Long-term ultrastable frequency dissemination via a 50-km spooled fiber link using a two-section DFB laser

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1. Introduction

Radio-frequency (RF) signals play a crucial role in modern communication, radar, radio astronomy, and other fields. With the increasing demand for high precision and stability in communication systems and scientific instruments, stable transmission and accurate phase reference have become key challenges. Traditional RF signal transmission often relies on transmission media and cables, but it is constrained by issues such as electromagnetic interference, transmission loss, and phase drift, which limit the performance improvement of the system. To address these challenges, fiber-optic-based RF phase-stable transmission technology has received extensive research and application in recent years. Fiber optics, as a low-loss and low-attenuation transmission medium, offers advantages such as high bandwidth, low transmission loss, and immunity to electromagnetic interference, making it an ideal choice for achieving high-precision and high-stability RF signal transmission. Fiber transmission enables the conversion of RF signals to optical signals through electro-optic modulation and modulation–demodulation techniques, which are then transmitted and restored to RF signals through photoelectric conversion at the receiving end. Direct modulation lasers (DMLs) offer high modulation bandwidth, enabling high-speed data transmission to meet the demands of large-scale data transfer. Additionally, DMLs achieve real-time performance and low latency, making them suitable for applications requiring quick response and real-time performance. Furthermore, this technology simplifies system architecture by replacing expensive modulators, reducing costs and complexity, while typically consuming less power, thus saving energy. The use of the REC technique eliminates the need for electron-beam lithography in
the fabrication of laser chips, resulting in lower manufacturing costs for analog DMLs\textsuperscript{[16–18]}. The key factors for assessing the performance of phase-stable transmission include transmission distance, transmission signal frequency range, stability loss, testing time, temperature disturbance resilience, phase compensation range, system cost, and integration level, among others\textsuperscript{[19–22]}. Currently, there are few systems in the research of long-distance frequency synchronization transmission that simultaneously meet all of these criteria.

In this paper, we propose a system design utilizing a two-section analog DML fabricated using the REC technique as the optical carrier RF transmission module for transmitting RF signals over a 50-km spooled fiber link. We present the characterization of the current-power curves and 3-dB modulation bandwidth of the analog DML and provide details on the experimental setup, techniques, and testing methods employed to achieve phase stability. We evaluate the long-term and short-term stability of the system whether DML applies current to the reflection section or not and investigate its resilience to temperature disturbances by introducing temperature variations in the transmission link.

2. Experimental Design

The schematic diagram of the phase-stable transmission system is shown in Fig. 1. The principle of phase stabilization in the entire transmission system is to actively detect the phase noise introduced during the link transmission at the central site and perform precompensation so that the remote-site users can use frequency signals consistent with the phase of a rubidium atomic clock. To measure the stability loss of the system transmission, both the central site and the remote site of the phase-stabilized transmission system are located within the Engineering Research Center of Precision Photonics Integration and System Application (Nanjing University), Ministry of Education. The transmission link uses a spooled 50 km G.652 optical fiber; such a setup makes the transmission link more sensitive to temperature changes and environmental vibrations. A portion of the optical signal transmitted to the remote site is demodulated by a photodetector (PD) to measure stability loss, while another portion carrying error signals is fed back to the central site via an optical circulator for compensation generation. The phase-stabilized transmission system compensates for the delay in the link by controlling the phase of an oven-controlled crystal oscillator (OCXO) using a proportional-integral-differential (PID) algorithm. The frequency signal generated by dielectric-resonant oscillator (DRO\textsubscript{1}) is referred to as

$$V_1 = A \cos(\omega_1 t + \tau_1).$$

(1)

$\omega_1$ is in the X-band. Due to variations in the signal amplitude caused by device performance, the signal amplitude will be disregarded in the subsequent equations. To measure the stability loss of the transmission system, it is necessary to determine the phase fluctuations caused by environmental effects during signal transmission in the optical fiber. Three DROs locked to a rubidium atomic clock are required to generate auxiliary signals, and the frequency signals generated by them are denoted as

$$V_2 = \cos(\omega_2 t + \tau_2),$$

$$V_3 = \cos(\omega_3 t + \tau_3),$$

$$V_p = \cos(\omega_p t + \tau_p),$$

(2)

and satisfy

$$\left\{ \begin{array}{l}
\omega_2 + \omega_3 = 2\omega_p \\
\tau_2 + \tau_3 = 2(\tau_p + \epsilon)
\end{array} \right..$$

(3)

The $V_1$ signal generated by DRO\textsubscript{1} is modulated by the two-section analog DML and then passes through the optical circulator (OC) and OC\textsubscript{1} (20:80) before entering the fiber link. To further improve the stability of the transmission system, the environmental effects on the distance between the analog DML and OC\textsubscript{1} need to be taken into account. Twenty percent of the optical signal coupled out by OC\textsubscript{1} is collected by PD\textsubscript{1} and demodulated, resulting in an electrical signal,

$$V_4 = \cos(\omega_1 t + \tau_4),$$

(4)

where $\tau_4$ carries the error information for this section. Most of the received optical signal at the remote site is sent back through the same path, except for a small portion that is demodulated by PD\textsubscript{2}. The returned optical signal is amplified by the erbium-doped fiber amplifier (EDFA) and then passes through an optical filter (OF) to remove excess background noise before being detected and demodulated by PD\textsubscript{3}. This results in an electrical signal,

$$V_5 = \cos(\omega_1 t + \tau_4 + 2\tau'),$$

(5)

where $\tau'$ represents the delay introduced by a single transmission on the link. By mixing $V_2$ and $V_4$, the difference frequency signal is obtained,

$$V_6 = \cos[(\omega_1 - \omega_2)t + (\tau_4 - \tau_2)].$$

(6)
and by mixing \( V_3 \) and \( V_5 \), the difference frequency signal is

\[
V_7 = \cos[(\omega_3 - \omega_1)t + (\tau_3 - \tau_4 - 2\tau^*)].
\]  

(7)

Finally, the difference frequency signal is obtained by mixing \( V_6 \) and \( V_7 \).

\[
V_8 = \cos[2(\omega_1 - \omega_3 - \omega_4)t + 2\tau_1 + 2\tau^* - \tau_2 - \tau_3] = \cos[2(\omega_1 - \omega_3) + 2(\tau_4 + \tau^* - \tau_p - \varepsilon)],
\]

(8)

where \( V_8 \) is the error signal applied to the OCXO. Since \( \varepsilon \) represents a fixed phase difference that does not affect the final frequency stability, it can be ignored. By continuously correcting the frequency and phase of the OCXO using \( V_8 \), it can satisfy

\[
\begin{align*}
\omega_1 &= \omega_p \\
\tau_4 + \tau^* &= \tau_p.
\end{align*}
\]

(9)

Therefore, the signal \( V_6 \) demodulated by \( PD_2 \) at the far end can be expressed as

\[
V_9 = \cos(\omega_1 t + \tau_4 + \tau^*) = \cos(\omega_p t + \tau_p),
\]

(10)

which indicates that the phase of the demodulated signal \( V_9 \) at the remote site is locked to the frequency signal \( V_p \) at the central site, achieving stable frequency transmission and synchronization.

3. Results and Discussion

The DML plays a crucial role in phase-stable transmission systems. As an optical carrier RF transmission module, it is responsible for modulating the desired RF signal onto the optical carrier. By modulating the laser’s current directly, RF signals can be transmitted over the fiber link without the need for an external modulator. The stability and performance of the DML directly impact the quality and reliability of the phase-stable transmission system.

In light of this, we have developed an analog DML that meets the requirements for high-precision phase-stable transmission. The schematic diagram of the two-section analog DML chip is shown in Fig. 2(a). The designed laser chip consists of a laser section (LS) and a reflection section (RS). The design of the LS is similar to a standard DFB laser, with a \( \lambda/4 \) shift added in the center of the grating layer. Antireflection (AR) coatings are applied to both surfaces to ensure wavelength accuracy. The wavelength of the laser is mainly determined by the sampling period in the laser section. The cavity length of the LS is 400 \( \mu \)m. Since power loss in optical signal transmission over long distances is inevitable, it is necessary for the laser to have a sufficiently high initial output power to overcome the degradation of the signal-to-noise ratio with increasing transmission distance. Therefore, the cavity length is designed to be relatively long. Considering the duty cycle of the sampled grating, the effective coupling coefficient is approximately 3000 m\(^{-1}\). Due to the presence of strong feedback in the RS, it is required to have a slightly smaller normalized coupling coefficient in the LS (less than 1.2) to ensure stable single-mode characteristics. The cavity length of the RS is 600 \( \mu \)m, and there is no phase shift in the grating layer. The LS and RS share a common seed grating, and the effective coupling coefficient of the reflection section is also 3000 m\(^{-1}\), which greatly reduces the fabrication requirements. Additionally, both the LS and RS have a duty cycle of 0.5, maximizing the coupling strength of the grating. The two-section analog DML fabricated using the REC technology not only has low production costs but also offers high wavelength accuracy.

The inset shows the packaged form of the analog DML chip. Static characteristics testing was performed on the packaged analog DML. Figure 2(b) shows the power-bias current (P-I) curves of the two-section analog DML. The green line represents the output power of the laser when the current of the RS is 0 mA and the current of the LS varies. The orange line represents the output power of the laser when the current of the LS is 140 mA and the current of the RS varies. The threshold current of the two-section analog DML is 30 mA, which can be optimized by increasing the grating coupling coefficient. Due to the longer cavity length designed, the two-section analog DML exhibits a higher saturated output power. Even when the current reaches 150 mA, the laser output power is still not saturated. Due to absorption loss, the feedback effect from the RS is weak when \( I_{RS} = 0 \text{ mA} \). When a small current is injected into the RS, the feedback is enhanced, leading to a significant increase in the laser output power. As the injected current into the RS continues to increase, the output power of the two-section analog DML reaches saturation. Figures 2(c) and 2(d) present the measurement results of the modulation bandwidth of the two-section analog DML using a vector network analyzer. When no current is injected into the RS, the analog DML behaves similarly to an
undoubtedly DFB laser with AR–AR coatings. As the injected current into the LS increases ($I_{LS} = 110, 120, 130, 140 \text{ mA}$), the modulation bandwidth of the analog DML also increases. When $I_{LS} = 150 \text{ mA}$, the modulation bandwidth reaches its maximum value, approximately $16 \text{ GHz}$. With the continuous increase in the injected current into the RS ($I_{RS} = 0, 5, 10, 15, 20, 25, 30, 35 \text{ mA}$), the modulation bandwidth of the analog DML further increases and can reach $18 \text{ GHz}$. This bandwidth is also covering the entire X-band.

To estimate the performance of the phase-stable transmission system, it is necessary to compare the received frequency signal $V_{10}$ at the remote site with the reference frequency signal $V_0$ in terms of relative phase. This provides the frequency stability of $V_{10}$ relative to $V_0$, representing the overall transmission stability of the system. Currently, the industry-standard frequency measurement instruments are the Microsemi 5125A from the United States and the VCH 320 from Russia. Due to limitations in measurement techniques (dual-mixing measurement) of these instruments, their long-term stability is difficult to measure at the level of $10^{-18}$. Under special measurement conditions (e.g., constant temperature, ultra-quiet environment, seismic resistance), they can achieve a stability level of $10^{-18}$.

Therefore, the dedicated frequency stability measurement instrument, Microsemi 5125A, does not meet the measurement requirements. Instead, a direct mixing method is proposed to directly evaluate the RF transmission performance. The principle is to mix the recovered RF signal $V_{10}$ at the terminal station with the source signal $V_0$. Since the frequencies of the two input signals are the same, the relative phase variation between the two input signals can be reflected by the amplitude fluctuation of the mixer output voltage. By using a high-precision voltmeter (Keithley 2010) to measure the voltage $V(t)$ at the intermediate frequency (IF) port of the mixer, the corresponding relative delay fluctuation $\Delta \phi(t)$ can be deduced. This can be used for calculating the frequency stability. In Fig. 1, the local oscillator (LO) input of the mixer serves as the reference frequency source,

$$V_0 = A \cos \omega t.$$  

The RF input of the mixer is the signal to be phase-detected,

$$V_{10} = B \cos(\omega t + \Delta \phi(t)).$$  

The difference frequency signal obtained after mixing $V_0$ and $V_{10}$, which have the same frequency but a phase difference $\Delta \phi(t)$, is

$$V_{IF}(t) = C \cos \Delta \phi(t) + D,$$  

where $C$ represents the amplitude of the beat frequency signal, and $D$ is the output DC potential. The measurement value of $V_{IF}$ can be monitored in real time using a digital multimeter. By manually changing the phase of the RF input signal to allow $\Delta \phi(t)$ to undergo a phase change of $2\pi$, the maximum value $V_{IF_{\text{max}}}$ and minimum value $V_{IF_{\text{min}}}$ will appear when $\Delta \phi(t)$ takes the values of $0$ and $\pi$, respectively. Through simple calculations, $C$ and $D$ can be expressed using the known maximum and minimum values,

$$C = \frac{V_{IF_{\text{max}}}-V_{IF_{\text{min}}}}{2},$$

$$D = \frac{V_{IF_{\text{max}}}-V_{IF_{\text{min}}}}{2}.$$  

Thus, the phase difference can be inferred from the measured values of $V_{IF}$ as

$$\Delta \phi(t) = \arccos \left[ \frac{2V_{IF}(t) - (V_{IF_{\text{max}}} + V_{IF_{\text{min}}})}{V_{IF_{\text{max}}} - V_{IF_{\text{min}}}} \right].$$  

The corresponding relative time delay fluctuation, $\Delta \Phi(t)$, is given by

$$\Delta \Phi(t) = \frac{\Delta \phi(t)}{2\pi \omega} = \arccos \left[ \frac{2V_{IF}(t) - (V_{IF_{\text{max}}} + V_{IF_{\text{min}}})}{V_{IF_{\text{max}}} - V_{IF_{\text{min}}}} \right].$$  

Once the value of $\Delta \Phi(t)$ is obtained, it can be used for calculating the frequency stability. The 50 km fiber spool is placed in the temperature control box shown in Fig. 1, and the temperature is varied dramatically to allow $\Delta \omega(t)$ to change over a complete cycle, resulting in obtaining $V_{IF_{\text{max}}}$ and $V_{IF_{\text{min}}}$. Figure 3(a) shows the variation of $V_{IF}$ measured by the digital multimeter within a period of 62,000 s. It can be observed that the voltage changes only by $0.179 \text{ mV}$ during the measurement period. Figure 3(b) represents the inferred phase fluctuation based on the $V_{IF}$ variation. The black line represents the compensated link delay jitter, while the red line represents the jitter of the system in free transmission. From the graph, it can be seen that the link delay variation of the fiber link in the free transmission is approximately 600 ps, whereas in the compensated system, the transmission time delay of the signal changes by only about 1.15 ps during the testing time.

Phase noise of the frequency signal is an important indicator for measuring short-term frequency stability. We measured the phase noise of the rubidium atomic clock reference signal (100 MHz) and the compensated/uncompensated frequency signal (100 MHz) after a 50 km transmission using a signal and spectrum analyzer. The results are shown in Fig. 4(a). The difference between the red and black lines can be used to evaluate the degradation of phase noise caused by environmental influences during fiber link transmission. It is mainly distributed...
nearly 3 orders of magnitude, reaching 6.55\times10^{-18} after a measurement time of 56,737 s. This is because the designed analog DML, when powered at the LS and RS, reduces the DML linewidth. Narrower linewidth results in higher frequency stability, lower noise, and increased coherence, thereby improving the performance of the phase-stable transmission system. Based on the measured time delay fluctuation $\Phi(t)$ during the stability testing process, the average value $\mu$ was calculated using the following formula:

$$\sigma = \sqrt{\frac{\sum_{i=1}^{n} (\Phi_i - \mu)^2}{n}}.$$  

By substituting the measured samples of $\Phi(t)$ into the formula, the frequency stability accuracy of the transmission system can be calculated. The calculated stability accuracy of the system is 0.04 ps. Although there is a slight decrease in frequency stability due to temperature-induced noise, it still reaches the level of $10^{-18}$, indicating that the system is capable of mitigating delay fluctuations caused by temperature variations within the corresponding range, using the formula

$$\delta = KLT.$$  

The delay fluctuations caused by temperature disturbances in the fiber link can be measured in a phase-stable transmission system. Given the average temperature coefficient of the fiber, $K$, as 35.1 ps/(km °C), the transmission link distance, $L$, as 50 km, and the temperature variation range, $T$, as 9.63° C, the value of $\delta$ is calculated to be 17.55 ns, which represents the phase compensation range of the stable transmission system as tens of nanoseconds. More importantly, after a 10 s latency, the stability $\sigma(\tau)$ of the transmission system is inversely proportional to the running time $1/\tau$, showing a typical stability curve of a phase-locked loop. The short-term stability of the transmission system is not significantly affected by the inclusion of temperature variations, remaining at the level of $10^{-14}$, indicating that temperature variations mainly affect long-term stability.

4. Conclusions

In this paper, we proposed a two-section analog DML based on REC technology, which achieves an output power exceeding 14 mW and a modulation bandwidth of up to 18 GHz. We applied this laser to a phase-stable transmission system. The experimental results demonstrate that the RF signal in the X-band, after being transmitted through a 50 km fiber link, exhibits a stability of $1.62 \times 10^{-14}$ at 1 s and a stability of $9.17 \times 10^{-18}$ at 10^4 s for a 100 MHz RF signal when the RS is not powered. When the RS is powered, the stability can be optimized to $6.96 \times 10^{-18}$ at $10^4$ s. Even with a temperature variation of approximately 10°C introduced to the transmission link within 8 h, the fiber transmission stability is still maintained within the range of $10^{-14}$ and $10^{-18}$, with average times of 1 s and 86,050 s, respectively. This proves that the system has excellent resistance to temperature disturbances and a wide phase compensation range.
By optimizing the link structure, especially in overcoming backward Rayleigh scattering, and combined with REC technology to improve the slope efficiency of a DFB laser, further improvement in the transmission stability of frequency signals can be achieved. Efforts are under way to optimize the operation of the phase-stable transmission system; the results will be published in a separate paper.

Acknowledgements

This work was supported by the National Key R&D Program of China (No. 2020YFB2205804), the National Natural Science Foundation of China (Nos. 62273355, 61975075, 61975076, and 62004094), the Natural Science Foundation of Jiangsu Province of China (No. BK20200334), and the Jiangsu Science and Technology Project (No. BE2017003-2).

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