

# Preparing of coherent superposition state in serial multi- $\Lambda$ -type system by stimulated Raman adiabatic passage

Qifang Li (李奇芳) and Ye Kuang (旷冶)

School of Physical Science and Technology, Sichuan University, Chengdu 610065

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A scheme for creating an arbitrary coherent superposition of two atomic states in serial multi- $\Lambda$ -type system is proposed. This technique with the application of a control field is based on the existence of two degenerate dark states and their interaction. The mixing of the dark states can be controlled by changing the relative delay time of the control pulse. One can get any desired superposition by changing the delay time of the control pulse.

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In recent years, the technique called stimulated Raman adiabatic passage (STIRAP) process has been intensively studied experimentally, analytically and numerically<sup>[1-10]</sup>. In the straightforward population transfer, the STIRAP has been applied to manipulate and create coherent state superposition. The original STIRAP process has thus been utilized to create coherent superposition in three- and four-level systems<sup>[1-5]</sup>, and to prepare N-component maximally coherent superposition state<sup>[6]</sup>. In most cases, the existence of a dark state is the basis of the adiabatic transfer, which utilizes the eigenstate corresponding to zero eigenenergy. If the system is prepared in this state at the initial time, it will remain there during the time of evolution as long as adiabatic process is maintained. If the adiabatic state is arranged to go over into the desired state at the final time, this process provides a smooth and efficient population transfer between the states. And the extension of STIRAP has been developed quickly. For instance, tripod-STIRAP<sup>[2,4]</sup>, fractional-STIRAP<sup>[7,8]</sup>, and other variations of STIRAP<sup>[9,10]</sup>.

In the present work, a scheme to create coherent superposition state of two states in serial multi- $\Lambda$ -type system<sup>[11]</sup> is proposed. Serial multi- $\Lambda$ -type System has been studied previously in population transfer<sup>[3]</sup>, molecular vibrational ladder climbing<sup>[11,12]</sup>, and creating coherent superposition state<sup>[13]</sup>. Creating coherent superposition state can be carried out via fractional-STIRAP in serial multi- $\Lambda$ -type system. But all the intermediate pulses must vanish simultaneously in fractional-STIRAP, which is very difficult to realize experimentally. But by using another control laser<sup>[2]</sup>, we can also create coherent superposition state. The advantage of this method is that we do not need to control the laser pulses vanishing simultaneously, instead, we only need to control the delay time of control pulse which is much easier to realize experimentally. This method has been used to create superposition state in three-level  $\Lambda$ -type system<sup>[2]</sup>. In this letter, we extend the method to serial multi- $\Lambda$ -type system, and our goal is to create superposition state of initial state and final state of  $\Lambda$ -type system. The results show that the final superposition state can be controlled by adjusting the time of the pulses (the relative delay of

the control pulse).

Firstly, we consider the five-level  $\Lambda$ -type system shown in Fig. 1. The atoms are assumed to be initially in state  $|1\rangle$ . The time-dependent Schrödinger equation for this system can be written as

$$\frac{d}{dt}C(t) = -iW(t)C(t), \quad (1)$$

where  $C(t)$  is a column vector, whose components are the probability amplitudes  $C_n(t)$ , and the evolution matrix  $W(t)$  has the form

$$W(t) = \frac{1}{2} \begin{pmatrix} 0 & P_1(t) & 0 & 0 & 0 & 0 \\ P_1(t) & 0 & S_1(t) & 0 & 0 & 0 \\ 0 & S_1(t) & 0 & P_2(t) & 0 & 0 \\ 0 & 0 & P_2(t) & 0 & S_2(t) & Q(t) \\ 0 & 0 & 0 & S_2(t) & 0 & 0 \\ 0 & 0 & 0 & Q(t) & 0 & 0 \end{pmatrix}, \quad (2)$$

where  $P_1(t)$ ,  $P_2(t)$ ,  $S_1(t)$ ,  $S_2(t)$ , and  $Q(t)$  are the time-dependent Rabi-frequencies of the pump, Stokes and control pulses, respectively. We assume  $P_1(t)$ ,  $P_2(t)$ ,  $S_1(t)$ ,  $S_2(t)$ , and  $Q(t)$  to be real without loss of generality. Then the eigenvalue of this system is

$$\lambda = 0, \pm\Omega_1(t), \pm\Omega_2(t), \quad (3)$$

where

$$\Omega_1(t) = \sqrt{P_1(t)^2 + S_1(t)^2}, \quad (4)$$

$$\Omega_2(t) = \sqrt{P_2(t)^2 + S_2(t)^2 + Q(t)^2}. \quad (5)$$

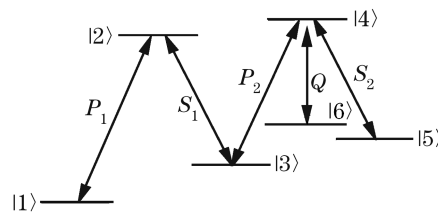


Fig. 1. Five-level  $\Lambda$ -type system.  $P_1$  and  $P_2$ : pump pulses;  $S_1$  and  $S_2$ : Stokes pulses;  $Q$ : the control pulse.

The analysis of the system is simplified by introducing a set of adiabatic states  $\Phi_k(t)$ . There exist two degenerate dark states with null eigenvalue and no component of atomic states  $\psi_2$  and  $\psi_4$ . And the two corresponding degenerate dark states are

$$|\Phi_1\rangle = \sin \varphi \cos \theta |1\rangle - \sin \varphi \sin \theta |3\rangle + \cos \varphi |5\rangle, \quad (6)$$

$$|\Phi_2\rangle = \cos \varphi \cos \theta \sin \alpha |1\rangle - \cos \varphi \sin \theta \sin \alpha |3\rangle - \sin \varphi \sin \alpha |5\rangle + \cos \alpha |6\rangle, \quad (7)$$

where

$$\tan \theta = \frac{P_2(t)}{S_2(t)}, \quad \tan \varphi = \frac{P_1(t)\sqrt{P_2^2(t) + S_2^2(t)}}{P_1(t)S_2(t)}, \quad (8)$$

$$\tan \alpha = \frac{Q(t)\sqrt{P_1^2(t) + S_1^2(t)}}{\sqrt{P_1(t)^2 P_2(t)^2 + S_1(t)^2 S_2(t)^2 + P_1(t)^2 S_2(t)^2}}. \quad (9)$$

Because the proposed technique is based on the existence of two degenerate dark states and their interaction, we do not write remaining eigenvectors  $\Phi_3$ ,  $\Phi_4$ ,  $\Phi_5$ , and  $\Phi_6$ . And in the adiabatic limit, the nonadiabatic coupling of dressed states  $\Phi_1(t)$  or  $\Phi_2(t)$  to the other dressed states can be neglected, only the transition between the degenerate dressed states  $\Phi_1(t)$  and  $\Phi_2(t)$  is important. The two degenerate adiabatic states  $\Phi_1(t)$  and  $\Phi_2(t)$  do not contain states  $\psi_2$  and  $\psi_4$ .

The desired pulse sequence to create an arbitrary superposition of  $\psi_1$  and  $\psi_5$  will be designed so that the two degenerate dark states correspond, for  $t \rightarrow \pm\infty$ , to bare atomic states:

$$\text{Initial stage : } \psi_1 \rightarrow \Phi_1, \quad (10)$$

$$\text{Interaction stage : } \Psi(t) \rightarrow \cos \Theta_\infty \Phi_1 + \sin \Theta_\infty \Phi_2, \quad (11)$$

$$\text{Final stage : } \Phi_1 \rightarrow \psi_1, \quad \Phi_2 \rightarrow \psi_5, \quad (12)$$

The result of the sequence state :

$$\Psi(t \rightarrow \infty) = \cos \Theta_\infty \psi_1 + \sin \Theta_\infty \psi_5, \quad (13)$$

where  $\Theta_\infty$  is the asymptotic mixing angle, and this angle determines the asymptotic superposition coefficients. From Ref. [2] we know

$$\Theta_\infty = \int_{-\infty}^t d\tau_Q \dot{\varphi}(\tau_Q) \sin \varphi(\tau_Q), \quad (14)$$

where  $\tau_Q$  is the delay time of the control pulses relative to the pump and Stokes pulses.

Initially the system will evolve from  $\psi_1$  to  $\Phi_1$ , and because of the coupling of  $\Phi_1$  and  $\Phi_2$ , it will finally end up with superposition state of  $\psi_1$  and  $\psi_5$ . For example, to generate equal superposition state, first to evolve  $\psi_1$  into  $\Phi_1$ , we should have  $\theta = 0$  and  $\varphi = \pi/2$ , which means that  $S_1(t)$  precedes  $P_1(t)$ , and  $S_2(t)$  precedes  $P_2(t)$  based on Eq. (8); at the end of interaction, to get superposition state of  $\psi_1$  and  $\psi_5$ , the mixing angles should be  $\theta = 0$ ,

$\varphi = \pi/2$ , and  $\alpha = \pi/2$ , which means that  $P_2(t)$  vanishes earlier than  $S_2(t)$ ,  $P_1(t)$  vanishes earlier than  $S_1(t)$ , and  $S_2(t)$  vanishes earlier than  $Q$  based on Eqs. (8) and (9). We illustrate the procedure in Fig. 2. Figure 2(a) shows the pulses and Fig. 2 (b) shows the resulting populations. We can see that the initial bare atomic state  $\psi_1$  is turned into an equal superposition state of  $\psi_1$  and  $\psi_5$ .

We can also generate any desired superposition by varying the delay time of the control pulse. From Eq. (14), we can get any desired superposition by altering the mixing angle  $\Theta_\infty$  which is governed by the relative delay time of the control pulse. So by varying the delay  $\tau_Q$  among the control pulse and the pump and Stokes pulses, we can

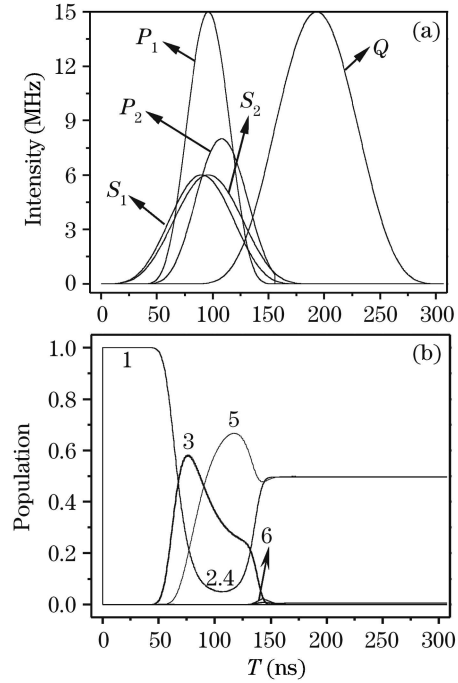


Fig. 2. (a) Example of pulses for coherence generation.  $A_{P_1} = 15$ ,  $A_{P_2} = 8$ ,  $A_{S_1} = A_{S_2} = 6$ ,  $A_Q = 15$ ,  $T_{P_1} = 120$ ,  $T_{P_2} = 1.2T_{P_1}$ ,  $T_{S_1} = 1.5T_{P_1}$ ,  $T_{S_2} = 1.6T_{P_1}$ , and  $T_Q = 1.9T_{P_1}$ ,  $\tau_Q = 0.66T_{P_1}$ ,  $\tau_{P_1} = \tau_{P_2} = 0.3T_{P_1}$ ; (b) time evolution of populations as produced by these pulses. The populations of excited states 2 and 4 remain zero.  $A_i$  ( $i = P_1, P_2, S_1, S_2, Q$ ) are the Rabi-frequencies of the pulses, and  $T_i$  ( $i = P_1, P_2, S_1, S_2, Q$ ) are the widths of the pulses.

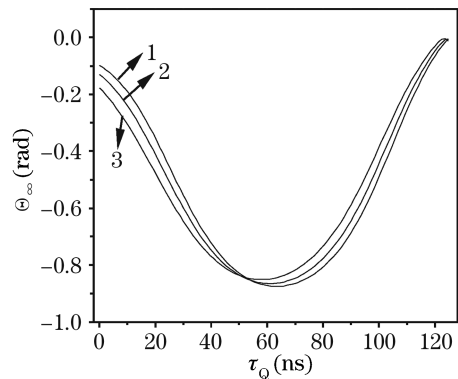


Fig. 3. Asymptotic mixing angle  $\Theta_\infty$  as a function of delay time  $\tau_Q$  of the control pulse. Curve 1, 2 and 3 show  $A_Q = 18$ , 15, and 13, respectively.

produce a range of superposition. Figure 3 shows the mixing angle  $\Theta_\infty$  as a function of the delay time  $\tau_Q$ . It can be seen that the mixing angle  $\Theta_\infty$  ranges from  $-0.1$  to  $-0.9$  as the delay time  $\tau_Q$  changes, and  $\Theta_\infty$  is not very sensitive to variations of the control-pulse amplitude. Then it is possible to choose the delay time to produce any desired superposition.

This method can be extended to the seven serial multi- $\Lambda$ -type system, in which the control pulse  $Q(t)$  couples the intermediate state  $\psi_6$  to a eighth state  $\psi_8$ . The system has two dark states:

$$\begin{aligned} \Phi_1 = & \sin \alpha \sin \beta \cos \gamma |1\rangle - \sin \alpha \sin \beta \sin \gamma |3\rangle \\ & + \sin \alpha \cos \beta |5\rangle - \cos \alpha |7\rangle, \end{aligned} \quad (15)$$

$$\begin{aligned} \Phi_2 = & \cos \alpha \sin \beta \cos \gamma \sin \theta |1\rangle - \cos \alpha \sin \beta \sin \gamma \sin \theta |3\rangle \\ & + \cos \alpha \cos \beta \sin \theta |5\rangle + \sin \alpha \sin \theta |7\rangle - \cos \theta |8\rangle, \end{aligned} \quad (16)$$

$$\begin{aligned} \tan \alpha = & \frac{S_3 \sqrt{S_1^2 S_2^2 + P_1^2 P_2^2 + P_1^2 S_2^2}}{P_1 P_2 P_3}, \\ \tan \beta = & \frac{S_2 \sqrt{S_1^2 + P_1^2}}{P_1 P_2}, \quad \tan \gamma = \frac{P_1}{S_1}, \end{aligned} \quad (17)$$

$$\tan \theta = \frac{Q \sqrt{S_1^2 S_2^2 + P_1^2 P_2^2 + P_1^2 S_2^2}}{\sqrt{S_1^2 S_2^2 S_3^2 + P_1^2 P_2^2 S_3^2 + P_1^2 S_2^2 S_3^2 + P_1^2 P_2^2 P_3^2}}. \quad (18)$$

In order to get the equal superposition state of  $\psi_1$  and  $\psi_7$ , we must achieve  $\alpha = \pi/2$ ,  $\beta = \pi/2$ , and  $\gamma = 0$  initially,  $\alpha = \pi/2$ ,  $\beta = \pi/2$ ,  $\gamma = 0$  and  $\theta = \pi/2$  at the end of interaction, which requires that the Stokes pulses arrive earlier but vanish later than the corresponding pump pulses, and the control pulse arrives and vanishes last.

So for any serial multi- $\Lambda$ -type system, we can create any superposition state of  $\psi_1$  and  $\psi_n$  if the control pulse  $Q(t)$  couples the intermediate state  $\psi_{n-1}$  to state  $\psi_{n+1}$ .

All the Stokes pulses arrive earlier but vanish later than the corresponding pump pulses, and the control pulse arrives and vanishes last.

In conclusion, we have analytically and numerically explored creating superposition states of  $\psi_1$  and  $\psi_n$  in serial multi- $\Lambda$ -type system. By using a controlled field, we have two degenerate dark states. Through the interaction of these two states and the proper design of laser pulse sequence, we can create arbitrary superposition state by only controlling the pulse delay time. This is much easier to realize experimentally than fractional-STIRAP.

Q. Li's e-mail address is lqfanna@163.com.

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