

# Theoretical study on longitudinally pumped Yb<sup>3+</sup>:Y<sub>2</sub>O<sub>3</sub> lasers

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To optimize the performance of longitudinally pumped Yb<sup>3+</sup>:Y<sub>2</sub>O<sub>3</sub> ceramic lasers, cavity parameters such as material length and output coupler transmission at a certain laser output power are calculated numerically using quasi-three-level laser model. The results show great potential of Yb<sup>3+</sup>:Y<sub>2</sub>O<sub>3</sub> ceramics for highly efficient diode-pumped solid-state lasers.

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Yb<sup>3+</sup>-doped laser materials are very attractive for ultra-short pulse lasers as well as high-power solid-state lasers due to their broad absorption and emission bandwidths. Y<sub>2</sub>O<sub>3</sub> is a promising solid-state laser material for trivalent lanthanide activators because of its some favorable properties, such as refractory nature, stability, and optical clarity over a broad spectral region. Thermal conductivity of Y<sub>2</sub>O<sub>3</sub> is much larger than that of YAG, and their thermal expansion coefficients are very similar<sup>[1]</sup>. However, it is not feasible to obtain large size Y<sub>2</sub>O<sub>3</sub> single crystals with sufficient optical quality by conventional melt-growth methods due to its melting temperature of 2430 °C and structure phase transition at 2280 °C. Therefore, there have been few reports on the Yb<sup>3+</sup> doped Y<sub>2</sub>O<sub>3</sub> lasers<sup>[2]</sup>.

Recently, highly transparent ceramics have been fabricated using the liquid-phase chemical reaction and non-press vacuum sintering method<sup>[3,4]</sup>. The quality and the size of the ceramics have been improved greatly and highly efficient laser oscillations have been obtained<sup>[1,2,5]</sup>. However, the performance of the Yb<sup>3+</sup>:Y<sub>2</sub>O<sub>3</sub> ceramic lasers has not been optimized. In this paper, we calculate numerically cavity parameters to

optimize the performance of Yb<sup>3+</sup>:Y<sub>2</sub>O<sub>3</sub> ceramic lasers.

Yb<sup>3+</sup>-doped Y<sub>2</sub>O<sub>3</sub> laser is a typical quasi-three-level system. The energy level diagram of Yb<sup>3+</sup> ions is shown in Fig. 1<sup>[6]</sup>. The Yb<sup>3+</sup> ions have two 4f<sup>13</sup> manifolds, <sup>2</sup>F<sub>5/2</sub>, and <sup>2</sup>F<sub>7/2</sub>, with energy gap of about 10225 cm<sup>-1</sup>. The upper laser level is the lowest of the three crystal-field components of <sup>2</sup>F<sub>5/2</sub> state. To the laser transition at 1076 nm, the lower laser level is the uppermost of the four crystal-field components of <sup>2</sup>F<sub>7/2</sub> state. To the laser transition at 1031 nm, the lower laser level is the third crystal-field component of <sup>2</sup>F<sub>7/2</sub> state. Assuming that relative populations of the levels can be described by a Boltzman distribution, the actual population densities in the lower and upper laser levels can be written as<sup>[7]</sup>

$$N_1 = \frac{g_1 N_L}{Z_L} \exp(-E_1/kT) = f_1 N_L, \quad (1)$$

$$N_2 = \frac{g_2 N_U}{Z_U} \exp(-E_2/kT) = f_2 N_U, \quad (2)$$

where Z<sub>L</sub> and Z<sub>U</sub> are the partition functions of the lower and upper states, respectively, which are defined as

$$Z_L = \sum_i g_i \exp(-E_i/kT),$$

$$Z_U = \sum_j g_j \exp(-E_j/kT), \quad (3)$$

where g<sub>i</sub> and g<sub>j</sub> are the degeneracies of the lower and upper states, respectively. For the Yb<sup>3+</sup> ions in Y<sub>2</sub>O<sub>3</sub> laser material, g<sub>i</sub> = g<sub>j</sub> = 1. E<sub>i</sub> and E<sub>j</sub> are measured from the lowest crystal-field component of <sup>2</sup>F<sub>7/2</sub> and <sup>2</sup>F<sub>5/2</sub> states, respectively, N<sub>L</sub> and N<sub>U</sub> are the total population densities of the <sup>2</sup>F<sub>7/2</sub> and <sup>2</sup>F<sub>5/2</sub> states, and f<sub>1</sub> and f<sub>2</sub> are the fractional populations in the lower and upper laser levels, respectively.

The formula of laser threshold has been obtained from the rate equations describing the population inversion and the photon density in the laser cavity in the steady-state case<sup>[8]</sup>

$$P_{th3} = \frac{\pi h \gamma_p (w_1^2 + w_p^2) (L + T + 2N_1^0 \sigma_{em} l)}{4\sigma_{em} \tau \eta_p \eta_a (f_1 + f_2)}, \quad (4)$$

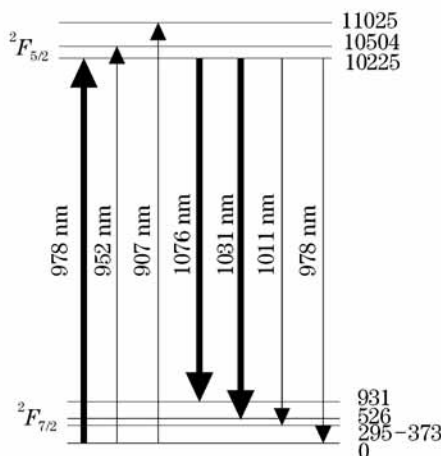


Fig. 1. Scheme of crystal splitting of the <sup>2</sup>F<sub>7/2</sub> and <sup>2</sup>F<sub>5/2</sub> levels of Yb<sup>3+</sup> ions in Y<sub>2</sub>O<sub>3</sub> laser. The levels of the upper and lower manifolds and their energies are shown. The laser transition is noted by the heavy line. The populations of the upper and lower laser levels are given by N<sub>2</sub> and N<sub>1</sub>, respectively.

**Table 1. Spectroscopic Parameters of the 10 at.-% Yb<sup>3+</sup>:Y<sub>2</sub>O<sub>3</sub> Ceramics**

Material	$\lambda_p$ (nm)	$\sigma_p$ ( $\times 10^{-20}$ cm <sup>2</sup> )	$\tau$ (ms)	$\lambda_{em}$ (nm)	$\sigma_{em}$ ( $\times 10^{-20}$ cm <sup>2</sup> )	$f_1$	$f_2$	$N_1^0$ ( $\times 10^{20}$ cm <sup>-3</sup> )
Transparent Ceramic	976	2.4 <sup>[10]</sup>	0.82 <sup>[4]</sup>	1031	0.92 <sup>[10]</sup>	0.06	0.78	1.25
				1076	0.36 <sup>[10]</sup>	0.009		0.18

where  $h\gamma_p$  is the pump photon energy,  $w_l$  is the laser-beam waist,  $w_p$  is the pump-beam waist,  $L$  is intrinsic cavity loss,  $T$  is the output coupler (OC) transmission,  $N_1^0$  is the unpumped population-inversion density of the lower laser level,  $\sigma_{em}$  is the gain cross section,  $\tau$  is the lifetime of the upper manifold,  $\eta_a = 1 - \exp(-\alpha l)$  is the fraction of incident pump power absorbed in a crystal of length  $l$  with absorption coefficient  $\alpha$ ,  $\eta_p$  is the pump quantum efficiency. The pumping process is assumed to have unity quantum efficiency.

Let  $w_l = w_p$ , the laser output power can be obtained from<sup>[7]</sup>

$$1 + \frac{B}{fS} \ln(1 + fS) = fF \left[ \frac{1}{fS} - \frac{1}{(fS)^2} \ln(1 + fS) \right], \quad (5)$$

where  $f = f_1 + f_2$ ,  $B = \frac{2N_1^0 \sigma_{em} l}{L+T}$ ,  $F = \frac{4P_p \tau \sigma_{em} \eta_a \eta_p}{\pi h \gamma_p w_l^2 (L+T)}$ ,  $S = \frac{2c \sigma_{em} \tau \Phi}{n \pi w_l^2 l}$ ,  $c$  is the velocity of light in vacuum,  $n$  is the refractive index,  $P_p$  is the incident pump power, the total number  $\Phi$  of laser photons in the cavity is given by  $\Phi = \frac{2n l P_L}{ch \gamma_L}$ , where  $P_L$  is the laser power traveling in one direction inside the cavity and  $\gamma_L$  is the laser frequency, the laser output power  $P_{out} = P_L T$ .

The optical properties of ceramics are very similar with those of single crystals<sup>[9]</sup>, so we can optimize the performance of ceramic lasers by the optical properties of single crystals. The spectroscopic parameters of 10 at.-% Yb<sup>3+</sup>-doped Y<sub>2</sub>O<sub>3</sub> are listed in Table 1. There exists the strongest absorption peak centered at 976 nm in the absorption spectrum of the Yb<sup>3+</sup>:Y<sub>2</sub>O<sub>3</sub> ceramics, so a diode laser at 976-nm wavelength is used to longitudinally pump Yb<sup>3+</sup>:Y<sub>2</sub>O<sub>3</sub> ceramics.

At the laser output power of 6 W, the incident pump power of the laser at 1031-nm wavelength versus OC transmission and material length is plotted according to

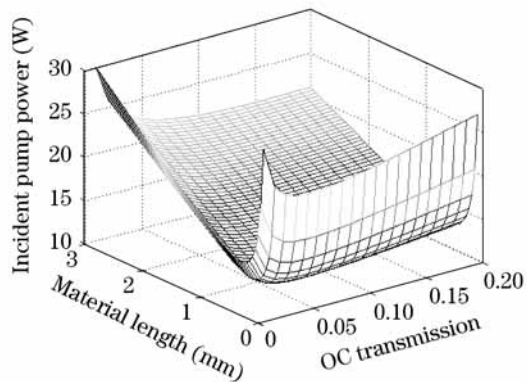


Fig. 2. Incident pump power of the laser at 1031-nm wavelength versus OC transmission and material length at the laser output power of 6 W.

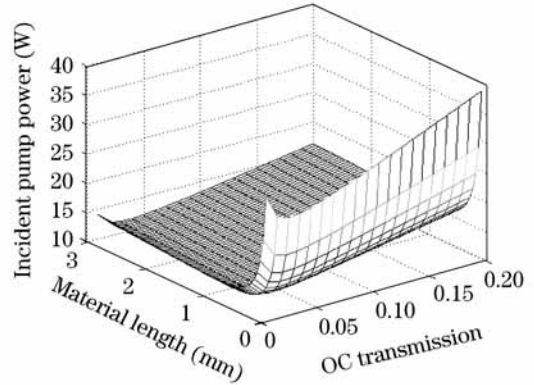


Fig. 3. Incident pump power of the laser at 1076-nm wavelength versus OC transmission and material length at the laser output power of 6 W.

Eq. (5) in Fig. 2. In calculation, we use the parameters  $w_p = w_l = 150 \mu\text{m}$  and  $L = 0.6\%$ . Figure 2 shows that OC transmission and material length have a great influence on incident pump power. When the OC transmission is a constant, there exists a length which minimizes the incident pump power; when the material length is a constant, there exists an OC transmission which minimizes the incident pump power too. In the conditions considered, the incident pump power is at its minimum of 11.64 W when the material length is 0.5 mm and the OC transmission is 6%. The corresponding lasing threshold power is 2.25 W, the slope efficiency is 66%, and the optical-optical conversion efficiency is 51.5%. When the laser output power increases, the optimum material length and the OC transmission increase too. For example, at the laser output power of 1 W, the optimum material length is 0.35 mm and OC transmission is 3%; at the laser output power of 10 W, the optimum material length is 0.6 mm and OC transmission is 8%.

Similarly, Fig. 3 shows the incident pump power of the laser at 1076-nm wavelength as a function of OC transmission and material length at the laser output power of 6 W. When the material length is 0.9 mm and the OC transmission is 3%, the performance of the laser at 1076-nm wavelength is optimized with the lasing threshold power of 1.49 W, the incident pump power of 10.55 W, the corresponding slope efficiency of 67%, and the optical-optical conversion efficiency of 56.9%.

We have presented an analysis of the performance of longitudinally pumped quasi-three-level Yb<sup>3+</sup>:Y<sub>2</sub>O<sub>3</sub> lasers. At the laser output power of 6 W, the laser at 1031-nm wavelength can be optimized with the slope efficiency of 66%, the optical-optical conversion efficiency of 51.5% at the material length of 0.5 mm and the OC transmission of 6%. The laser at 1076-nm wavelength can be optimized with the slope efficiency of 67% and optical-optical conversion efficiency of 56.9% at

the material length of 0.9 mm and the OC transmission of 3%. The performance of  $\text{Yb}^{3+}:\text{Y}_2\text{O}_3$  lasers is optimized by choosing an appropriate material length and an appropriate OC transmission at a certain laser output power. The calculated results show great potential of  $\text{Yb}^{3+}:\text{Y}_2\text{O}_3$  ceramics for highly efficient diode-pumped solid-state lasers.

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