区域内设置两个人体定位节点，使用最小二乘法估计理论误差，其最大理论误差为 70 cm 。实验中估计了八个人体位置，将所有的估计位置点连接起来形成估计路径。估计路径与预设路径十分接近。实验中的最小和最大定位误差分别为 4.42 cm 和 16.91 cm 。


关 键 词：热释电红外探测器；人体定位；最小二乘法Received date：2019－05－24，revised date：2019－11－24 收稿日期：2019－05－24，修回日期：2019－11－24
基金项目：国家重点研发计划（2016YFB0401500），江苏省重点研发计划（BE2016173），南京大学优秀博士研究生创新能力提升计划B
Foundation items：Supported by the National Key R\＆D Plan（2016YFB0401500），R\＆D Plan of Jiangsu Science and Technology Department （BE2016173），and Program B for Outstanding PhD Candidate of Nanjing University
作者简介（biography）：吴勤勤（1991－），男，江西南昌人，博士研究生。主要研究领域为热释电红外探测器及其应用，激光雷达系统及相关算法。
E－mail：wuqinqingreat＠sina．com
＊通信作者（＊Corresponding author）：E－mail：yqwang＠nju．edu．cn

## Introduction

Human tracking and localization technology is one of most significant topic for the security ${ }^{[1]}$ and machine vision ${ }^{[2]}$ ．Researchers have done a lot of work for the hu－ man localization and tracking．There are some kinds of strategy for human tracking and localization．The first strategy utilizes vision device to detect the target，such as visible－light camera and near－infrared camera ${ }^{[3]}$ ．The visible－light camera and near－infrared camera can quick and precise to find targets based on the computer vision and digital image processing techniques ${ }^{[4]}$ ．But the envi－ ronment factors such as high light background or weak light condition will affect the detection．And not all occa－ sions are suitable for installation of camera，such as bed－ room or toilet．In addition，the near－infrared camera need to use the near infrared source for illumination．The detection range of near－infrared camera is limited by the limitation of source illumination range．The second strat－ egy is based on wearable device．This method requires target human to wear a device on his glasses or collar， such as near－infrared led．And this method uses a detec－ tor such as position sensitive device（PSD）to track the wearable device ${ }^{[5]}$ ．However，the power unit for the wearable device cannot work for a long time，and the wearable device will lead to discomfort．The dense sens－ ing based activity monitoring is the third strategy，such as environment state－change sensors ${ }^{[6]}$ ，break－beam sen－ sors，pressure mats，contact switches ${ }^{[7]}$ ，microphones and pyroelectric infrared sensors．The dense sensing is suitable for intelligent environment enabled applica－ tions ${ }^{[8]}$ ．

Pyroelectric infrared sensors（PIR）${ }^{[9-11]}$ received ex－ tensive attention due to the low cost，low power consump－ tion and excellent performances．The PIR can detect the mid－infrared light（ $8 \sim 14 \mu \mathrm{~m}$ ）emitted by human body． Thus，the PIR can detect the human body without any help of other light source，and the human body doesn＇t need to equip any device．Furthermore，the detection based on the PIR doesn＇t belong to the imaging detec－ tion．Thus，it won＇t invade human privacy．It is suitable for most occasions．And the PIR only can be triggered by the dynamic changed light．The invariable light or heater in the field of views（FOVs）cannot trigger the sensor． Thus，the localization system composed by PIRs can avoid disturbances caused by the obstacles．

In this paper，a FOV modulation strategy is pro－ posed，and the human localization node based on the pro－ posed strategy is fabricated．The proposed FOVs modula－ tion strategy can improve the human localization resolu－ tion without reduction of the detection distance of the PIR．Owing to larger angle of modulated FOV and small－ er angle of sampling area（SA），the modulation strategy can achieve larger theoretical detection distance and higher angle resolution compare with the strategies which are reported in ${ }^{[12-14]}$ ．For our node，the angle of the modu－
lated FOV of each PIR is $36^{\circ}$ ，and the angle of each SA is $4^{\circ}$ ．We use two nodes to localize the human position in a $600 \mathrm{~cm} \times 600 \mathrm{~cm}$ square area，and the theoretical error is analyzed．The maximum theoretical error is about 70 cm ．For the experiment，the minimum and maximum lo－ calization errors are about 4.42 cm and 16.91 cm respec－ tively．

## 1 The principle of human localization by use of PIR

PIR is a frequently－used human body detection de－ vice．It is sensitive to $8 \sim 14 \mu \mathrm{~m}$ infrared light．The Fres－ nel lens can enhance the detection distance of PIR．If a human walks in the FOV of the PIR，the PIR will be trig－ gered and output analog signal．Process the signal to de－ termine the state of the PIR．Use the＇ 0 ＇and＇ 1 ＇（two states）to represent the PIRs are triggered or not ${ }^{[13,15]}$ ． According the states of the PIRs，the position of the hu－ man can be estimated．Some papers have been reported that use the PIRs to localize human position．In Ref．12， fourteen separate masks are used to modulate the FOVs of fourteen PIRs，the angle of the SA for each PIR is set to $5^{\circ}$ ，the sketch map of the modulation strategy can be seen in Fig． 1 （a）．In Refs．13－14，researchers use a mask to modulate the FOV of one PIR．The modulation strategy is shown in Fig．1（b）．


Fig． 1 The sketch map of the modulation strategy of Ref． 12 and Refs．13－14（a）The modulation strategy of Ref．12，（b）the mod－ ulation strategy of Refs．13－14
图1 文献［12］及［13－14］中所使用的调制策略示意图（a）文献 ［12］所使用的调制策略，（b）文献［13－14］所使用的调制策略

As shown in Fig．1（a－b），the $\sigma$ represents the angle resolution．Obviously，for these two kinds of modulation strategies，the smaller degree of FOV of PIR is，the high－ er angle resolution of system can be achieved．However， the smaller degree of FOV is，the less infrared energy the PIR can receive．It will impact the detection distance of the PIR．The sketch map of the proposed FOVs modula－ tion strategy can be seen in Fig． 2.

As shown in Fig． 2 （a），there is a rectangular win－ dow on the mask，and it can modulate the FOV of the PIR．The projection of the modulated FOV on $X-Y$ plane


Fig． 2 The sketch map of the proposed FOVs modulation strate－ gy（a）the FOV of one PIR is modulated by a mask，（b）ideally， the starting points of the FOVs of multiple PIRs are located at same point（ $Q$ ），and the FOVs stagger and overlap with each oth－ er to form multiple SAs．
图2 提出的视场调制策略示意图（a）遮光板调制单个热释电红外探测器的视场，（b）理想情况下，多个热释电红外探测器视场的起点位于同一点 $(Q)$ ，并且这些视场相互交错重叠形成多个采样区域。
is a fan－shaped．Set the angle of the projection to be $\gamma$ ． In order to achieve human position localization，multiple PIRs should be used．In this paper，we describe the pro－ posed modulation strategy based on the node which in－ cludes nine PIRs．The FOVs are labeled as $\mathrm{FOV}_{k}(k=1$ ， $2,3, \cdots \cdots, K, K=9)$ ．The FOVs of PIRs interleave and overlap with each other to form multiple SAs，as shown in Fig．2（b）．Ideally，assume that all the PIRs are located at same point $(Q)$ ．Thus，the starting points of all FOVs are also located at this point．

Set the angle of the detection area of the node which includes $K$ PIRs to be $\psi$ ，as shown in Fig．2（b）．The SAs are labeled as $S_{l}(l=1,2,3, \cdots \cdots, L)$ ．The angle $\sigma$ of each SA can be described in Eq．1：

$$
\begin{equation*}
\sigma=\frac{\psi}{L} \tag{1}
\end{equation*}
$$

where $L$ is the total number of SAs．And for the proposed strategy，$\psi$ also can be described as Eq． 2 ：

$$
\begin{equation*}
\psi=2 \gamma-\sigma=\frac{2 L \gamma}{L+1} \tag{2}
\end{equation*}
$$

The relationship between $K$ and $L$ can be described as Eq．3：

$$
\begin{equation*}
L=2 K-1 \tag{3}
\end{equation*}
$$

Substitute the Eq． 2 and Eq． 3 into Eq．1，the $\sigma=$ $\gamma / K$ can be obtained．For the proposed modulation strate－ gy，the angle resolution $\sigma$ is related to $\gamma$ and $K$ ．If the $\gamma$ is given，we can increase the $K$ to improve the angle reso－ lution，and the $\gamma$ doesn＇t need to be reduced．In order to verify the proposed modulation strategy，the human local－ ization node which include nine PIRs is fabricated，as shown in Fig．3（a）and Fig．3（b）．For the node，the $\gamma$ is equal to $36^{\circ}$ ，the $\psi$ is equal to $68^{\circ}, L$ is equal to 17 ，the $\sigma$ is equal to $4^{\circ}$ ．In addition，for the node and the pro－ posed modulation strategy，the maximum detection dis－ tance of each PIR is about 7 m ．

For the node，the PIRs（KP500B，Nisaila．The pa－ rameters of the KP500B can be seen in Table．1）are ar－ ranged in $3 \times 3$ matrix，the horizontal distance between ad－ jacent PIRs is 3.4 cm ．The arrangement of PIRs are shown in Fig．3（a）．The angle of the original FOV of the


Fig． 3 The physical map of the node，and the sketch map of the sampling areas in non－ideal case（a）The arrangement of PIRs， （b）the physical map of whole node，（c）the sketch map of the sampling areas of the node in non－ideal case
图3 节点实物图及非理想情况下采样区域示意图（a）热释电红外探测器的排布示意图，（b）整个节点的实物图，（c）非理想情况下采样区域示意图。

PIR with Fresnel lens is about $100^{\circ}$ ．The nine windows on the mask and the nine PIRs are corresponding one by one．As shown in Fig．3，it is impossible to set all detec－ tors at the same point．The $\mathrm{PIR}_{1} \sim \mathrm{PIR}_{3}$ move 3.4 cm to－ ward to left relative to $\mathrm{PIR}_{4} \sim \mathrm{PIR}_{6}$ ，and the $\mathrm{PIR}_{7} \sim \mathrm{PIR}_{9}$ move 3.4 cm toward to right relative to the $\mathrm{PIR}_{4} \sim \mathrm{PIR}_{6}$ ．As shown in Fig．3（c），if the $X$ axis coordinates of starting points of the FOVs of $\mathrm{PIR}_{4} \sim \mathrm{PIR}_{6}$ are $x$ ，the $X$ axis coordi－ nates of starting points of the FOVs of the $\mathrm{PIR}_{1} \sim \mathrm{PIR}_{3}$ and the $\mathrm{PIR}_{7} \sim \mathrm{PIR}_{9}$ are $x+3.4$ and $x-3.4$ respectively．Of course，the angles of the FOVs and the SAs remain un－ changed despite the movement of FOVs．

Table 1 The parameters of the KP500B
表1 KP500B 的参数

| Item | Parameters |
| :---: | :---: |
| Pass Band | $5 \sim 14 \mu \mathrm{~m}$ |
| Transmittance of the filter | $>75 \%$ |
| Sensitivity | $3300 \mathrm{~V} / \mathrm{W}$ |
| Detectivity | $1.5 \times 108 \mathrm{~cm} \cdot \mathrm{Hzl} / 2 \cdot \mathrm{~W}-1$ |
| Noise | $<200 \mathrm{mV}\left(\mathrm{mVp}-\mathrm{p}, 25^{\circ} \mathrm{C}\right)$ |

When human walks into different sampling area， the different combination of＇ 0 ＇，and＇ 1 ＇sequence can be got．Thus，the＇ 0 ＇and＇ 1 ＇sequence can indicate which SA the human located in．The codes of SAs are list in Table 2.

If the human located in a SA，we can think that the SA is＇triggered＇．Assume a human located in $S_{l}$ ，and only the $S_{l}$ is＇triggered＇．We can assume that the human is moving at the angular bisector line $A_{l}$ of the $S_{l}$ ．Such as the point $P$ which is locate at $A_{l}$ ，as shown in Fig．3（c）． The angle $\theta$ between the $A_{l}$ and $X$ axis can be described in Eq． $4^{[15]}$ ．

$$
\begin{equation*}
\theta=\frac{\pi-\psi}{2}+\frac{\psi}{L} l-\frac{\psi}{2 L} \tag{4}
\end{equation*}
$$

It should be noted that there is no case that multiple SAs are triggered simultaneously for the proposed modu－ lation strategy．However，the human body may cover multiple SAs or the human body only covers one SA，and

Table 2 The codes scheme of the 17－SAs．
表 217 个采样区域的编码序列

| SA | The state of PIR |  |  |  |  |  |  |  |  | Sequence |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |  |
| 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 100000000 |
| 2 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 110000000 |
| 3 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 111000000 |
| ．．．．．． |  |  |  |  | $\cdots$ |  |  |  |  | ．．．．．． |
| 15 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 1 | 000000111 |
| 16 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 000000011 |
| 17 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 000000001 |

he（she）makes minor motion．In these case，the multiple SAs can take turn to be triggered．Assume these SAs are $S_{l}, S_{l+1}, \cdots \cdots, S_{l+m}$ ，we can think that the human is located at the angular bisector line of the area which consists of $S_{l}$ ， $S_{l+1}, \cdots \cdots, S_{l+m}$ ．The $\theta$ can be described in Eq．5：

$$
\begin{equation*}
\theta=\frac{\pi-\psi}{2}+\frac{\psi}{L} m-\frac{\psi}{2 L}(m-l+1) \tag{5}
\end{equation*}
$$

In order to further verify the proposed modulation strategy．We use the node to localize the human posi－ tion．At least two nodes are required for localization．As－ sume that there are two nodes are set in a square area （ $600 \mathrm{~cm} \times 600 \mathrm{~cm}$ ），as shown in Fig．4．The symmetry axes of the detection areas of the node－1 and node－2 inter－ sect vertically at $Q^{\prime}$ ，and they intersect the $X$ and $Y$ axes at $Q_{1}(300,0)$ and $Q_{2}(0,300)$ respectively．The valid lo－ calization area of two nodes human localization equip－ ment is colored in lilac．


Fig． 4 Two nodes are used for human localization．图4 两个节点应用于人体定位

Name the＇triggered＇SAs $S_{i l}(i=1,2)$ ．The $i$ is the index of nodes．The angle between angular bisector $A_{i l}$ and $X$ axis is named $\theta_{i t}$ ．It should be noticed that，the $\theta_{1 l}$ and $\theta_{2 l}$ are equal to $\theta$ and $\theta-\pi / 2$ respectively，the $\theta$ can be calculated by using the Eq． 4 or Eq．5．According to Fig．3（c），the coordinates of the intersections $\left(x_{i l}, y_{i l}\right)$ of the $A_{i l}$ and $X$ axis or $Y$ axis can be calculated，and they are listed in Table ． 3.

The slopes of the angular bisector $A_{i l}$ are name $k_{i l}$（if

Table 3 The intersection（ $x_{i v} y_{i l}$ ）of the angular bisector $A_{i l}$ and $X$ axis or $Y$ axis．
表3 角平分线 $A_{i l}$ 和 $X$ 轴或 $Y$ 轴的交点 $\left(x_{i l}, y_{i l}\right)$

| The Angular Bisector | $x_{i l}(\mathrm{~cm})$ | $y_{i l}(\mathrm{~cm})$ |
| :---: | :---: | :---: |
| $A_{11}, A_{12}, A_{1(10)}, A_{1(11)}$ | $300+3.4$ | 0 |
| $A_{13}, A_{1(12)}$ | $300+1.7$ | 0 |
| $A_{14}, A_{15}, A_{1(9)}, A_{1(13)}, A_{1(14)}$ | 300 | 0 |
| $A_{16}, A_{1(15)}$ | $300-1.7$ | 0 |
| $A_{17}, A_{18}, A_{1(16)}, A_{1(17)}$ | $300-3.4$ | 0 |
| $A_{21}, A_{22}, A_{2(10)}, A_{2(11)}$ | 0 | $300-3.4$ |
| $A_{23}, A_{2(12)}$ | 0 | $300-1.7$ |
| $A_{24}, A_{25}, A_{29}, A_{2(13)}, A_{2(14)}$ | 0 | 300 |
| $A_{26}, A_{2(15)}$ | 0 | $300+1.7$ |
| $A_{27}, A_{28}, A_{2(16)}, A_{2(17)}$ | 0 | $300+3.4$ |

the $k_{i l}$ is exist），and they can be described in Eq． 6.

$$
\begin{equation*}
k_{i l}=\tan \theta_{i l} \tag{6}
\end{equation*}
$$

And the expressions of the angular bisectors of the ＇triggered＇SAs can be described in Eq．7：

$$
\begin{equation*}
y_{e s t}-y_{i l}=k_{i l}\left(x_{\text {est }}-x_{i l}\right) \tag{7}
\end{equation*}
$$

where the $\left(x_{\text {est }}, y_{\text {est }}\right)$ is the estimated human position． Substituting the $i=1$ and $i=2$ into the Eq．7．Then the Eq． 8 can be got．

$$
\left\{\begin{array}{l}
y_{\text {est }}-y_{1 l}=k_{1 l}\left(x_{\text {est }}-x_{1 l}\right)  \tag{8}\\
y_{\text {est }}-y_{2 l}=k_{2 l}\left(x_{\text {est }}-x_{2 l}\right)
\end{array}\right.
$$

The Eq． 8 in matrix form can be described in Eq． 9

$$
\begin{equation*}
A p=B \tag{9}
\end{equation*}
$$

where $\boldsymbol{p}=\left[x_{\text {est }}, y_{\text {est }}\right]^{\mathrm{T}}, \boldsymbol{A}$ and $\boldsymbol{B}$ can be described as fol－ lows：

$$
\begin{aligned}
\boldsymbol{A} & =\left[\begin{array}{ll}
k_{1 l} & -1 \\
k_{2 l} & -1
\end{array}\right] \\
\boldsymbol{B} & =\left[\begin{array}{l}
k_{1 l} x_{1 l}-y_{1 l} \\
k_{2 l} x_{2 l}-y_{2 l}
\end{array}\right]
\end{aligned}
$$

The human position $P$ can be calculated by Eq．10：

$$
\begin{gather*}
x_{\mathrm{est}}=\frac{y_{2 l}-y_{1 l}+k_{1 l} x_{1 l}-k_{2 l} x_{2 l}}{k_{1 l}-k_{2 l}} \\
y_{\text {est }}=\frac{k_{1 l}\left(k_{2 l} x_{1 l}-x_{2 l}\right)+k_{1 l} y_{2 l}-k_{2 l} y_{1 l}}{k_{1 l}-k_{2 l}} \tag{10}
\end{gather*}
$$

Substituting the values of $k_{i l}$ and the corresponding $\left(x_{i l}, y_{i l}\right)$ which are listed in Table 3 into Eq．10，the hu－ man position can be calculated．In addition，the $k_{1 l}$ may not exist．In this case，the $x_{\text {est }}=x_{1 l}=300$ ．And substitute it into Eq．8．The $y_{\text {est }}=y_{2 l}+k_{2 l}\left(300-x_{2 l}\right)$ can be ob－ tained．

## 2 The estimation error analysis

The errors result from the hypothesis that the human is located at the angular bisector of the＇triggered＇SA． The estimation human position is $\left(x_{\text {est }}, y_{\text {est }}\right)$ ．Assuming the errors of $x_{\text {est }}, y_{\text {est }}$ are $\Delta x, \Delta y$ respectively．Thus，the real coordinate of the human position $(x, y)$ can be de－ scribed in Eq．11：

$$
\left\{\begin{array}{l}
x_{\text {est }}=x-\Delta x  \tag{11}\\
y_{\text {est }}=y-\Delta y
\end{array}\right.
$$

Substituting the Eq． 11 into the Eq．8，the Eq． 12 can be got．

$$
\left\{\begin{array}{l}
k_{1 l} \Delta x-\Delta y=k_{1 l} x-k_{1 l} x_{1 l}-y+y_{1 l}  \tag{12}\\
k_{2 l} \Delta x-\Delta y=k_{2 l} x-k_{2 l} x_{2 l}-y+y_{2 l}
\end{array}\right.
$$

Set the $\Delta \boldsymbol{p}=[\Delta x, \Delta y]^{\mathrm{T}}$ ．The matrix form of Eq． 12 is shown in Eq．13：

$$
\begin{equation*}
C \Delta p=\Delta b \tag{13}
\end{equation*}
$$

where the $\boldsymbol{C}$ and $\Delta \boldsymbol{b}$ are described as follows：

$$
\begin{gathered}
\boldsymbol{C}=\left[\begin{array}{ll}
k_{1 l} & -1 \\
k_{2 l} & -1
\end{array}\right] \\
\boldsymbol{\Delta} \boldsymbol{b}=\left[\begin{array}{l}
k_{1 l} x-k_{1 l} x_{1 l}-y+y_{1 l} \\
k_{2 l} x-k_{2 l} x_{2 l}-y+y_{2 l}
\end{array}\right]
\end{gathered}
$$

The least square estimation for error can be de－ scribed in Eq．（14）：

$$
\begin{equation*}
\Delta \boldsymbol{p}=\left(\boldsymbol{C}^{\mathrm{T}} \boldsymbol{C}\right)^{-1} \boldsymbol{C}^{T} \Delta \boldsymbol{b} \tag{14}
\end{equation*}
$$

And if the $k_{1 l}$ does not exists，the $x_{11}=300$ ．Thus， the $\Delta x=0, \Delta y=y-y_{2 l}+k_{21} x_{2 l}-k_{21} x$ ，and it can be simplified to $\Delta y=y-y_{2 l}-k_{21} x$ ．

According to the formulas mentioned above，the lo－ calization error of two nodes human localization equip－ ment can be calculated by using the numerical simula－ tion．The error is shown in Fig．5（a）and Fig．5（b）．

It can be seen from Fig． 5 （a－b），the farther away from two nodes，the larger localization error is．And as shown in Fig．5（a），in the quadrilateral which is formed by intersections of two SAs of two nodes，the farther away from the intersection of the two angular bisectors，the larger localization error is．The maximum theoretical er－ ror of the two nodes human localization equipment in 600 $\mathrm{cm} \times 600 \mathrm{~cm}$ square area is about 70 cm ，as shown in Fig．5（b）．We only analyze the error in the case that the human only＇trigger＇one SA of a node，because there is no case that multiple SAs are triggered simultaneously for the proposed modulation strategy．Assume the human lo－ cates at the angular bisector line of the area which is con－ sist of multiple SAs，the method of human position local－ ization and error analysis are same with that mentioned above．


Fig． 5 The error analysis of the two nodes human localization equipment（a）Plane diagram of error analysis，（b）3D diagram of error analysis．
图5 两节点人体定位装置的误差分析（a）误差分析结果平面图，（b）误差分析结果三维图。

## 3 Experiment and discussion

In order to verify the proposed FOVs modulation strategy and the node，the human position localization ex－ periments have been done．According to the setup which is shown in Fig．4，we set two nodes in a $600 \mathrm{~cm} \times 600 \mathrm{~cm}$ square area，and the coordinates of node－1 and node－2 are $(300,0)$ and $(0,300)$ respectively．Before the ex－ periments，the directions of two nodes should be calibrat－ ed to make the symmetry axes of detection areas of two nodes are perpendicular．And they are also perpendicu－ lar to the sidelines of the square area．The target human walks along the predefined route on the ground，stop in eight setting positions and do some minor movement． The speed is about $1 \mathrm{~m} / \mathrm{s}$ ．Record the output signals of the PIRs and then determine their states．The states de－ termined processes can be seen in Fig． 6.

The original signal of a PIR is shown in Fig． 6 （a）． The signal is denoised by using the wavelet soft threshold noise reduction method．The denoised signal is shown in Fig．6（b）．The absolute value of the denoised signal is calculated，as shown in Fig．6（c）．But this process can introduce some interference points into the signal．The interference points are emphatic marked by red boxes，as shown in Fig．6（c）．In order to reduce the impact of the interference points，the signal should be smoothed，as shown in Fig．6（d）．Set a threshold（15\％of the maxi－ mum of signal）．If the amplitude of the signal is larger than the threshold，set the amplitude to＇ 1 ＇，else to


Fig． 6 The PIR states determined processes（a）the original sig－ nal，（b）denoise the signal by using wavelet soft threshold noise reduction method，（c）calculate the absolute values of the sig－ nal，（d）smoothing the signal，（e）set a threshold．If the ampli－ tude of the signal larger than the threshold，set the amplitude to ＇ 1 ＇，else to＇ 0 ＇，（ f ）further optimize the signal to determine the state of the PIR．
图6 热释电红外探测器状态确定过程（a）初始信号，（b）使用小波软阈值消噪法对信号降噪，（c）计算信号的绝对值，（d）平滑信号，（e）设置阈值，如果信号的幅度大于阈值，则将信号的幅度置1，否则置 0 ，（f）进一步优化信号以确定热释电红外探测器的状态。
＇0＇，as shown in Fig． 6 （e）．Some parts of state signal are misjudged due to the small absolute value，and they are marked by the red boxes，as shown in Fig．6（e）．Fur－ ther optimize the signal to determine the final state of the PIR，as shown in Fig．6（f）．After the states of all PIRs are determined，the＇triggered＇SAs can be determined． The recorded＇triggered＇SAs of two nodes in experi－ ments are shown in Table 4.

It can be seen from the Table 4，multiple SAs are take turn to be＇triggered＇when the human stands at the

Table 4 The result of the experiment
表4 实验结果

| No． | Node－1 | Node－2 | Real／cm | Estimation／cm | Error／cm |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $r_{1}$ | $S_{12} \sim S_{11}$ | $S_{6} \sim S_{8}$ | $(250,270)$ | $(254.6,266.6)$ | 8.09 |
| $r_{2}$ | $S_{10} \sim S_{9}$ | $S_{8} \sim S_{9}$ | $(290,290)$ | $(293.2,293.2)$ | 4.47 |
| $r_{3}$ | $S_{8} \sim S_{7}$ | $S_{9} \sim S_{10}$ | $(325,310)$ | $(329.0,308.1)$ | 4.42 |
| $r_{4}$ | $S_{7} \sim S_{6}$ | $S_{10} \sim S_{11}$ | $(365,335)$ | $(355.5,334.0)$ | 9.57 |
| $r_{5}$ | $S_{6} \sim S_{5}$ | $S_{11} \sim S_{12}$ | $(400,370)$ | $(392.0,364.9)$ | 9.44 |
| $r_{6}$ | $S_{5} \sim S_{4}$ | $S_{12} \sim S_{13}$ | $(425,400)$ | $(432.5,407.8)$ | 10.86 |
| $r_{7}$ | $S_{5} \sim S_{4}$ | $S_{13} \sim S_{14}$ | $(450,435)$ | $(444.4,444.4)$ | 10.94 |
| $r_{8}$ | $S_{4}$ | $S_{14} \sim S_{15}$ | $(470,480)$ | $(479.7,493.8)$ | 16.91 |

setting positions and does some minor motions．The＇trig－ gered＇SAs of two nodes are listed in $2^{\text {th }}$ and $3^{\text {th }}$ columns of Table 4．According to the＇triggered＇SAs of the node－ 1 and node－2，the $\theta_{1 l}$ and $\theta_{2 l}$ can be calculated by Eq． 4 or Eq．5．The slopes $k_{1 l}, k_{2 l}$ and two straight line expres－ sions can be determined by Eq． 6 and Eq． 8 respective－ ly．The estimation human position is the intersection of these two straight lines．The coordinates of eight setting positions and corresponding estimated positions are listed in $4^{\text {th }}$ and $5^{\text {th }}$ columns of Table 4 ．The errors are calculat－ ed and listed in $7^{\text {th }}$ column of Table 4 ．It can be seen from the $7^{\text {th }}$ column of Table 4 ，the minimum and maxi－ mum errors are about 4.42 cm and 16.91 cm respective－ ly．The average error is about 9.34 cm ．The minimum error 4.42 cm is smaller than 9 cm and 32 cm which are reported in Ref． 15 and 13 respectively．The maximum error is similar to the maximum error which is reported in Ref．15．The smaller minimum error may be due to the higher angle resolution．The node used in experiment can be seen in Fig． 7 （a），the height of the node is 130 cm ．Connect all the estimated points to form the estima－ tion route．The estimated route and predefined route can be seen in Fig．7（b）．The predefined route and estimat－ ed route are represented by the red curve and blue curve respectively．It can be seen from the Fig．7（b）that the estimated route is close to the predefined route．

In practice，some factors can affect the accuracy of human localization by using PIRs．For example，the oth－ er heating sources in FOV，human body temperature and


Fig． 7 The pyroelectric infrared human localization node and the experiment result（a）the pyroelectric infrared human local－ ization node，（b）the predefined route and estimated route．
图7 热释电红外人体定位节点及实验结果（a）热释电红外人体定位节点，（b）预设路径及估计路径
so on．The dynamic infrared source，such as the moving animal，the air conditioner at working，head shaking heating system and the flying curtains，can affect the lo－ calization．Commonly，the pyroelectric signals caused by above heaters are different with that of human．The in－ terference signals can be filtered by suitable filter．And the pattern recognition algorithms can be used to recog－ nize whether the heater is human or not ${ }^{[16-17]}$ ．The tem－ perature of body can also affect the detection of the PIR． The human body temperature is generally maintained at about $36^{\circ} \mathrm{C}$ ．But it may change drastically after the hu－ man stay in cold or hot condition for a long time．Owing to the weaker pyroelectric signal，low body temperature may lead to incorrect localization．The high human body temperature doesn＇$t$ affect the localization．And the problems caused by the body temperature may go away quickly once the body returns to a normal tempera－ ture ${ }^{[18]}$ ．Furthermore，the proposed method only can lo－ calize one human at one time．We are researching more advanced algorithms to enable the localization system to support multi－objective localization simultaneously．

## 4 Conclusion

In this paper，a field of views of pyroelectric infra－ red sensors modulation strategy is proposed．For the strategy，the angle resolution is related to the angle of FOV of localization system and the number of the PIRs． The proposed FOVs modulation strategy can improve the angle resolution without reduction of the detection dis－ tance of PIR．The theoretical localization error also be analyzed by using the least square estimation．The errors result from the hypothesis that the human is located at the angular bisector of the＇triggered＇SA．In order to verify the proposed strategy．The human localization node which include nine PIRs is fabricated．The degrees of each SA，the FOV of each PIR and the detection area of the node are $4^{\circ}, 36^{\circ}$ and $68^{\circ}$ respectively．The maxi－ mum theoretical error of the two nodes localization equip－ ment in $600 \mathrm{~cm} \times 600 \mathrm{~cm}$ square area is about 70 cm ．Ac－ cording to the state sequences of PIRs of the nodes，the target human position can be estimated．We set two nodes in a $600 \mathrm{~cm} \times 600 \mathrm{~cm}$ square area，and do the local－ ization experiments．Eight positions are estimated．The minimum and maximum errors are about 4.42 cm and 16.91 cm respectively．The estimation route is close to the predefined route．The detection distance of the node is about 7 m ．The experiment result indicates that the proposed FOVs modulation strategy is valid．

## Acknowledge

This work supported by the National Key R\＆D plan
（2016YFB0401500），R\＆D plan of Jiangsu science and technology department（BE2016173）and program B for outstanding PhD candidate of Nanjing University．

## References

［1］Chodon P，Adhikari D M，Nepal G C，et al．Passive infrared（PIR） sensor based security system［J］．International Journal of Electrical， Electronics \＆Computer System，2013，14（2）：1－5．
［2］Feng G D，Guo X M，Wang G L，Infrared motion sensing system for human－following robots［J］．Sensors and Actuators A：Physical， 2012，186：1－7．
［3］Chowdhury M，Gao J B，Islam R．Robust human detection and local－ ization in security applications［J］．Concurrency and Computation－ Practice \＆Experience，2017，29：e3977．
［4］Kakumanu P，Makrogiannis S，Bourbakis N．A survey of skin－color modeling and detection methods［J］．Pattern Recognition，2007， 40 （3）：1106－1122．
［5］Meijer G C M，Vandrecht J，Dejong P C，et al．New concepts for smart signal processors and their application to PSD displacement transducers［J］．Sensors and Actuators A：Physical，1992，35（1）： 23－30．
［6］Tapia E M，Intille S S，Larson K．Activity recognition in the home using simple and ubiquitous sensors［C］／／2nd International Confer－ ence on Pervasive Computing，2004，3001：158－175．
［7］Wilson D H，Atkeson C．Simultaneous tracking and activity recogni－ tion（STAR）using many anonymous，binary sensor［C］／／Pervasive Computing，Proceedings，2005，3468：62－79．
［8］Chen L，Hoey J，Nugent C D，et al．Sensor－based activity recogni－ tion［J］．IEEE Transactions on Systems Man and Cybernetics Part C－ Applications and Reviews，2012，42（6）：790－808．
［9］Sun X Y，Luo W B，Meng J，et al．Monolithic pyroelectric infrared detectors using SiO 2 aerogel thin films［J］．Sensors and Actuators $A$ ： Physical，2015，228：69－74．
［10］Wu Q Q，Wang Y Q，Ren S P．Low cost and anti－noise infrared de－ vice based on saw－tooth thermal isolation structure［J］．Sensors and Actuators A：Physical，2017，266：178－184．
［11］Luo W B，Wu Q Q，Wu C G，et al． $\mathrm{Pb}(\mathrm{ZrTi}) 0.98 \mathrm{Mn} 0.0203$ weight ratio effects on the properties of $\mathrm{Pb}(\mathrm{ZrTi}) 0.98 \mathrm{Mn} 0.0203 / \mathrm{P}$（VDF－ TrFE）compostie film and infrared detectors［J］．Journal of Materials Science：Materials in Electronics，2017，28（4）：3474－3480．
［12］Zhou W C，Li F M，Li D，et al．A human body positioning system with pyroelectric infrared sensor［J］．International Journal of Sensor Networks，2016，21（2）：108－115．
［13］Jiang L，Zhang T，He F，et al，Preprocessing design in pyroelectric infrared sensor－based human－tracking system：on sensor selection and calibration［J］．IEEE Transactions on Systems Man Cybernetics－ Systems，2017，47（2）：263－275．
［14］Shankar M，Burchett J B，Hao Q，et al．Human－tracking systems us－ ing pyroelectric infrared detectors［J］．Optical Engineering，2006， 45（10）： 106401.
［15］Feng G D，Guo X M，Wang G L．Infrared motion sensing system for human－following robots［J］．Sensors and Actuators A：Physical， 2012，185：11－7．
［16］Gong W G，Wen K，He L F，et al．Human and Nonhuman Recogni－ tion Using Pyroelectric Infrared Detector［J］．International Journal of Thermophysics，2012，33（10－11）：2237－2241．
［17］Zhao J D，Gong W G，Tang Y Z，et al．EMD－based symbolic dynam－ ic analysis for the recognition of human and nonhuman pyroelectric infrared signals［J］．Sensors，16（1）： 126.
［18］Gong J，Zhang Y，Zhou X．Pyro：Thumb－tip gesture recognition us－ ing pyroelectric infrared sensing［C］／／UIST＇17：Proceedings of The 30th Annual ACM Symposium On User Interface Software And Tech－ nology，2017，553－563．

