Sidelobe suppression for coherent beam combining with laser beams placed along a Fermat spiral

Yang Gao (高旸), Jiali Liao (廖家莉), Jun Xu (徐军), and Zhanrong Zhou (周战荣)

1 Xi’an Research Institute of High Technology, Xi’an 710025, China
2 School of Physics and Optoelectronic Engineering, Xidian University, Xi’an 710071, China
3 State Key Laboratory of Pulsed Power Laser Technology, Hefei 230037, China

*Corresponding author: gaoyang_nudt@126.com
**Corresponding author: zhouzhou78@163.com
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We proposed an aperiodic laser beam distribution, in which the laser beams are placed along a Fermat spiral, to suppress the sidelobe power in the coherent beam combining. Owing to the changed distances between two consecutive beams, the conditions of the sidelobe suppression are naturally satisfied. The Fermat spiral array was demonstrated to achieve a better sidelobe suppression than the periodic arrays, and the effects of various factors on the sidelobe suppression were analyzed numerically. Experiments were carried out to verify the sidelobe suppression by different Fermat spiral arrays, and the results matched well with the simulations.

Keywords: coherent beam combining; sidelobe suppression; Fermat spiral; intensity distribution.
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1. Introduction

Because of the influence of heat damage, nonlinear effect, mode instability, and brightness of the pump source, the output power of a single laser is limited [1–3]. Coherent beam combining (CBC) of multiple laser modules is an effective solution to obtain higher output power and good beam quality simultaneously [4,5]. When the optical phase and optical axes of each laser beam are controlled, the whole laser array can be regarded as a single laser with a large aperture [6–8]. Although the beam quality of this method is not as good as that of a single laser module, it shows superiority with weaker heat effect and lower cost. In addition, CBC has potential applications in free-space optical communication, optical manipulation, and so on [9,10].

In most CBC systems, the apertures of the laser beams are configured as the hexagon array, the square array, and their derivative arrays [11–13]. In these tiled-aperture geometries, the laser beams are uniformly distributed in space and have a constant spatial period. As a result, the main lobe of the coherent combining beam is surrounded by obvious sidelobes, which cannot be eliminated fundamentally. Sidelobe suppression is an important issue, not only in CBC systems, but also in many other fields of research, such as super-oscillation in optics, which is one kind of destructive interference of light with different frequencies at some points at small intervals [14–16]. Increasing the number of the laser beams is a promising approach to improve the output power of the main lobe [17]. However, the large number of laser beams brings about the difficulty for the phase control [18,19]. It has been proven that the Fermat spiral (FS) is a useful element pattern for synthetic aperture devices in radars and acoustics [20–22]. However, the FS has never been used for CBC of laser beams, at least from our search.

In this Letter, we proposed an aperiodic FS tiled-aperture geometry for laser beams to suppress the sidelobe power in the CBC. This Letter is organized as follows. First, FS distribution of the laser beams is introduced, comparing the hexagon array and the square array. Second, the far-field intensity distribution is analyzed by the Kirchhoff scalar diffraction theory, and the factors that affect the sidelobe suppression are discussed in detail, including the number of the laser beams, the distance parameter, the laser beam diameter, and the fill factor. Additionally, the intensity distributions obtained by different designed arrays are investigated numerically. Finally, experiments were carried out to demonstrate the effects of the FS beam array on the sidelobe suppression in CBC.

2. Design and Principle

In this study, the laser beams in the CBC optical system are arranged along an FS. Thus, the distribution of the laser beam centers can be described by
where $r_i$ is the distance of the $i$th laser beam center to the spiral center, $\theta_i$ is the angular displacement, and $s$ and $\beta$ control the distance and the angular displacement between the laser beams along the spiral, respectively. In this Letter, $2\pi\beta$ is equal to 137.5°; thus, the laser array is a spiral array with uniform spatial density[23].

We assume that all of the laser beams have the same circular aperture, and the intensity of each beam follows Gaussian distribution. Thus, the optical field distribution of the laser beam on the laser emission plane is given by

$$U = \sum_{i=1}^{n} A_i(\vec{r}) \times \text{circ}(\vec{r}),$$  \hspace{1cm} (3)

where $n$ is the total number of laser beams, $A_i(\vec{r})$ and $\text{circ}(\vec{r})$ are the optical field distribution and the aperture of the $i$th laser beam, respectively, and can be described by

$$A_i(\vec{r}) = A_0 \exp \left( -\frac{|\vec{r} - \vec{r}_i|^2}{w_0^2} \right),$$  \hspace{1cm} (4)

$$\text{circ}(\vec{r}) = \begin{cases} 1, & \text{if } |\vec{r} - \vec{r}_i|^2 \leq a^2/4 \\ 0, & \text{if } |\vec{r} - \vec{r}_i|^2 > a^2/4 \end{cases},$$  \hspace{1cm} (5)

where $A_0$ and $w_0$ are constants in the Gaussian function, $a$ represents the common diameter of all the apertures, and $\vec{r}_i$ is the center coordinate of the $i$th aperture and can be determined by Eqs. (1) and (2). Here, we assume that the center of the $i$th aperture and the center of the $i$th laser beam are in the same position.

The laser array is placed in the $xOy$ plane, and the light propagates along the $z$ direction. According to the Kirchhoff scalar diffraction theory, the far-field optical distribution is given by

$$U(f_x,f_y) = \frac{e^{ikz}}{j\lambda z} \exp \left[\frac{jk}{2z} (x^2 + y^2)\right] F\{U(x,y)\}_{f_x \rightarrow \frac{f_x}{2\pi}, f_y \rightarrow \frac{f_y}{2\pi}},$$  \hspace{1cm} (6)

where $\lambda$ is the wavelength, $k = 2\pi/\lambda$ is the wave vector, $F\{U(x,y)\}$ denotes the Fourier transform, $z$ is the light propagation distance, which should meet the far-field diffraction condition $[z \gg k \times D^2/8, D$ is the diameter of the laser beam array], and $(x, y)$ and $(f_x, f_y)$ denote the coordinates in the spatial and frequency domains, respectively.

Based on the Kirchhoff scalar diffraction theory, the far-field intensity distributions of different laser arrays were calculated, and the results are shown in Fig. 1. It is clear that the sidelobes shown in Fig. 1(f) are much weaker than the sidelobes shown in Figs. 1(d) and 1(e). It denotes that the FS beam array is a promising approach for the suppression of the sidelobe power in the CBC system, compared to the hexagon array and the square array.

3. Analysis

In an optical CBC system, there are always sidelobes in the interference pattern, but the fraction of power encircled in those sidelobes can be significantly decreased by making proper choices. In this section, we analyze the impact of different parameters on the interference pattern lobe distribution, for example, the beam number, beam diameter, beam spacing, and filling factor. In addition, the intensity distributions obtained by different beam arrays are investigated and compared at the end of this section.

From Eqs. (1) and (2), the distance between two consecutive laser beams is set according to the FS, which naturally satisfies the condition of sidelobe suppression. As a result, the sidelobes were suppressed by the FS beam array significantly, in contrast to the periodic arrays, such as the hexagon array and the square array. The far-field intensity distributions obtained by the FS beam arrays with different numbers of laser beams are shown in Figs. 2(a)–2(h). Specifically, the total number of laser beams $n$ is equal to 7, 19, 37, 61, 91, 127, 169, and 217, corresponding to the beam numbers of the hexagon arrays with the orders of 2, 3, 4, 5, 6, 7, 8, and 9, respectively. The intensity variations along the $y$ axis are shown in Fig. 2(i), corresponding to Figs. 2(a)–2(h). In this simulation, the diameter of the sub-aperture is 1 mm, and the distance between the tiled-aperture and the interference pattern is 850 m. It is found that the fraction of power encircled in those sidelobes can be significantly decreased by making the proper choice of laser beam numbers. The larger the number of the laser beams, the weaker the sidelobe will be. It is shown in Fig. 2(i) that the diameter of the main lobe decreases with the increase of the beam number, corresponding to the predicted results via the Kirchhoff scalar diffraction theory.

The main lobe intensity $I_0$ and the peak intensity ratio $\eta$ were calculated to evaluate the effects of the sidelobe suppression, and they are defined as

$$\eta = \frac{I_{\text{main}}}{I_{\text{side}}},$$

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The main lobe intensity $I_0$ and the peak intensity ratio $\eta$ were calculated to evaluate the effects of the sidelobe suppression, and they are defined as

$$\eta = \frac{I_{\text{main}}}{I_{\text{side}}},$$
where $I_{\text{main}}$ and $I_{\text{total}}$ denote the intensity of the main lobe and the total intensity of the beam, and $I_{\text{main-max}}$ and $I_{\text{side-max}}$ denote the maximum intensities of the main lobe and the sidelobe. The diameter of the main lobe was estimated to be the diameter of the Airy disk. In this case, the main lobe intensity represents the ratio of the main lobe intensity to the total intensity, and the peak intensity ratio represents the ratio of the maximum intensity of the main lobe to the maximum intensity of the sidelobe. The bigger $I_0$ and $\eta$ are, the better the effect of the sidelobe suppression will be.

The effects of the diameter of the laser beam on the sidelobe suppression with a constant $s$ were investigated numerically, and the results are shown in Fig. 3. The main lobe intensity is coherently combined by all of the laser beams; thus, it increases steadily with the laser beam diameter, as shown in Fig. 3(a). Due to the aperiodicity of the FS array, the sidelobe power decreases with the increase of the laser beam diameter, as shown in Fig. 3(b). When the number of laser beams is very small, the peak intensity ratio does not increase significantly with the laser beam diameter, as shown with the red solid line in Fig. 3(b). On the contrary, the peak intensity ratio increases obviously when $n$ is equal to 19 and 37, and the laser beam diameter is larger than 40 pixels. Particularly, the main lobe intensity is 0.68, and the maximum value of the main lobe intensity is 54 times more than that of the sidelobe intensity, with the laser beam number of 37 and the laser beam diameter of 45 pixels. It denotes that the sidelobe power can be suppressed by the FS array, without the large-scale array, compared to the hexagon array and the square array.

The fill factor is defined as the percentage of the sum of the sub-aperture areas to the area of the array circumcircle. The fill factor increases with the increase of the laser beam diameter and the decrease of the distance parameter $s$. We investigated the effect of the parameter $s$ on the sidelobe power, the results are shown in Fig. 4, and the simulation results match well with those shown in Fig. 3.

We further investigated the effect of the fill factor on the sidelobe suppression. From Eqs. (1) and (2), it is found that the fill factor is a constant when the ratio of the distance parameter $s$ to the laser beam diameter is constant. We assume that the distance parameter $s$ is two times the laser beam diameter, and the corresponding main lobe intensity and the peak intensity ratio are shown in Fig. 5. It is found that the main lobe intensity and the peak intensity ratio are almost unchanged when the fill factor remains constant, regardless of the distance parameter $s$. It is demonstrated that the fill factor is a primary factor on the sidelobe suppression for CBC, with the laser beams arranged as an FS array. It is a classical result, and everything goes as expected. In addition, it is also shown that the sidelobe can be further suppressed by the increase of the laser beam numbers.

Taking advantage of the rotation symmetry, the FS array matches well with the circular aperture of the optical system, compared to the hexagon array and the square array. Thus, the fill factor of the FS array is larger than those of the hexagon array and the square array.
array and the square array, with the same size of array circumference. As a result, the advantage of the FS array in sidelobe suppression should be considered. The fill factor and performance of the sidelobe suppression of three different arrays are investigated by simulation, and the results are shown in Fig. 6.

The fill factor of the FS array increases with the laser beam number, while that of the hexagon array and the square array decreases with the laser beam number, as shown in Fig. 6(a). It is demonstrated that the fill factor of the FS array is superior to that of the hexagon and square array. As verified in the analyses above, the sidelobe suppression is primarily determined by the fill factor of the laser array. Thus, the main lobe intensity and the peak intensity ratio of the FS array increase together with the fill factor, as shown in Figs. 6(b) and 6(c). Additionally, it is illustrated that the main lobe intensity and the peak intensity ratio of the FS array increase obviously, while those of the hexagon and square arrays change slightly. Here, the slight change is the result of the combined action of the fill factor and the laser beam numbers. It is also indicated that the beam quality can be improved by the FS array without changing the distance parameter (or spatial period), compared to the hexagon array and the square array.

4. Experiment

An optical system was set up to verify the performance of the FS array. As shown in Fig. 7, the optical system was composed of the laser, polarizing films, laser beam expanders, metal plate with through-holes, convex lens, optical filter, and CCD. The through-holes, which were arranged along the FS, were fabricated in a metal plate to generate the equivalent laser beam array in CBC. When the expanded laser beam with the diameter of several millimeters propagated through the metal plate, the FS beam array was generated. To observe the intensity distribution of the combining beam in a finite distance, a CCD was installed on the focus plane of the convex lens. The optical filter was placed in front of the CCD to filter out the stray light. Additionally, the polarizing films were used as power attenuators, which can feasibly control the laser beam intensity to avoid the overexposure on the CCD. The wavelength of the laser was 632.8 nm. The clear aperture and focal length of the convex lens were 100 mm and 400 mm, respectively. The through-holes on the metal plate were with the same diameter of 1 mm.

The combining beams of four different designed FS arrays were investigated in the experiments to verify the regularity of the intensity distribution analyzed in the above simulations. The fill factors of the FS arrays were not very high because of the limitation of the fabrication accuracy. The 2D intensity...
distribution of the combining beams, captured by the CCD, is shown in Figs. 8(a)–8(d). Figure 8(e) shows the one-dimensional (1D) intensity variations along the x axis, corresponding to Figs. 8(a)–8(d). The characteristics of the FS arrays and the image processing results are shown in Table 1.

As listed in Table 1, the fill factor of the FS array [Fig. 8(b)] is larger than that of the FS array [Fig. 8(a)]. In Table 1, it is demonstrated that the main lobe intensity and the peak intensity ratio of FS array [Fig. 8(b)] are larger than those of FS array [Fig. 8(a)]. These results match well with the simulation results and are confirmed again by the results of FS arrays [Figs. 8(c) and 8(d)] in Table 1. Meanwhile, the main lobe intensity and the peak intensity ratio of FS arrays [Figs. 8(a) and 8(c)] in Table 1 are nearly the same, because the two FS arrays are with the same fill factor. We found the same conclusion from the results of FS arrays [Figs. 8(b) and 8(d)] in Table 1. Additionally, it is illustrated that the increase of the total number of the laser beams also leads to sidelobe suppression. All of the experimental values are smaller than the simulation results; it is caused by the inhomogeneity of the laser array power and can be improved by mode modulation in further experiments.

Table 1. The Characteristics and the Image Processing Results.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Fig. 8(a)</th>
<th>Fig. 8(b)</th>
<th>Fig. 8(c)</th>
<th>Fig. 8(d)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Laser beam number</td>
<td>24</td>
<td>42</td>
<td>92</td>
<td>168</td>
</tr>
<tr>
<td>Diameter of the array (mm)</td>
<td>21</td>
<td>21</td>
<td>44</td>
<td>44</td>
</tr>
<tr>
<td>Fill factor</td>
<td>5%</td>
<td>9%</td>
<td>5%</td>
<td>9%</td>
</tr>
<tr>
<td>Main lobe intensity (in experiment)</td>
<td>4%</td>
<td>9%</td>
<td>3%</td>
<td>9%</td>
</tr>
<tr>
<td>Main lobe intensity (in simulation)</td>
<td>6%</td>
<td>13%</td>
<td>7%</td>
<td>17%</td>
</tr>
<tr>
<td>Peak intensity ratio (in experiment)</td>
<td>2</td>
<td>3</td>
<td>2</td>
<td>3</td>
</tr>
<tr>
<td>Peak intensity ratio (in simulation)</td>
<td>4</td>
<td>9</td>
<td>9</td>
<td>21</td>
</tr>
</tbody>
</table>

Meanwhile, the fabrication error, which leads to the phase error, may be another factor caused by the mismatch. Furthermore, the mismatch is amplified by the total number of laser beams.

5. Conclusion

In this Letter, we proposed an aperiodic distribution for the laser array to suppress the sidelobe power in the CBC. All of the laser beams are placed along an FS; thus, the coherent condition of the sidelobe is not satisfied. Therefore, more energy is concentrated in the main lobe. Taking advantage of the rotation symmetry, the fill factor of the FS array is larger than those of the periodic arrays; thus, the sidelobe is further suppressed. Numerical simulations indicate that the sidelobes are effectively suppressed by the FS array, and the fill factor and laser beam number are the primary factors of sidelobe suppression. The experiments were also carried out to verify the performance of the FS array, and the results agreed well with the simulation results. The FS array provides a feasible approach for the beam arrangement in the CBC system to achieve high combined beam quality.

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