# Serrated periodic electrode for high energy efficiency and large bandwidth acousto－optic modulators 

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#### Abstract

In an acousto－optic modulator，the electrode shape plays an important role in performance，since it affects the distribution of the acoustic field．The acousto－optic modulator based on the conventional rectangular electrode has the problems of low energy efficiency and small modulation bandwidth due to an imperfect acoustic field．In this paper，a new serrated periodic electrode has been proposed for using acousto－optic modulator transducers．The proposed electrode has the following advantages．By using serrated periodic electrodes to suppress the sidelobes，the collimation of the acoustic field in the direction perpendicular to the light incidence is improved．This makes the acousto－optic modulator have a stable dif－ fraction efficiency fluctuation and high energy efficiency．In addition，the electrode has a large divergence angle in the direction of light incidence，so a large bandwidth can be obtained．The simulations and experiments demonstrate that the serrated periodic electrode has an increased bandwidth and high energy efficiency．


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## 1．Introduction

The acousto－optic modulator（AOM）is a device that controls the power of a laser beam by means of an electrically driven sig－ nal that is based on the acousto－optic effect ${ }^{[1,2]}$ ．The acousto－ optic effect is generated in acousto－optic crystals．Elastic strain is generated by sound waves through an acousto－optical crystals， causing the refractive index of the medium to change．When the light wave through the medium is disturbed by the sound waves， the diffraction phenomenon will occur．Benefiting from the mechanism of the acousto－optic effect，the AOM has the advan－ tages of small size，low power consumption，and fast rising time， which have been widely applied to the fields of laser communi－ cation ${ }^{[3]}$ ，laser measurement ${ }^{[4]}$ ，and fiber－optic sensors ${ }^{[5]}$ ．

In these application areas，power consumption and band－ width are important indicators of acousto－optic modulation devices．Ultimately，these are closely related to diffraction effi－ ciency．The acoustic beam is an important factor affecting the diffraction efficiency of AOM，which is generated by the elec－ trodes on the transducer through the inverse piezoelectric effect． Nowadays，most of the electrodes on AOM transducers are
rectangular．From the spectral analysis，the rectangular electrode produces more sidelobes；this represents a high degree of diver－ gence of the sound beam．This results in lower AOM energy efficiency using rectangular electrodes．In addition，small band－ width was generated by rectangular electrodes．Olbrish et al． investigated the effect of different geometries of the electrodes on the suppression of the sidelobes of the acousto field ${ }^{[6]}$ ． From the spectral analysis，the change of the shape of the elec－ trode can suppress the sidelobes of the acoustic field and concen－ trate the acoustic beam，which in turn improves the AOM diffraction efficiency．Wachman et al．proposed a side－ dithered pseudo－random electrode that can effectively reduce the sidelobes and improve the homogeneity of the sound field ${ }^{[7]}$ ． Wu et al．theoretically analyzed the acoustic near－field distribu－ tion characteristics of rectangular，diamond，and hexagonal shapes ${ }^{[8]}$ ．Hexagonal electrodes have the most uniform sound field distribution for good performance．These efforts are essen－ tial to improve the performance of AOM devices．

In this paper，a serrated periodic electrode is proposed．In the direction of vertical light incidence，the acoustic field produced by the serrated periodic electrode is more collimated，which
makes less energy escape from the main sound beam and can reduce AOM power consumption. In the direction of light incidence, the divergence angle of the acoustic wave is large due to serrated edge diffraction of serrated periodic electrodes. This makes the AOM bandwidth larger.

Simulation and experimental results show that serrated periodic electrodes have the advantages of high energy efficiency and large bandwidth compared to conventional rectangular electrodes. Under certain experimental conditions, the power consumption of AOM with serrated periodic electrodes can be reduced by $40 \%$ and the bandwidth increased by $31 \%$ compared to the conventional rectangular electrode. This research helps to reduce the power consumption of AOMs and other acoustooptic devices and to increase their bandwidth.

## 2. Approach

### 2.1. Analysis of rectangular and conventional apodization electrode

The AOM is an acousto-optic device that converts electrical signals into optical signals based on acousto-optic interactions ${ }^{[9]}$. It consists of an ultrasonic transducer, an acousto-optic crystal, and an acoustic energy absorption layer, as shown in Fig. 1. The ultrasonic transducer is the component that emits sound waves and consists of three parts: a top electrode, a piezoelectric crystal, and a bottom electrode. Under a high-frequency AC voltage between the top and bottom electrodes, the piezoelectric crystal vibrates at high frequencies to produce ultrasound. The shape and position of the electrodes determine the range of vibration of the piezoelectric crystal and subsequently the distribution of the acoustic field in the acousto-optic crystal.

The efficiency of the acousto-optical interaction is mainly limited by the acoustic field in the acousto-optical crystal ${ }^{[8]}$. The transducer plays a decisive role in the distribution of the acoustic field. The electrodes of the transducer determine the shape of the sound beam. To improve the acoustic field distribution by adjusting the electrode shape, the acoustic field distribution of the conventional rectangular electrode was calculated and analyzed for its deficiencies ${ }^{[10]}$. A typical AOM is used as the source of the simulation parameters ${ }^{[9]}$. The length of the


Fig. 1. The structure of the AOM.


Fig. 2. (a) Rectangular superimposed and normalized sound field distribution; (b) distribution of the acoustical field along the $z$ axis.
electrodes is 29 mm and the height is 1.5 mm . The entire measured acoustic field range is $29 \mathrm{~cm} \times 5 \mathrm{~cm} \times 12 \mathrm{~cm}$, and the central drive frequency is 80 MHz . The wavelength of the sound wave propagating in the crystal is $71.8 \mu \mathrm{~m}$. If boundary discretization coarser than $\lambda / 2$ is employed, the resulting acoustic field would be distorted because of spatial aliasing ${ }^{[11-13]}$. For simplicity, we set the sampling spacing to $25 \mu \mathrm{~m}$. As shown in Fig. 2(a), the sound pressure at each sampling plane along the direction of light incidence ( $z$ axis) is superimposed and normalized to obtain the propagation trend of the sound wave along the plane perpendicular to the direction of light incidence. The incident light undergoes Bragg diffraction in the main lobe region of the acoustic wave. However, a portion of the acoustic wave deviates from the main region and does not participate in the acousto-optical interaction, as shown in Fig. 2(b), which reduces the acoustic energy efficiency of the acousto-optical device.

Spectrum can be used to analyze the directional distribution of the acoustic beam at rectangular electrodes ${ }^{[14,15]}$. As shown in Fig. 3(a), according to the angular spectrum theory, the acoustic


Fig. 3. (a) Schematic diagram for analyzing the direction of sound waves using the spectrum; (b) Fourier transform of a rectangular electrode; (c) Fourier transform of a diamond electrode; (d) Fourier transform of a Gaussian electrode.


Fig. 4. (a) Acousto-optical interaction length of the diamond electrode; (b) acousto-optical interaction length of the Gaussian electrode.
waves generated by different electrodes can all be expressed as a superposition of plane waves in different directions. And the intensity of the acoustic waves in different directions can be analyzed by analyzing the frequency spectrum of the acoustic waves after Fourier transformation,

$$
\begin{equation*}
F[h(x)]=H(f)=\int h(x) e^{-j 2 \pi f x} \mathrm{~d} x . \tag{1}
\end{equation*}
$$

The rectangular electrode in one dimension can be represented as a rectangular window, whose spectrum is a sincsquared function. The sinc function has several significant side flaps, which can explain the divergence of the acoustic beam from the rectangular electrode. In the study of acousto-optical devices, apodization electrodes can be used to reduce the acoustic beam in other directions and improve the collimation of the acoustic beam ${ }^{[16-18]}$. As shown in Figs. 3(c) and 3(d), diamond and Gaussian electrode shapes have a high suppression of sidelobes in the spectrum. However, the AOM based on diamond and Gaussian electrodes does not modulate the incident light uniformly. In an AOM, the width of the incident light is slightly smaller than the width of the main sound beam to ensure that the entire beam is involved in the acousto-optic interaction. Ideally, the length of any part of the beam involved in the acousto-optical interaction should be equal. The area of the acoustic beam is mainly distributed directly above the electrode area. As shown in Fig. 4, the acousto-optical interaction length of marginal incident light is much shorter than that of the center incident light, which results in an uneven intensity of the diffracted beam.

### 2.2. Serrated periodic electrode

In conjunction with the analysis of the advantages and disadvantages of rectangular and conventional apodization electrode in


Fig. 5. (a) Simulation size of serrated periodic electrode (in mm); (b) Fourier transform of the serrated periodic electrode.


Fig. 6. Acousto-optical interaction length of the serrated periodic electrode.

Section 2.A, a serrated periodic electrode is proposed. First, the serrated periodic electrode inherits the advantages of the variable trace electrode and improves the collimation of the acoustic wave perpendicular to the direction of light incidence. As shown in Fig. 5(b), the sidelobes are suppressed in the spectrum of the serrated periodic electrodes.

Second, as shown in Fig. 6, the serrated periodic electrodes extend the acousto-optical interaction length of marginal incident light. In addition, the acoustic waves emitted by this serrated edge fill the acoustic-free area between the serrations along the $x$ axis, resulting in a longer acousto-optical interaction area for the marginal incident light.

Third, the serrated electrode edges increase the divergence angle of the sound waves in the vertical light incidence direction, which enhances the bandwidth of the AOM. As shown in Eq. (2), divergence angle tends to be negatively correlated with the length of the electrode structure,

$$
\begin{equation*}
\theta=\frac{\lambda}{2 L}, \tag{2}
\end{equation*}
$$

where $\theta$ is the divergence angle of the acoustic beam, $\lambda$ is the wavelength, and $L$ is the length of the structure. Compared to a rectangular electrode, the length of serration in the serrated electrode is shorter, resulting in a more diffuse sound wave.

In addition, the serrated periodic electrode has a greater impedance than a rectangular shape of the same size due to the smaller area. As a result, the serrated electrode has a larger $A C$ voltage at the same input power.


Fig. 7. (a) Phase distribution at sawtooth period electrode (inner width 0.5 mm ); (b) phase distribution at sawtooth period electrode (inner width 0.8 mm ); (c) phase distribution at sawtooth period electrode (inner width 1.3 mm ); (d) phase distribution at rectangular electrode.

## 3. Simulation

Simulation results are presented to verify that the acoustic beam emitted by the serrated periodic electrode is collimated in the direction perpendicular to the incidence of light and has a large divergence angle in the direction of light incidence. To clearly demonstrate the effect, we have changed the internal width of the serrated periodic electrodes, as shown in Fig. 7. The calculated acoustic field distribution is superimposed along the $y$ axis, and the phase distribution is taken out. The simulation results


Fig. 8. (a) Amplitude distribution of rectangular electrode; (b) serrated periodic electrode (inner width: 1.3 mm ); (c) serrated periodic electrode (inner width: 0.8 mm ); (d) serrated periodic electrode (inner width: 0.5 mm ).
show that the waveform of the acoustic wave gradually changes from a plane wave to a wavy waveform as $h$ decreases. The advantage of a wavy waveform is that it produces a large angle of divergence of the acoustic wave compared to a plane wave, which facilitates the increase in bandwidth.

On the other hand, we calculated the amplitude distribution in the direction of vertical light incidence for serrated periodic electrodes with different internal widths. The calculated acoustic field distribution is superimposed along the $z$ axis, and its amplitude distribution is taken out. As shown in Fig. 8, as the internal width of the serrated electrode decreases, the sidelobes of the sound field intercept become smaller. This means that the acoustic beam is collimated, and there is no excess escaping energy. This is effective in reducing power consumption when acousto-optical diffraction occurs.

## 4. Experiment

### 4.1. Equipment and materials

We conduct comparative experiment on our AOMs with serrated periodic and rectangular electrodes to verify the effectiveness of the serrated periodic electrode. To obtain AOMs for experiment, $0^{\circ} X$ quartz crystal is used as the AO medium, $36^{\circ} \mathrm{YLiNbO}_{3}$ is used as the piezoelectric material to excite longitudinal acoustic wave, and 1064 nm antireflective film is plated on the light pass surfaces. The opposite side of the transducer is designed as an inclined plane for multiple reflections to absorb and dissipate heat. The fabricated AOM is shown in Fig. 9, and the effective light incident area is about 3.5 mm away from the transducer. In order to improve the measurement accuracy, the five-dimensional controllable motor scanning platform is used in the test process to avoid the errors caused by human measurement factors (see Fig. 10). The test platform can collect the optical power data in real time and calculate the average value synchronously to reduce the measurement errors. A thermoelectric cooler (TEC) radiator is installed under the AOM fixture to reduce the interference of the temperature gradient field to the supersonic field in AOM.

As shown in Fig. 11, the length $L$ and width $H$ of the electrode are 29 mm and 1.5 mm for the AOM. And, three control groups with different inner width are designed for serrated periodic electrodes, including $h=0.5 \mathrm{~mm}, 0.8 \mathrm{~mm}, 1.3 \mathrm{~mm}$ and $w=0.5 \mathrm{~mm}$. The center frequency of the AOM is 80 MHz ,


Fig. 9. Typical AOM configuration with serrated periodic electrode.


Fig. 10. Five-dimensional controllable motor scanning test platform.


Fig. 11. Serrated periodic electrodes with different inner widths.
a solid-state 1064 nm laser with a beam diameter of 1.2 mm is used, and the beam divergence angle is about 1 mad .

### 4.2. Experiment and analysis

In order to verify the effectiveness of serrated periodic electrodes, we compare and analyze the samples from three aspects, including sound energy efficiency, acoustic field collimation, and bandwidth.

First, we experimentally compare the sound energy efficiency of serrated periodic electrodes and rectangular electrodes. The sound energy efficiency is measured when the incident light is fixed 1.5 mm away from the transducer. As shown in Fig. 12, under the same experimental conditions, we obtained the diffraction efficiency curves of AOMs with different electrode sizes under varying RF powers. It can be seen from the test efficiency curves that the serrated periodic electrodes can obtain higher efficiency at lower power. The diffraction efficiency peaks of serrated periodic electrodes $h=0.5 \mathrm{~mm}, 0.8 \mathrm{~mm}, 1.3 \mathrm{~mm}$ appear at $14 \mathrm{~W}, 16 \mathrm{~W}$, and 20 W , respectively, while the diffraction efficiency peak of the rectangular electrode is 24 W . Under this experimental conditions, the power consumption of AOM with serrated periodic electrodes can be reduced by $40 \%$ compared to


Fig. 12. Diffraction efficiency curves of serrated and rectangular electrodes.
the conventional rectangular electrode. This is related to the effective sound field width of the AOM. According to the diffraction efficiency relation,

$$
\begin{equation*}
\eta=\sin ^{2}\left(\frac{\pi}{\lambda} \sqrt{\frac{M_{2} L P_{a}}{2 H}}\right) \tag{3}
\end{equation*}
$$

where $M_{2}$ is the acousto-optic merit coefficients of the medium, and $P_{a}$ is the injected RF power. The diffraction efficiency is inversely proportional to the electrode width $H$. The electrode width $H$ is the macroscopic manifestation of the effective vibration source of the piezoelectric transducer. When the $H$ of the serrated periodic electrodes decreases, the sidelobe of the superposition area of the acoustic field in the acousto-optic medium decreases and the energy is more concentrated. The effective acoustic field width is more concentrated in a certain region, thus showing the advance of the peak diffraction efficiency.

Then, a comparative verification of the acoustic field collimation of the serrated electrode and the rectangular electrode was carried out. A digital holographic interferometer was used to photograph the acoustic field inside the acousto-optical crystal along the direction of the vertical light incidence. As shown in Fig. 13, the serrated periodic electrode has the significant effect of suppressing the acoustic beam outside the main peak.

Also, we measured the diffraction efficiency for different incident light positions along the $x$ axis to verify the collimation of the acoustic beam. From the results of the efficiency curve in Fig. 12, the 18 W RF power is selected for testing when both the serrated periodic electrodes and the rectangular electrode have better diffraction efficiency. We scanned along the $x$ axis


Fig. 13. (a) Acoustic field distribution inside an acousto-optical crystal with rectangular electrode; (b) acoustic field distribution inside an acousto-optical crystal with serrated periodic electrode (inner width: 0.5 mm ).


Fig. 14. Incident position of the light beam.
on the scanning test platform. The distance between the tangent of the incident beam parallel to the transducer and the transducer is set as $D$, and the value of $D$ is $0-3.5 \mathrm{~mm}$ (see Fig. 14). The experimental results of diffracted light efficiency at different sound field propagation depths are shown in Fig. 15. From the comparison of the efficiency curves scanned along the $x$ axis, it can be seen that the flatness of the serrated periodic electrodes is better than that of the rectangular electrode while keeping the overall length and width parameters of the electrode unchanged, and as the inner width $h$ decreases, the curve becomes smoother. The range of scanning diffraction efficiency of the serrated periodic electrodes at $h=0.5 \mathrm{~mm}$, 0.8 mm , and 1.3 mm is $4.38 \%, 5.83 \%$, and $8.95 \%$, respectively, while the range of scanning diffraction efficiency of the rectangular electrode is $11.74 \%$. The experimental results are in agreement with the simulation results (see Fig. 8).

Finally, the comparative verification of the efficiency bandwidth of the serrated periodic electrodes, hexagonal electrodes, and the rectangular electrode is carried out. With a fixed point of action and RF power, the diffraction efficiency of the AOM varies with the RF frequency. The corresponding frequency range from the peak to half is defined as the 3 dB efficiency bandwidth. According to the previous results (see Figs. 12 and 15), a certain propagation depth and RF power when both the serrated periodic electrodes and the rectangular electrode have better diffraction efficiencies are used as the preconditions for the test; that is, the propagation depth is 1.5 mm , and the RF power is 15 W . The efficiency bandwidth tests were performed


Fig. 15. Diffracted light efficiency curves under different incident positions of the beam.


Fig. 16. 3 dB efficiency bandwidth curves for different electrodes.
on sawtooth electrodes and rectangles using the deflector test method; the resulting experimental results are as shown in Fig. 16. The deflector test method shows that the efficiency bandwidths of the serrated periodic electrodes $h=0.5 \mathrm{~mm}$, 0.8 mm , and 1.3 mm are $38 \mathrm{MHz}, 34 \mathrm{MHz}$, and 32 MHz , respectively, while the efficiency bandwidths of hexagonal electrodes and rectangular electrodes are 33 MHz and 29 MHz , respectively. Under these experimental conditions, the bandwidth of the AOM based on serrated periodic electrodes is increased by $31 \%$ compared to rectangular electrodes and by $15 \%$ compared to hexagonal electrodes. Experimental results proved that, as the inner width of the serrated periodic electrode decreases, the resulting acoustic wave has a greater angle of dispersion in the direction of light propagation, thereby increasing the bandwidth of the device.

## 5. Conclusion

In this paper, we propose a serrated periodic electrode that is applied to an AOM. The serrated periodic electrode inherits the advantages of the apodization electrode and enhances the collimation of the acoustic beam in the direction of vertical light incidence, and it improves the defect that occurs when the acousto-optical interaction length of the apodization electrode is not uniform. The serrated periodic electrode has a larger bandwidth due to its serrated edge diffraction. The simulation and experimental results demonstrate the high energy efficiency and large bandwidth of the serrated periodic electrode by comparing it with the conventional rectangular electrode. In future work, we will compare the serrated periodic electrodes with other apodization electrodes to refine our study. This research will help to reduce power consumption and increase the bandwidth of AOMs and other acousto-optical devices.

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