# Non－scanning，non－interferometric，three－dimensional optical profilometer with nanometer resolution 

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#### Abstract

A non－scanning，non－interferometric，three－dimensional（3D）optical profilometer based on geometric op－ tics，critical angle principle，and the use of a charge－coupled device（CCD）camera is presented．The surface profile of the test specimen can be transferred into the reflectance profile．The reflectance profile， obtained from a CCD，is the ratio of the intensity at the critical angle to the intensity obtained at the total internal reflection angle．The optical profilometer provides a sub－micron measuring range with nanometer resolution and can be used to measure roughness or surface defects in real time．


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Optical profilometers may be distinguished into two types：scanning and non－scanning types．Scanning profilometers have better axial resolution but spend much time in measuring．For three－dimensional（3D） surface profile measurement，scanning approaches such as confocal microscopy ${ }^{[1-3]}$ ，or near－field microscopy ${ }^{[4]}$ ， which have high axial and lateral resolutions for measur－ ing a small scanned area，are usually not used to mea－ sure a large surface profile．Non－scanning approaches such as the noninterferometric method ${ }^{[5,6]}$ ，interference microscopy ${ }^{[7-10]}$ ，and second－harmonic generation ${ }^{[11]}$ ， can measure a large surface field，but the surface height calculation based on the fringe analysis is more complex．

In this letter，a new non－scanning and non－ interferometric optical profilometer based on the critical angle method ${ }^{[12-14]}$ and the use of a charge－coupled de－ vice（CCD）camera is proposed．The algorithm of the critical angle method transforms the surface height into the reflectance ${ }^{[14]}$ ，and a CCD is used to measure the re－ flectance profile at the image plane．From the reflectance profile，two－dimensional（2D）and 3D electronic images may be obtained simultaneously．The profilometer is a useful and rapid approach for measuring a large surface profile（the whole area of the reflection beam）in one shot．The test area may be the whole size of the beam and is directly dependent on optical magnification and CCD size．In the current method，even large area mea－ surements can be obtained if the optical magnification is less or equal to one，and the incident angle or reflection times of the prism can be changed to adjust the measure－ ment resolution according to the user＇s need．

From Fig．1，the surface height between two points in an interval $\Delta x$ is given as

$$
\begin{equation*}
\Delta h=\Delta x \alpha \tag{1}
\end{equation*}
$$

where $\alpha$ is the height gradient in the $x$－direction，and the reflected light deflects at an angle $2 \alpha$ from the incident light．Let the deflected light be incident into a paral－ lelogram prism at the nearby critical angle．The light，
twice reflected in the prism as shown in Fig．2，has a re－ flectance given as $R_{\mathrm{s}}^{2}=R_{\mathrm{s} 2}$ ，where $R_{\mathrm{s}}$ is the reflectance of the s－polarized light after one reflection．The reflectance curve $R_{\mathrm{s} 2}$ versus the incident angle $\theta$ is shown in Fig． 3. Therefore，the reflectance is inversely proportional to the incident angle $\theta$ at the nearby critical angle．Let two ad－ jacent light rays be parallel and normally incident to two points of the specimen，respectively．If there is a small surface height between the two points，the deflection an－ gles are given as

$$
\begin{equation*}
2 \alpha_{1}=2 \mathrm{~d} h_{1} / \mathrm{d} x \tag{2}
\end{equation*}
$$

and

$$
\begin{equation*}
2 \alpha_{2}=2 \mathrm{~d} h_{2} / \mathrm{d} x \tag{3}
\end{equation*}
$$

respectively，and the deviation angles from the initial in－ cident angle are $\Delta \theta_{1}=2 \alpha_{1}$ and $\Delta \theta_{2}=2 \alpha_{2}$ ，respectively， where $\mathrm{d} h_{1} / \mathrm{d} x$ and $\mathrm{d} h_{2} / \mathrm{d} x$ are the slope of the points in the $x$－axis at $h\left(x_{1}\right)=h_{1}$ and $h\left(x_{2}\right)=h_{2}$ ，respectively．


Fig．1．Ray reflected from an incline plane．


Fig．2．Ray reflected twice in the parallelogram prism．


Fig. 3. Reflectance curve of $R_{\mathrm{s} 2}$ versus the incident angle $\theta$.
The initial incident angle $\theta_{0}$ is the angle at which the ray reflects from the first point on the $x$-axis and then incident into the prism. Thus, the reflectance difference $\Delta R_{\mathrm{s} 2}\left[\Delta R_{\mathrm{s} 2}=R_{\mathrm{s} 2}\left(\theta_{2}\right)-R_{\mathrm{s} 1}\left(\theta_{1}\right)\right]$ between the two angles is inversely proportional to the difference $\theta_{2}-\theta_{1}$ and the surface height $\Delta h=h_{2}-h_{1}$, where $\theta_{2}=\theta_{0}+\Delta \theta_{2}$ and $\theta_{1}=\theta_{0}+\Delta \theta_{1}$. The surface height is expressed as

$$
\begin{equation*}
\Delta h=\Delta R_{\mathrm{s} 2} \cdot M \tag{4}
\end{equation*}
$$

where $M$ is the transfer constant. The image system is afocal and consists of two lenses (O2 and L3), a polarized beam-splitter (PBS), and a CCD to increase optical magnification (Fig. 4). The optical transverse magnifiycation $M_{\mathrm{T}}$ is equal to the value of $f_{3} / f_{\mathrm{O} 2}$, where $f_{\mathrm{O} 2}$ and $f_{3}$ are the focal lengths of lenses O 2 and L 3 , respectively. The deviation angle $\Delta \theta$ decreases to the value of $2 \alpha / M_{\mathrm{T}}$. Thus, the transfer constant $M$ is given as

$$
\begin{equation*}
M=\frac{f_{3}}{2 m f_{\mathrm{O} 2}} \Delta x \tag{5}
\end{equation*}
$$

where $R_{\mathrm{s} 2}$ is the average slope, $m=\Delta R_{\mathrm{s} 2} / \Delta \theta$, is negative if $\alpha>0$. Therefore, the transfer constant is dependent on the optical magnification $M_{\mathrm{T}}$ and the slope of the reflectance $m$; i.e., $M<0$. From Eqs. (4) and (5), the surface height proportional to the reflectance and is given as

$$
\begin{equation*}
h(x, y)=\int \mathrm{d} h=\int M \mathrm{~d} R_{\mathrm{s} 2}=M R_{\mathrm{s} 2}(x, y)+h_{0} \tag{6}
\end{equation*}
$$

where $h_{0}$ is the initial height on the surface at the initial incident angle $\theta=\theta_{0}$.

The experimental setup is shown in Fig. 4, where a beam from a $\mathrm{He}-\mathrm{Ne}$ laser with a $632.8-\mathrm{nm}$ wavelength is incident to an isolator and then to a beam expander (consisting of an objective O1, a pinhole, and a lens L1), and a polarizer $\mathrm{P}\left(0^{\circ}\right)$. The transmission axis of the polarizer is parallel to the $x$-axis. The isolator is used to prevent the light from the optical system from returning to the laser. Thus, the light out of the polarizer $\left(\mathrm{P}\left(0^{\circ}\right)\right)$ is a p-polarized light. If a beam, whose polarization direction with respect to the slow or fast axis of a quarter-waveplate $\left(\mathrm{W}_{\lambda / 4}\right)$ is $45^{\circ}$, passes twice, the polarization is rotated $90^{\circ}$; i.e., the p-polarized light becomes an s-polarized light. For this reason, the polarization of the beam reflected from the test surface and passing the quarter-waveplate $\left(W_{\lambda / 4}\right)$ again becomes an
s-polarized light. It is then reflected by the PBS and is incident to the angular sensor (a parallelogram prism with a refractive index of 1.51509 ) at the nearby critical angle. The sensor transforms the deviation angle $\triangle \theta$ (due to the height gradient) into the reflectance variation $\Delta R_{\mathrm{s} 2}$. The s-polarized light is used because the reflectance slope of the s-polarization is more consistent than that of the p-polarization, making it convenient to calculate the average slope of reflectance. The image system consists of the lenses O2 and L3, PBS, and CCD. The CCD is located at the imaging plane and is used to catch the intensity profile of the image. Two incident angles (the nearby critical angle and the total internal reflection (TIR) angle) of the prism are set and used to catch two images with the CCD. The incident angle is adjusted and changed using a rotation stage (URS 100PP, Newport, USA) with an angular resolution of $2 \times 10^{-4}\left({ }^{\circ}\right)$. The reference and the test images are caught at the TIR and the nearby critical angle, respectively. The average reflectance of the reference and test images are set to 1.0 and 0.7 , respectively, and the initial angle $\theta_{0}$ is made equal to the angle at $R_{\mathrm{s} 2}=0.7$. In addition, to address the problem of image displacement due to the change in the incident angle from $\theta_{0}$ to TIR, the CCD is laterally translated at a corresponding distance to superpose all the identical points of the two images. The intensity ratios between the test and the reference images must be calculated at each image point. The reflectance profile is then obtained.
In the current experiment, the specimen, a mirror with $\lambda / 20$ roughness, is tested, and an atomic force microscope (AFM) is used to test and verify our method. The transverse magnification $M_{\mathrm{T}}$ is equal to 11.8 and the CCD size is $1024 \times 768$ (pixels). The pixel size is $4.65 \times 4.65$ $(\mu \mathrm{m})$ and $M=-210 \mathrm{~nm}$. Thus, the lateral resolution is $0.4 \mu \mathrm{~m}$. The experimental results are shown in Fig. 5. Figure 5(a) displays the results of the proposed method and Fig. 5(b) gives the AFM results. Figure 5(a) is a 3D pattern depicting a section of a test area $400 \times 300(\mu \mathrm{~m})$. The average roughness $R_{\text {av }}$ for the proposed method and for the AFM are 6 and 10 nm , respectively, whereas the root-mean-square roughness $R_{\mathrm{rms}}$ are 7 and 13 nm , respectively. These results are quite close to each other. If the results from the AFM are defined as the standard, the difference between the proposed method's results and those of the AFM may be viewed as the system error. Thus, the system error is about 6 nm . In another case, a grating with 20 lines $/ \mathrm{mm}$ grooves was tested. The 3D


Fig. 4. Experimental setup.


Fig. 5. (a) 3D roughness pattern results and (b) 3D roughness pattern of the AFM results of the mirror with $\ddot{e} / 20$ roughness.


Fig. 6. (a) 3 D surface profile pattern of a 20 lines $/ \mathrm{mm}$ grating; (b) 2D average surface profile pattern of (a).
and 2D profiles are shown in Figs. 6(a) and (b), respectively. The results from another surface profilometer (Dektak-6M, Veeco, USA), which is a contact type profilometer with a tip size of $12.5 \mu \mathrm{~m}$, are shown in Fig. 7. The resulting average height $h_{\text {av }}$ from the proposed method is 89.9 nm , whereas for the Dektak-6M, $h_{\mathrm{av}}=85.4 \mathrm{~nm}$, with a height difference of 4.5 nm and an error of about $5 \%$. These results are again very close to each other. For the $0-255$ gray levels of CCD (8-bits A/D converter), the minimum variation percentage of $R_{\mathrm{s} 2}$ is $1 / 256$. Thus, the error percentage of the height is $0.4 \%$. From Eq. (6), the height resolution is given as

$$
\begin{equation*}
\left|\Delta h_{\min }\right|=\left|M \Delta R_{\mathrm{s} 2 \min }\right| \tag{7}
\end{equation*}
$$

Substituting the values $M=-210 \mathrm{~nm}$ and $\Delta R_{\mathrm{s} 2 \min }=$ $1 / 256$ into Eq. (7), the best height resolution obtained is 0.8 nm . The feasibility of the proposed method is thus demonstrated.

In conclusion, a 3D non-scanning and non-interferometric optical profilometer based on the critical angle method is proposed and verified using AFM. The error between the proposed method and AFM is about 6 nm . For the 11.8 optical magnification, the lateral and axial resolutions are $0.4 \mu \mathrm{~m}$ and 0.8 nm , respectively.


Fig. 7. Surface profile results of a 20 lines/mm grating using Dektak-6M.

The performance is better than that of Dektak-6M. The proposed approach has several advantages, including simplicity, speed, and large area measurement.
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