

# Terahertz beam reconfigurable micro-strip Quasi-Yagi-Uda antenna based on monolayer graphene

YAO Wen-Long, GUO Xu-Guang\*, ZHU Yi-Ming, LI Ping

(Shanghai Key Lab of Modern Optical Systems, Terahertz Technology Innovation Research Institute, and Engineering Research Center of Optical Instrument and System, Ministry of Education, University of Shanghai for Saence and Technology, Shanghai 200093, China)

**Abstract:** We propose a beam reconfigurable micro-strip quasi-Yagi-Uda (QYU) antenna operating at terahertz (THz) frequencies. The antenna, on a metal-backed SiO<sub>2</sub> substrate, consists of a metallic micro-strip transmission line, a metallic reflector, a metallic half-round micro patch, and three groups of monolayer-graphene-patch directors. Because the conductivities of the graphene patches can be electrically tuned, the radiation direction of the QYU antenna can be dynamically controlled by adjusting the bias voltages applied to the graphene patches. The basic properties and the tunable behaviors of the antenna are systemically simulated and optimized. It has very fast modulation speed and very low return loss. In particular, the numerical results show that the main radiation lobe angle  $\varphi$  (azimuth angle) of the QYU antenna can be swept from 30° to 150° in  $\theta=60^\circ$  (zenith angle) plane with different configurations of bias voltages applied to the graphene-patch directors. The proposed antenna is very suitable for THz beam reconfigurable applications, such as phased array radar systems.

**Key words:** beam reconfigurable antenna, graphene, patch antenna, Yagi-Uda antenna

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## 基于石墨烯的波束可重构太赫兹天线

姚文龙, 郭旭光\*, 朱亦鸣, 李萍

(上海市现代光学系统重点实验室, 教育部太赫兹技术创新研究院, 光学仪器与系统工程研究中心, 上海理工大学, 上海 200093)

**摘要:** 设计了一种工作在大赫兹(THz)频率下的微带八木(QYU)天线. 该天线由金属微带传输线、金属反射器、金属半圆形辐射贴片和三组单分子层-石墨烯-贴片导向器组成. 由于石墨烯的电导率可电调谐特性, 可以通过调整施加在石墨烯导向器上的偏置电压来动态调控天线的辐射方向. 通过对天线的基本性能和可调制特性系统地模拟和优化, 数值结果表明, 通过改变加在石墨烯导向器的偏压, 天线的主辐射波瓣角 $\varphi$ (方位角)可以在30°-150°的范围内进行扫描, 并且具有非常快的调制速度和非常低的回波损耗. 该天线非常适合于相控阵雷达等THz波束可重构应用.

**关键词:** 波束可重构天线; 石墨烯; 贴片天线; 八木天线

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## Introduction

The beam reconfigurable antennas have attracted growing interests, the beam directivities and the radiation patterns of which can be dynamically changed according to demand. Such antennas have the potentials to avoid noise sources, provide larger coverage by steering

the angle of the main lobe, and improve the beam steering capability<sup>[1-2]</sup>. The reconfigurability of beam directivity is a frontier subject in the field of antennas. The beam reconfigurable antennas can be exploited in the multiple-input-multiple-output (MIMO) systems to increase the system capacity<sup>[3]</sup>. And such antennas are compatible with micro-strip-based monolithic-microwave integrated-

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**Biography:** Yao Wen-Long (1991-), male, Changchun, Jilin, M. A. Research fields focus on Terahertz antenna. E-mail: 1299514128@qq.com

\* **Corresponding author:** E-mail: xgguo\_sh@qq.com; ymzhu@usst.edu.cn

circuit (MMIC), which are useful to improve the performance of MMIC. Traditionally, the ways to realize reconfigurable antennas are mostly to load high-frequency electronic devices and use mechanical methods to adjust the antenna structures, which are complicated in structure, frequency limited, and inefficient<sup>[1]</sup>. Graphene, as the first truly two-dimensional material, has unique thermal, mechanical, optical, and electrical properties<sup>[4-7]</sup>. Among all these interesting properties, the bias-voltage-tunable optical conductivity covering the THz band is very useful for providing an effective way to realize real-time electrically reconfigurable THz antennas.

In recent years, many investigations have been performed in the research of graphene-based reconfigurable THz antennas and a series of progress has been achieved. Dragoman *et al.* designed a graphene-based THz dipole antenna and confirmed that the radiation characteristics can be controlled by applying a bias voltage to graphene<sup>[8]</sup>. Llatser *et al.* proposed a graphene nano-patch antenna and systematically analyzed its THz radiation characteristics<sup>[9]</sup>. Huang *et al.* proposed a switchable high-impedance surface (HIS) based on single-layer graphene and designed a radiation pattern reconfigurable THz antenna based on such a switchable HIS<sup>[10]</sup>. Zheng *et al.* proposed a reconfigurable MIMO system using graphene nano-patch antennas<sup>[11]</sup>. Wu *et al.* designed a graphene-based Yagi-Uda antenna with reconfigurable radiation patterns<sup>[12]</sup>. However, these antennas are not very good at steering the angle of the THz beam due to the limited steering angle and the low radiation efficiency.

The Yagi-Uda antenna was first reported in 1928<sup>[13]</sup>. Because of the feature characteristics, such as end-fire radiating pattern and simple structure, the Yagi-Uda antennas have been used to design the beam reconfigurable antennas<sup>[14-17]</sup>. Several approaches for achieving the reconfigurability of antenna are through micro-strip Yagi-Uda antennas<sup>[18]</sup>, which we refer to as quasi-Yagi-Uda (QYU) antennas. In general, a QYU antenna is composed of several patches (one driven element, one reflector, and one or more directors) that are electromagnetically coupled to one another to steer the angle of the main lobe.

In this paper, a type of graphene-based beam reconfigurable QYU antennas working at THz frequencies is proposed. Graphene patches are used to replace the metallic parasitic elements in the conventional Yagi-Uda antenna, and the patches are divided into three groups, each of which is as a director. Because the complex conductivity of graphene can be tuned by applying different bias voltages, by switching the states of different group of graphene-patch directors, the graphene patches can be operated as directors or not, and the function of sending (receiving) signals only toward (from) the target direction is achieved. When bias voltages are applied to different graphene-patch directors, the beam direction of the proposed device can be scanned in the wide-angle (azimuth angle  $\varphi$ ) range of  $30^\circ$ - $150^\circ$  in zenith angle  $\theta=60^\circ$  plane. Moreover, it

has very fast modulation speed, low return loss, and high radiation efficiency.

## 1 Tunability of graphene optical conductivity

Graphene is a two-dimensional material composed of one layer of carbon atoms with a two-dimensional honeycomb lattice structure, which was first obtained in 2004 by Geim and Novoselov<sup>[19]</sup>. For a single-layer graphene, due to the unique electric band structure of linear energy-momentum dispersion relation near the Dirac cones at the K and K' points in the first Brillouin zone, the optical conductivity can be written as the sum of the intra-band conductivity  $\sigma_{\text{intra}}$  and the inter-band conductivity  $\sigma_{\text{inter}}$ <sup>[20,22-23]</sup>,

$$\sigma_{\text{intra}} = \frac{2e^2 K_B T}{\pi \hbar (\Gamma - j\omega)} \ln \left[ \frac{\left( -\frac{E_F}{2K_B T} \right) +}{\left( \frac{E_F}{2K_B T} \right)} \right], \quad (1)$$

and

$$\sigma_{\text{inter}} = \frac{-je^2}{4\pi \hbar} \ln \left[ \frac{2|\mu_c| - (\omega - j2\Gamma)\hbar}{2|\mu_c| + (\omega - j2\Gamma)\hbar} \right], \quad (2)$$

where  $e$  is the electron charge,  $\omega$  is the angular frequency,  $K_B$  is the Boltzmann constant,  $\hbar$  is the reduced Planck constant,  $T$  is the temperature in Kelvin,  $E_F$  is the Fermi energy,  $\mu_c$  is the chemical potential, and  $\Gamma=1/2\tau$  is the carrier scattering rate with  $\tau$  the carrier scattering time.

In the microwave, THz, and far-infrared spectral bands, theoretical and experimental investigations show that the optical conductivity of graphene satisfies the widely used Drude model<sup>[21,24-28]</sup>. And in the THz band, inter-band transitions are prohibited due to insufficient incident photon energy, and intra-band transitions are in the dominant position. Within the framework of Boltzmann transport theory, the intra-band Drude conductivity for single-layer graphene in THz band can be written as<sup>[24,26,29]</sup>,

$$\sigma_{\text{intra}} = \frac{je^2|E_F|/\hbar^2}{\pi(\omega + j\Gamma)}. \quad (3)$$

The Fermi energy  $E_F$  is a function of carrier concentration  $N$ ,

$$E_F = \pm \hbar v_f (\pi |N|)^{1/2}, \quad (4)$$

where  $v_f$  is the Fermi velocity, and the positive (negative) sign in the formula represents the electron (hole) doping.

From equations (3) and (4), the intra-band optical conductivity can be controlled by adjusting the Fermi energy (carrier concentration) in graphene. The bipolar electrical doping effect of graphene allows its electron (hole) concentration to be continuously changed up to  $10^{13} \text{ cm}^{-2}$ <sup>[20,30]</sup>. Therefore, a bias voltage can be applied

to effectively adjust the carrier concentration and then the optical conductivity of graphene.

## 2 Simulation and antenna performance

### 2.1 QYU antenna with one group of director

Recently, beam reconfigurable antennas have attracted many interests in wireless communication<sup>[31]</sup>. In some cases, in order to vary the resonant frequencies, the lengths of dipolar graphene antennas can be dynamically changed<sup>[32]</sup>. In other scenarios, by phasing different elements of an antenna array, the reconfiguration features can be realized. In this paper, as shown in Fig. 1, a QYU antenna working at 500 GHz is proposed to realize the beam reconfigurable feature.

The features of the proposed antenna are numerically simulated with the ANSYS High Frequency Structure Simulator (HFSS) software<sup>[33]</sup>. The antenna working at 500 GHz and operating frequency range of the antenna is from 470 GHz to 530 GHz. The wave port excitation mode is selected and the input impedance is set to 50  $\Omega$ . The layered impedance boundary condition is used for the thin graphene patches. Each graphene patch has two states. If a high bias voltage (Fermi energy  $\mu_c=1$  eV, denoted as “1”) is applied to the graphene patches, the conductivity of the graphene patches will significantly in-

crease. This will result in the metal-like behavior of graphene patches, and the graphene patches work as directors as in the conventional Yagi-Uda antenna. On the contrary, once a low or no bias voltage (Fermi energy  $\mu_c=0$  eV, denoted as “0”) is applied to the graphene patches, they will behave as thin dielectric layers, which have no essential influence on the behavior of the patch antenna. Depending on the different bias voltages applied to the graphene patches, the antenna can work in two different states (state 1 for  $\mu_c=0$  eV and state 2 for  $\mu_c=1$  eV).

Fig. 1(a) and (b) show the schematic of the antenna. The substrate is a high resistivity silicon wafer with the size of  $L_x \times L_s$  and  $L_s=1.8$  mm the length and width. There is a copper ground layer with thickness  $T$  on the high resistivity silicon substrate. A 30- $\mu\text{m}$ -thick ( $t_s$ )  $\text{SiO}_2$  dielectric cavity layer is on the metallic ground layer. The relative permittivity of  $\text{SiO}_2$  is  $\epsilon_r=4$ . The size of the micro-strip fed line is  $l_m \times w_m$ , the driven patch is  $L \times W$ , and the thickness of both of the micro-strip fed line and the driven patch is  $T$ . The size of the reflector patches is  $l_r \times w_r$ , the distance between the reflector patch and the driven patch is given by  $l_{rs}$ . The graphene patches are used as the director in the Yagi-Uda antenna, the size of which is given by  $l_d \times w_d$ , and the gap between the two graphene patches is given by  $g$ . The p-doped silicon strips beneath the graphene patches are used as electrical connections between the metallic gating pads and the gra-

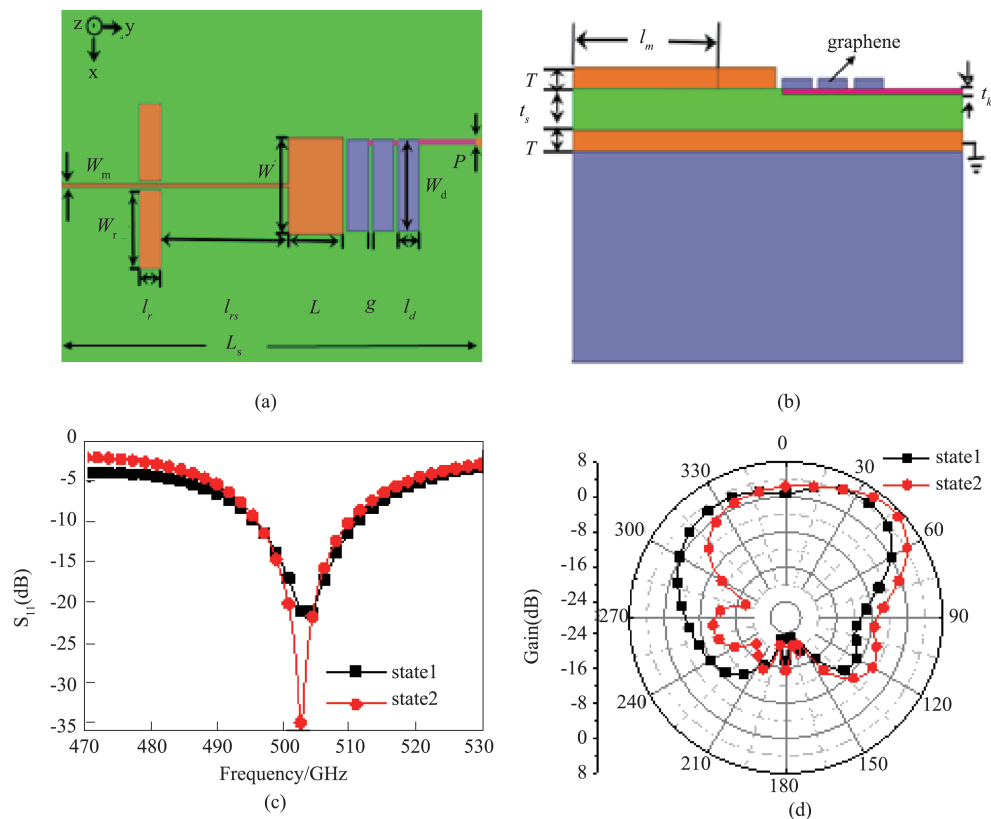


Fig. 1 Schematic of the proposed antenna and the basic performance parameters, (a) Top view, (b) Side view, (c) Reflection coefficient  $S_{11}$ , and (d) Simulated radiation patterns in E-plane for the two working states of the antenna (states 1 and 2 for the cases of unbiased and biased)

图1 天线原理图和基本性能参数, (a)天线的俯视图, (b)天线的侧视图, (c)反射系数 $S_{11}$ , (d)石墨烯-贴片的两种状态下天线E面辐射方向图(状态1:无偏和状态2:加偏置电压)

phene patches, and the thickness of the doped Si strip is given by  $t_k$ . The dimension of the driven copper patch is  $p \times p$ . As reported in Ref. [34], We can calculate the theoretical value of the length ( $L$ ) and width ( $W$ ) of the driven patch. Further,  $L$ ,  $W$  and other parameters of the antenna are optimized by simulation and the results are listed in Table 1.

Fig. 1(c) depicts the reflection coefficients  $S_{11}$  for the antenna working in state 1 and state 2 for the proposed antenna. The antenna is resonating at 500 GHz, and the -10 dB return loss bandwidth is about 3% (495 GHz - 510 GHz). When the antenna is in state 1 and state 2 respectively, the simulated radiation pattern in E-plane (where the electric field vector and the maximum radiation direction are located) of the proposed antenna is shown in Fig. 1(d). It can be observed that in E-plane when the antenna is in state 1, the antenna behaves as a conventional patch antenna. When the antenna is in state 2, the angle of the main lobe veers round along the graphene patches. This confirms the effect of the graphene director on the radiation direction of the antenna.

## 2.2 QYU antenna with two groups of directors

The antenna structure shown in Fig. 1 confirms the guiding effect of the graphene director on the beam direction in E-plane. But it cannot achieve the beam shift in the zenith angle direction. To overcome this deficiency, we design an improved antenna structure shown in Fig. 2

**Table 1** Antenna parameters (units:  $\mu\text{m}$ )

$L$	130	$w_m$	5	$l_{rs}$	300	$g$	8
$W$	190	$l_r$	50	$l_d$	50	$T$	0.2
$l_m$	540	$w_r$	150	$w_d$	179	$t_s$	30
$t_k$	0.2	$p$	10				

(a). Compared with the former antenna structure, the graphene-patch director is divided into two groups, and each of the two groups is similar to the director in the conventional Yagi-Uda antenna. The gap between the graphene patches along the  $y$ -axis is  $g=8\mu\text{m}$  and the widths of all the gaps are the same. All the graphene patches have the same size, given by  $l_{d2}=129\mu\text{m}$  and  $w_{d2}=94\mu\text{m}$ . To realize strong coupling between the driven patches and the two neighboring graphene patches of the director, a very small value of  $s=0.5\mu\text{m}$  is chosen. In order to keep strong couplings between the neighboring graphene patches within the same group, the parameters  $l_{d2}$  and  $g$  are optimized, and the parameters  $h_1=39\mu\text{m}$  and  $h_2=76\mu\text{m}$  are also optimized to realize a higher gain. The two groups of graphene directors are labeled as  $D_1$  and  $D_2$ , respectively. Depending on the different bias voltages applied to the graphene patches, the antenna can work in three different states, (state 1:  $(1, 0)$  with  $\mu_c=1\text{ eV}$  for graphene patches in  $D_1$  and  $\mu_c=0\text{ eV}$  for graphene patches in  $D_2$ ; state 2:  $(0, 1)$ ; and state 3:  $(1, 1)$ ).

Fig. 2(b) shows the reflection coefficient  $S_{11}$  of the

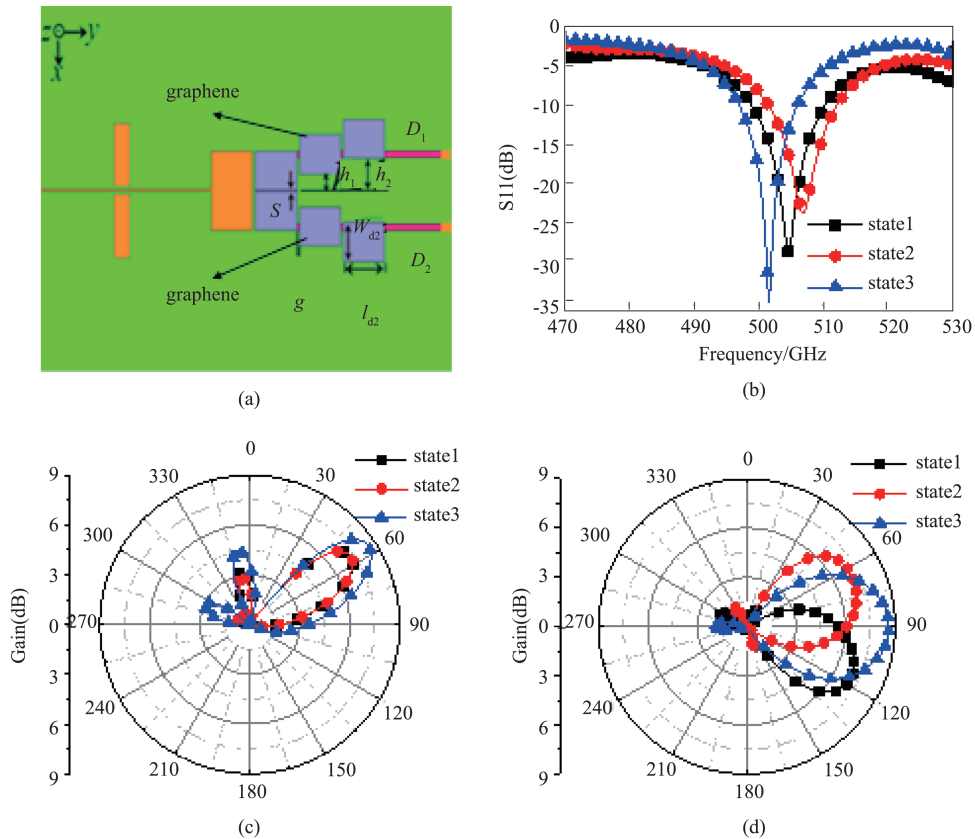


Fig. 2 (a) Schematic of the antenna with two groups of directors, (b) Reflection coefficient  $S_{11}$ , (c) E-plane radiation pattern and (d)  $\theta = 60^\circ$  plane radiation pattern of the proposed antenna operating at different states.

图2 (a)天线结构示意图,(b)反射系数 $S_{11}$ , (c) E面辐射方向图, (d)天线在不同工作状态下的 $\theta = 60^\circ$ 平面辐射方向图

proposed antenna. The resonant frequency of the antenna is about 500 GHz, and for different working states of the antenna, the resonant frequency reveals a tiny shift. It is because that the effective impedance of the graphene directors and the driven patch is a little different when the antenna works in different states. The -10 dB return loss bandwidth is about 2.5%.

Fig. 2(d) shows the radiation pattern of the antenna in  $\theta=60^\circ$  plane. It can be observed that, when the antenna is in states 1, 2, and 3, the angles of the main lobe in  $\theta=60^\circ$  plane are about  $120^\circ$ ,  $60^\circ$ , and  $90^\circ$ , respectively. Thus, the angle of the main lobe for the antenna in  $\theta=60^\circ$  plane can be swept from  $60^\circ$  to  $120^\circ$ . While in the E-plane, the angle of the main lobe is fixed at about  $\theta=60^\circ$ , as shown in Fig. 2(c).

### 2.3 QYU antenna with three groups of directors

For the antenna structure mentioned in subsection 2.2, the main lobe can be swept from  $60^\circ$  to  $120^\circ$  in  $\theta=60^\circ$  plane. In order to increase the steering angle, a QYU antenna with three groups of graphene-patch directors is considered. In this case, we find that a rectangle driven metallic patch does not work well. Therefore, the driven metallic patch is changed from a rectangle patch to a half-round patch, and the structure of the improved antenna is shown in Fig. 3(a).

Fig. 3(a) shows the structure of the antenna with three groups of graphene-patch directors. Different from the former two antennas, the driven patch is a half-round

patch. The graphene patches are divided into three groups, and each of them is similar to the director in the conventional Yagi-Uda antenna. The diameter of the driven patch is  $W_1=370 \mu\text{m}$ , and the distance between the reflector patch and the driven patch is  $l_{rs}=175 \mu\text{m}$ . The gap between two neighboring graphene patches in the first and the third group is given by  $g_1=15 \mu\text{m}$ , and the gap between two neighboring graphene patches in the second group is given by  $g=20 \mu\text{m}$ . The angle of graphene patches in each group is given by  $\alpha_1=58^\circ$ ,  $\alpha_2=40.3^\circ$ , and  $\alpha_3=30.2^\circ$  respectively, and the width of the graphene patch is given by  $l_{ds}=100 \mu\text{m}$ . The three groups of graphene directors are labeled as  $D_1$ ,  $D_2$ , and  $D_3$ , respectively. Depending on the different bias voltages applied to the graphene patches, the antenna can work in six different states, (state 1: (1, 0, 0) with  $\mu_c=1 \text{ eV}$  for graphene patches in  $D_1$  and  $\mu_c=0 \text{ eV}$  for graphene patches in  $D_2$  and  $D_3$ ; state 2: (1, 1, 0); state 3: (0, 1, 0); state 4: (0, 1, 1); state 5: (0, 0, 1) and state 6: (1, 1, 1)).

Fig. 3(b) shows the simulated reflection coefficient  $S_{11}$  of the antenna. The resonant frequency of this antenna is around 500 GHz. In all working states, good impedance matching with the return loss  $S_{11}<-30 \text{ dB}$  is obtained around the resonant frequency. The -10 dB return loss bandwidth is about 8%.

Fig. 3(d) shows radiation patterns of the proposed antenna in the  $\theta=60^\circ$  plane operated at different states. One can see that in state 1, only  $D_1$  works as a director,

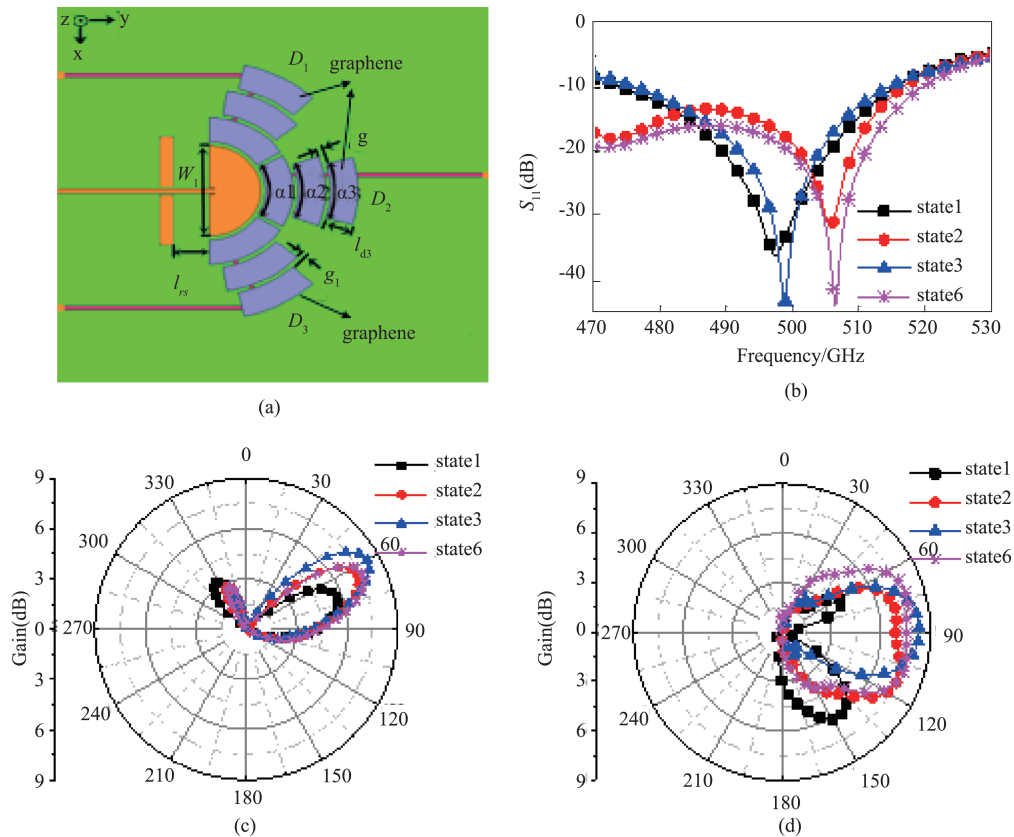


Fig. 3 (a) Structure of the antenna with three groups of directors, (b) Reflection coefficient  $S_{11}$  of the proposed antenna operating at different states, (c) E-plane radiation pattern, and (d) Radiation pattern in  $\theta=60^\circ$  plane

图3 (a)天线结构示意图, (b)反射系数  $S_{11}$ , (c) E面辐射方向图, (d) 天线在不同工作状态下的  $\theta=60^\circ$  平面辐射方向图



and the angle of the main lobe is  $150^\circ$ . In state 2, both  $D_1$  and  $D_2$  work as directors, and the angle of the main lobe is  $110^\circ$ . In state 3 only  $D_2$  works as a director, and the angle of the main lobe is  $90^\circ$ . Because of the symmetry of the antenna, the radiation patterns of the antenna working in states 4 and 5 and working in states 1 and 2 will be symmetric about the  $y$ -axis. Thereby the beam in  $\theta=60^\circ$  plane of the antenna can be deflected from  $30^\circ$  to  $150^\circ$ . While the angle of the main lobe in E-plane is fixed at about  $\theta=60^\circ$ , as shown in Fig. 3(c). The maximal values of gain are in the range of 6.5 dB - 8.7 dB. The angles of the main lobe and the maximal values of gain for the antenna in different working conditions are shown in table 2.

Fig. 4(a-1)-(a-4) and (b-1)-(b-4) show the 3D radiation patterns that are observed from different perspectives of the antenna. From the 3D radiation patterns, the beam reconfigurable ability can be seen clearly. Fig. 4(c-1)-(c-4) show the surface current distributions for the proposed antenna in different working conditions. It is easy to see that different group graphene patches of the antenna are resonating in different working conditions. For instance, in state 1, as shown in Fig. 4(c-1), only

$D_1$  is resonating, the surface current is excited only on  $D_1$  and it works as a director, the other graphene patches with  $\mu_c=0$  eV have no effects on the behaviors of the antenna. While in state 2, only  $D_1$  and  $D_2$  are resonating. Because of the symmetry of the structure, the surface current distributions of the antenna working in states 4 and 5 and the antenna working in states 2 and 1 will be symmetric about the  $y$ -axis. The variations of radiation patterns are well-explained by the current distributions of the antenna working in different states. And the capacitive structure is used to apply bias voltages to graphene patches to achieve electrical regulation. Therefore, when a bias voltage is applied to graphene, there is no current distribution or voltage drop on the surface, and the voltage is evenly distributed.

### 3 Discussion

In this Section, the effects of the relaxation time in graphene and the p-doped silicon strip are discussed. The graphene quality is primarily determined by the relaxation time. In the above simulations, the relaxation time 20 ps in graphene is selected. In Fig. 5(a), several relaxation times in the range of 0.1-20 ps are set in the

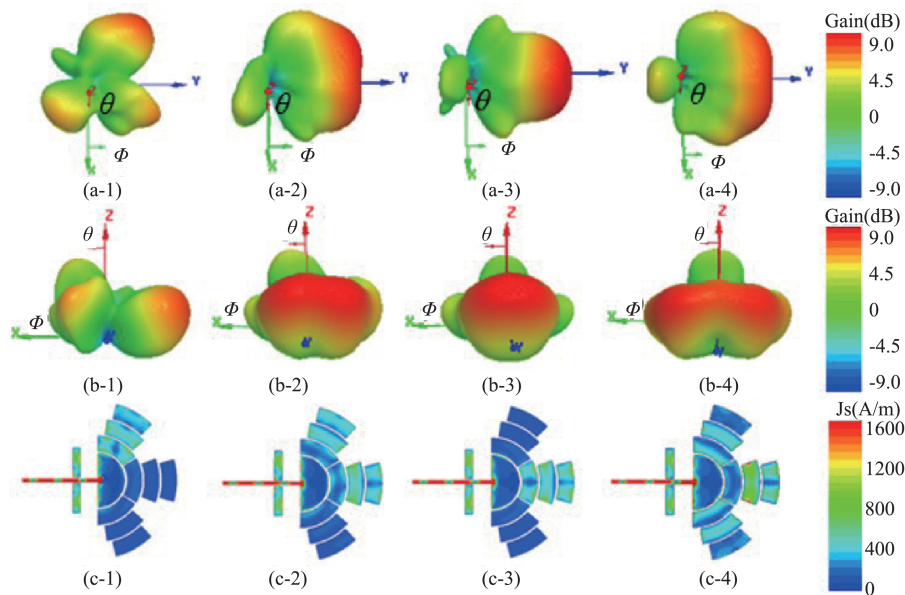


Fig. 4 (a-1)~(a-4) and (b-1)~(b-4), 3D radiation patterns in different planes. (c-1)~(c-4) Surface current ( $J_s$ ) distributions for the proposed antenna in different working states. (a-1), (b-1), and (c-1) for state 1; (a-2), (b-2), and (c-2) for state 2; (a-3), (b-3), and (c-3) for state 3; (a-4), (b-4), and (c-4) for state 6.

图4 (a-1)~(a-4)和(b-1)~(b-4), 三维辐射方向图。(c-1)~(c-4) 天线在不同工作状态下表面电流分布图,其中,(a-1),(b-1),和(c-1)对应状态 1;(a-2),(b-2),和(c-2)对应状态 2;(a-3),(b-3),和(c-3)对应状态 3;(a-4),(b-4),和(c-4)对应状态 6

**Table 2 Antenna performance**

Working state of antenna	1	2	3	4	5	6
Return loss (dB)	-36	-32	-43	-32	-36	-44
Voltage standing wave ratio (VSWR)	1.03	1.12	1.01	1.12	1.03	1.01
-10 dB bandwidth	9%	12%	8%	12%	8%	14%
Angle of main lobe ( $\varphi$ )	$150^\circ$	$110^\circ$	$90^\circ$	$60^\circ$	$30^\circ$	$90^\circ$
Gain (dB)	6.6	7.8	8.7	7.8	6.6	7.5
Radiation efficiency	85%	90%	85%	90%	85%	96%

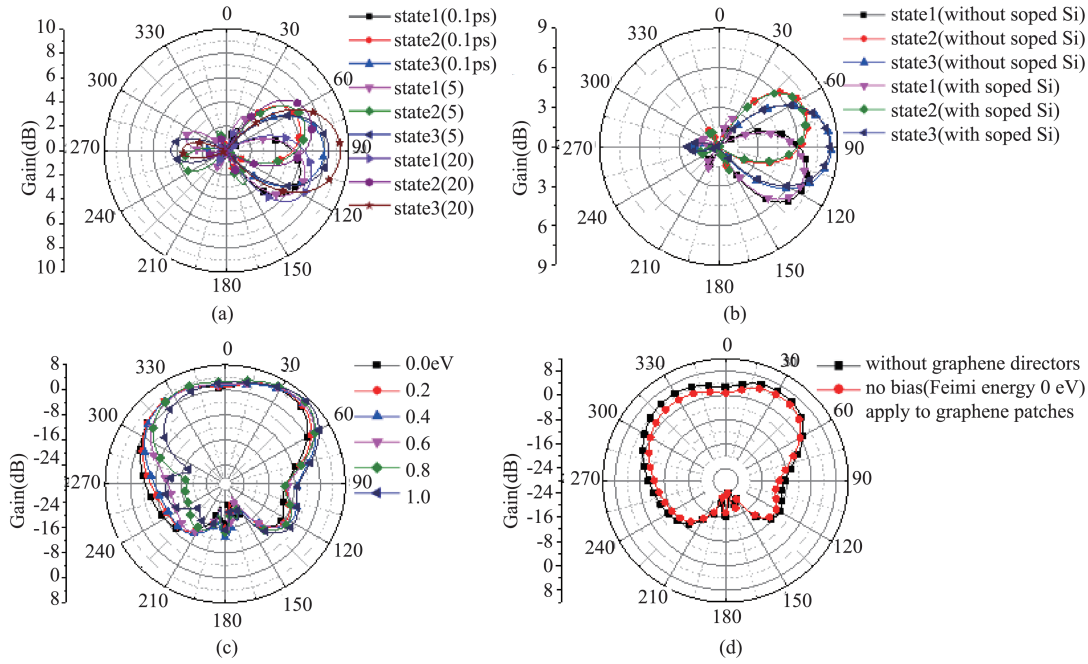


Fig. 5 (a) and (b) Radiation patterns of antenna proposed in Section 2. 2, (a) With different electron relaxation times in graphene, (b) With and without p-doped silicon strips, (c) and (d) Radiation patterns of antenna proposed in section 2. 1, (c) With different bias voltages applied to the graphene-patch directors, and (d) With graphene-patch directors with  $\mu_c=0$  eV and without graphene-patch directors.

图5 (a)和(b)在2.2节中提出的天线辐射方向图, (a)石墨烯的不同电子弛豫时间, (b)有轻掺杂硅条和没有轻掺杂硅条. (c)和(d)在2.1节中提出的天线的辐射方向图, (c)石墨烯-贴片导向器施加不同偏置电压, (d)石墨烯-贴片导向器工作在无偏状态(施加0 eV偏压)和没有石墨烯-贴片导向器

simulations. The numerical results show that the relaxation time has a negligible effect on the angle of the main lobe and very little effect on the gain of the antenna. The gain of the antenna increases with the increase in relaxation time.

We also study the effects of the p-doped silicon strips. As shown in Fig. 5(b), the p-doped silicon strips have negligible effects on antenna performance. The electron plasma frequency is<sup>[35]</sup>

$$f_r = \left( n_0 e^2 / 4\pi^2 m_e \varepsilon_0 \varepsilon \right)^{1/2}, \quad (5)$$

where  $n_0$  is the electron density,  $e$  is the electron charge,  $m_e$  is the electron effective mass,  $\varepsilon_0$  is the vacuum dielectric constant and  $\varepsilon$  is the dielectric permittivity.

The p-doped silicon, which we choose has a very low doping concentration ( $1e15 \text{ cm}^{-3}$ ), from equation (5), the electron plasma frequency of the p-doped silicon is 116 GHz, which is much less than the antenna working frequency (500GHz). Thus, the p-doped silicon strips have negligible effects on antenna performance.

The magnitudes of bias voltages applied to the graphene patches are considered for the antenna mentioned in section 2. 1, as shown in Fig. 5(c). As the Fermi energy increase from  $\mu_c=0$  eV to  $\mu_c=1$  eV, the graphene patches change from dielectric layers to metal-like layers, and the angle of the main lobe in E-plane converts from  $\theta=0^\circ$  to  $\theta=50^\circ$ . Especially when the Fermi energy is lower than 0.4 eV, the graphene patches cannot be operated as directors, and when the Fermi energy is higher than 0.5 eV, the graphene patches gradually behave as

metal-like layers and work as directors. Furthermore, if the Fermi energy  $\mu_c=0$  eV, as shown in Fig. 5(d), the radiation patterns of the antenna are almost the same as those of the antenna without graphene patches. This indicates that the graphene patches with  $\mu_c=0$  eV mainly behave as dielectric layers.

## 4 Conclusion

In this work, reconfigurable QYU micro-strip antennas with graphene-patch directors are proposed. Because the complex conductivity of graphene can be tuned by changing the bias voltages, the graphene patches can be electrically switched between metallic state and dielectric state. Therefore, the graphene-patch directors can be electrically reconfigurable and the main lobe angle of the antenna can be electrically swept in a large range in  $\theta=60^\circ$  plane ( $60^\circ$  to  $120^\circ$  for the configuration of two graphene-patch directors and  $30^\circ$  to  $150^\circ$  for the configuration of three graphene-patch directors). The reconfigurable behaviors of the antenna are not sensitive to the scattering time of graphene. It is expected that such a graphene-based antenna is attractive for THz application in the future.

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