

# Digital measuring scheme for half-wave voltage of Y-tap multiple integrated optical circuit

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A high-precision digital measuring scheme for half-wave voltage of Y-tap multiple integrated optical circuits is proposed. This scheme is based on Sagnac interferometer modulated with digital step waveform whose frequency is half of eigen frequency of the interferometer. The technology and measuring precision are discussed. An experimental setup is made and the temperature-dependences of half-wave voltage of two samples are studied. Analysis and experimental study prove that this scheme is convenient and accurate. OCIS codes: 130.3120, 120.5790, 060.5060.

Y-tap multiple integrated optical circuit (MIOC), which has single polarization waveguide Y-tap fabricated in LiNbO<sub>3</sub> with annealing proton exchanged (APE) technology and two phase modulators based on Pockels effect, is one of the key components of close-loop fiber optic gyroscope (FOG). It takes the roles of mode filter (polarizer), directional coupler, and phase modulator in FOG<sup>[1]</sup>. As an electro-optic component, the half-wave voltage  $V_\pi$ , which is defined as the voltage that can produce  $\pi$  phase change of light wave propagating in MIOC, is a special parameter that will vary with environmental temperature and directly bring nonlinearity in close-loop FOG. Model compensation is an effective approach to reduce this defect<sup>[2]</sup>, so it is very important to get accurate model with precision measuring. In general, Mach-Zehnder interferometer formed with two MIOCs can be used to measure  $V_\pi$  and moderate precision can be gotten with complex system and special modulation technology<sup>[3]</sup>. However, the measuring precision is limited because this system has poor stability. To satisfy the demand of high precision measuring and modeling, an all-digital scheme based on Sagnac interferometer is proposed and discussed. With this technology, two MIOC samples are studied.

Figure 1 is the schematic diagram for  $V_\pi$  measurement. The superluminescent diode (SLD), coupler, detector, fiber coil, and the MIOC to be measured compose a Sagnac interferometer. In Fig. 1, the coupler takes the charge of sending the light from SLD to MIOC and guiding the coming back signal to the detector; MIOC and fiber coil form a closed optical path, the light from point  $J$  is splitted into two parts propagating along converse direction and then recombining at  $J$ . The interference output signal is monitored by a digital oscillograph, it

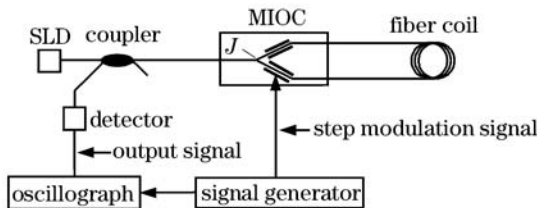


Fig. 1. Schematic diagram for  $V_\pi$  measurement.

can be described as<sup>[1]</sup>

$$v_o = K(1 + \cos \phi), \tag{1}$$

where  $K$  is the coefficient related with the incident optical power on detector and the gain of detector module,  $\phi$  is the nonreciprocal phase which can be produced by rotation or nonreciprocal modulation.

Herein, the measuring system is always still and  $\phi$  is attributed to nonreciprocal modulation only. Figure 2 shows the modulation signal and relative waveforms when a digital step modulation signal generated by a digital signal generator is added to the electrode of MIOC. In this figure, waveform A represents the relation of  $v_o$  and  $\phi$  described by Eq. (1). The step height and width of modulation signal C are  $V_s$  and  $\tau$  ( $\tau$  is the time needed for light transmitting through the fiber coil once), respectively, and the frequency is half of the eigen frequency of the Sagnac interferometer, the period of modulation signal is  $4\tau$ . Because the modulator is at one end of the coil, the clockwise (cw) and counter clockwise (ccw) light signals are modulated at different time. The time difference is  $\tau$  which is attributed to the fiber coil delay. The phase produced by the modulator can be calculated by<sup>[1]</sup>

$$\phi(t) = \phi_m(t) - \phi_m(t - \tau), \tag{2}$$

where  $\phi_m(t)$  and  $\phi_m(t - \tau)$  represent the modulation

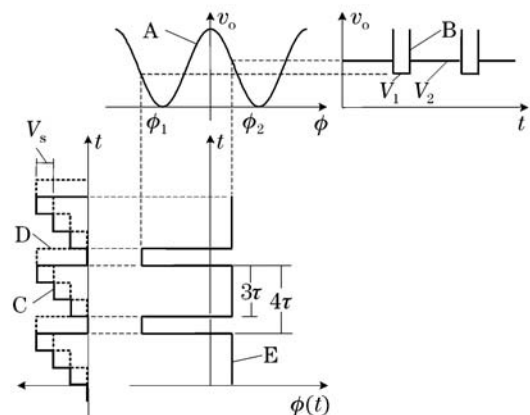


Fig. 2. Digital step modulation signal and relative waveforms.

phases of ccw and cw propagating light, namely waveform C (solid lines) and D (dashed lines) in Fig. 2. Waveform E in Fig. 2 represents  $\phi(t)$  which is described by Eq. (2) and has the period of  $4\tau$ . Waveform B is the output of detector. During a modulation period, the modulation phase differences  $\phi_1$  and  $\phi_2$  for ccw and cw light will be

$$\phi_1 = \phi(t) = -\frac{3\pi V_s}{V_\pi}, \quad (0 < t < \tau), \quad (3)$$

$$\phi_2 = \phi(t) = \frac{\pi V_s}{V_\pi}, \quad (\tau < t < 4\tau), \quad (4)$$

the corresponding outputs are

$$V_1 = K[1 + \cos(\phi_1)], \quad (5)$$

$$V_2 = K[1 + \cos(\phi_2)]. \quad (6)$$

Let  $V_1 = V_2$ , combining Eqs. (3)–(6), the first non-zero solution of  $V_\pi$  is

$$V_\pi = 2 \cdot V_s. \quad (7)$$

$V_s$  is artificially set, so adjusting  $V_s$  from low to high, when  $V_1$  is equal to  $V_2$  for the first time, the half-wave voltage  $V_\pi$  is  $2V_s$  and the accurate measurement is realized. The practical waveforms during measuring procedure are shown in Fig. 3. The difference between  $V_1$  and  $V_2$  varies obviously when  $V_s$  changes 2 mV.

When  $V_1 \approx V_2$ ,  $\phi_1 \approx -3\pi/2$ , and  $\phi_2 \approx \pi/2$ ,  $V_1, V_2$  are very sensitive with the variation of  $V_s$ , as shown in Fig. 3. Let

$$\Delta V = V_2 - V_1, \quad (8)$$

$\Delta V$  can be used to judge whether Eq. (7) is satisfied. From Eqs. (3)–(6), Eq. (8) can be

$$\Delta V \approx 2K \sin\left(\frac{2\pi \cdot \Delta V_s}{V_\pi}\right). \quad (9)$$

The value of  $\Delta V_s$  is determined by the resolution of signal detection system. This measuring technology is similar to the signal processing in close-loop FOG. We can use it to estimate the accuracy of  $\Delta V_s$ . For example,  $1^\circ/\text{hour}$  bias drift can be achieved easily in FOG and it

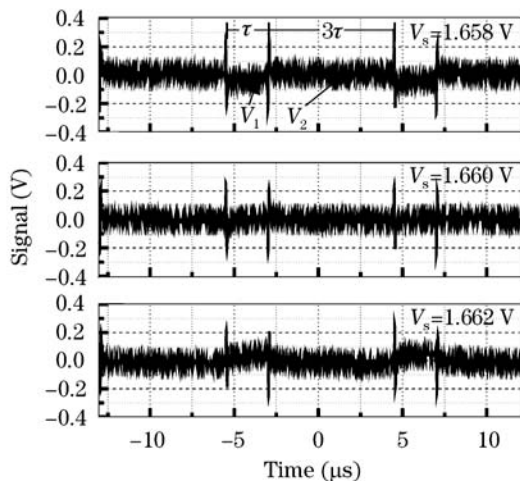


Fig. 3. Waveforms during the measuring procedure.

approximately corresponds to  $10^{-6}$ -rad phase drift. In Eq. (9), this means  $2\pi \cdot \Delta V_s / V_\pi \approx 10^{-6}$ .  $V_\pi$  is only a few voltages,  $\Delta V_s$  will be much smaller. This proves that this scheme can achieve very high accuracy. Otherwise, when  $V_1 = V_2$ , Eq. (7) is satisfied and  $\phi_1 = -3\pi/2$ ,  $\phi_2 = \pi/2$ , the measuring veracity is guaranteed naturally.

From Eqs. (3)–(6) and (8), we know it is the  $2\pi$  phase difference between  $\phi_1$  and  $\phi_2$  that makes Eq. (7) satisfied. During a modulation period, which is about a few microseconds, we can define whether  $V_1 = V_2$  is satisfied and the measuring procedure can be thought as instantaneous. So, any nonreciprocal phase shift induced by other factors, such as environmental temperature varying, rotation, etc., will not affect the measurement because these changes are all slow. With the same reason, the measurement is insensitive to the small variation of  $K$  induced by optical path loss change or source power change in Eq. (1). This means the measurement is insensitive to environment and high precision can be achieved.

A digital auto measuring setup is made based on Fig. 1 and shown in Fig. 4. The output from detector is digitized with a 12-bit analog/digital converter (A/D), the digital step signal is generated with a 12-bit digital/analog converter (D/A) and the computer takes the role to calculate the voltage difference and adjust the step height. The length of fiber coil is about 500 m and the operation wavelength is  $1.3 \mu\text{m}$ . In the experiment, only the MIOC which is connected with coupler and fiber coil by fuse splicing is mounted in a temperature chamber (TC),  $V_\pi$  is measured at different temperature from  $-40$  to  $60^\circ\text{C}$ .

Two MIOC samples from different companies have been tested. The results are shown in Figs. 5 and 6. The  $V_\pi$  variations are respectively 0.163 and 0.251 V within

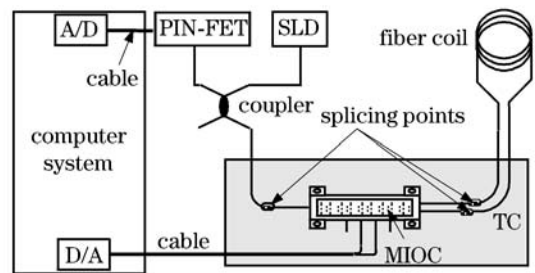


Fig. 4. Digital experimental setup. FET: field effect transistor.

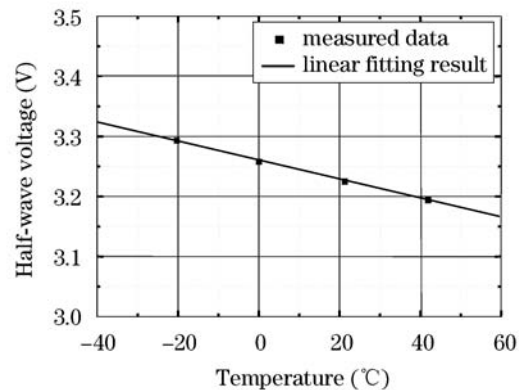


Fig. 5. Test result of sample 1.

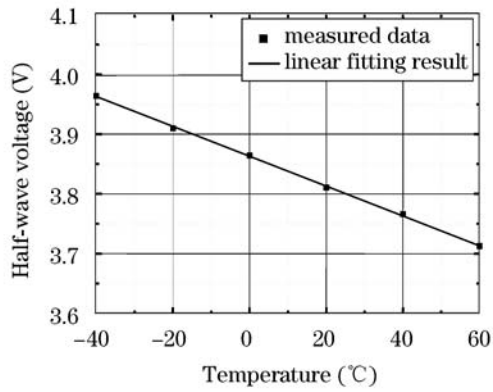


Fig. 6. Test result of sample 2.

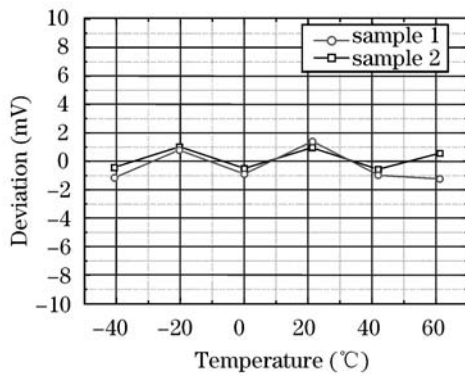


Fig. 7. Linear deviation of the tested data.

the whole temperature range from  $-40$  to  $60$  °C. After least square polynomial fit with the measured data from  $-40$  to  $60$  °C, the variations are found to be linear in the test temperature range and the temperature coefficients are  $503$  and  $654$  ppm/°C, respectively. The result is similar as the data reported in Ref. [4]. The absolute linear deviation is calculated and the value is about  $1$  mV (see Fig. 7). This proves that the measurement has high precision and the temperature dependence of  $V_{\pi}$  has good linearity.

In summary, experimental study and detail discussion demonstrate that the proposed scheme can measure  $V_{\pi}$  of Y-tap MIOC conveniently and accurately. Experimental study on the temperature-dependence of  $V_{\pi}$  of MIOC also shows that  $V_{\pi}$  decreases as temperature increases with good linearity. With this digital scheme, the accurate temperature model can be obtained easily.

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