Effect of concentration quenching on the spectroscopic properties of Er³⁺/Yb³⁺ co-doped AlF₃-based glasses

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A series of highly ${\rm Er}^{3+}/{\rm Yb}^{3+}$ co-doped fluoroal uminate glasses have been investigated in order to develop a microchip laser at 1.54 $\mu{\rm m}$ under 980 nm excitation. Measurements of absorption, emission and upconversion spectra have been performed to examine the effect of ${\rm Er}^{3+}/{\rm Yb}^{3+}$ concentration quenching on spectroscopic properties. In the glasses with ${\rm Er}^{3+}$ concentrations below 10 mol%, concentration quenching is very low and the ${\rm Er}^{3+}/{\rm Yb}^{3+}$ co-doped fluoroal uminate glasses have stronger fluorescence of 1.54 $\mu{\rm m}$ due to the ${}^4I_{13/2} \rightarrow {}^4I_{15/2}$ transition than that of ${\rm Er}^{3+}$ singly-doped glasses. As ${\rm Er}^{3+}$ concentrations above 10 mol% in the ${\rm Er}^{3+}/{\rm Yb}^{3+}$ co-doped samples, concentration quenching of 1.54 $\mu{\rm m}$ does obviously occur as a result of the back energy transfer from ${\rm Er}^{3+}$ to ${\rm Yb}^{3+}$. To obtain the highest emission efficiency at 1.54 $\mu{\rm m}$, the optimum doping-concentration ratio of ${\rm Er}^{3+}/{\rm Yb}^{3+}$ was found to be approximately 1:1 in mol fraction when the ${\rm Er}^{3+}$ concentration is less than 10 mol%.

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Laser oscillators based on an erbium-doped laser system which can be operated in a microchip configuration [1-3]have recently become the subject of great interest, especially for their potential use at 1.54 μm and for telemetry at an eye-safe wavelength. So far, microchip lasers at wavelengths of 1.06^[1,2] and 1.340 μm ^[3] have been mainly investigated in rare earth ions doped crystalline host materials. High power microchip laser operation in glass hosts requires that rare earth concentration should be at least one order of magnitude higher than those in crystalline hosts. This increase is required in order to obtain sufficient absorption of the pumping radiation in short active-length of material and to compensate for small gain^[1]. However, the occurrence of cluster and concentration quenching in high rare earth concentrations in most of glass systems are the major obstacle in this area^[1,4]. According to the above reasons, only several papers have been published since the first erbium doped glass-based microchip laser has been reported in 1993^[5]. To our knowledge, there are no reports that systematically analyzed the effect of concentration quenching on the spectroscopic properties of highly Er³⁺/Yb³⁺ codoped fluoroaluminate glasses.

Fluoride glass is a good host for rare earth doping and to obtain high efficiency upconversion luminescence because of its lower phonon energy than oxide glasses $[^{6,7}]$. Fluoride glass also has more symmetric and smaller crystal fields than oxide glass systems $[^{8}]$. ZrF_4 -based (fluorozirconate) glasses and AlF_3 -based (fluoroaluminate) glasses are two main types of fluoride glasses. Most of the previous works are focusing on the ZrF_4 -based glasses with high Er^{3+} singly doped $[^{9-12}]$. In fact, Er^{3+} highly doped fluoroaluminate glass also has a strong 1.54- μ m emission under 980-nm excitation $[^{13}]$. In addition, fluoroaluminate glass offers another important advantage over fluorozirconate glass for using as a laser host because of its higher glass transition temperature, and more chemically and mechanically durable than fluorozirconate $[^{14}]$. Furthermore, fluoroaluminate glass

systems have high ability to allow very high ytterbium-incorporation $^{[15]}$.

The development of erbium glass laser systems has renewed the requirements for additional researches of improving laser glass properties and performance. It is well known that three-level laser system requires more population in the excited metastable level than that in the ground level. Because 1.54- μm Er³⁺ laser is a three-lever laser system, so Yb³⁺ ion is always chosen as sensitizer for co-doping to achieve efficient laser operation. In the Yb³⁺ energy level scheme, there are only two manifolds, i.e., the $^2F_{7/2}$ ground state and the $^2F_{5/2}$ excited state. Yb³⁺ laser materials have a strong absorption peak, which is well coupled to a 980-nm InGaAs laser diode. It is commonly believed that, because of the simplest energy scheme of Yb³⁺ ion concentration quenching, excited state absorption, up-conversion and multi-phonon relaxation do not occur in this ion^[16]. In this work, Yb³⁺ is added to Er³⁺ doped fluoroaluminate glasses and the emission intensity depended upon Er³⁺ and Yb³⁺ concentration is investigated. The mechanism of energy-transfer between Er³⁺ and Yb³⁺ in high Er³⁺/Yb³⁺ co-doped fluoroaluminate glasses is also discussed. An optimum Er³⁺/Yb³⁺ concentration ratio is found experimentally.

A series of fluoroaluminate glass samples are prepared using reagent grade AlF₃, MgF₂, CaF₂, SrF₂, BaF₂, YF₃, ErF₃ and YbF₃ as the starting materials. The batch compositions of the glasses are listed in Table 1.

Accurately weighted 5-g batches are thoroughly mixed and moved into platinum crucibles. 10 wt % of ammonium bifluoride (NH₄F·HF) is mixed with each batch. The batches are melted in the temperature range of 1000 $-1050~^{\circ}\mathrm{C}$ for 15 minutes under an Ar atmosphere. The melts are cast into preheated brass molds, and then the obtained glasses are annealed at their transition temperatures determined by differential thermal analysis (DTA). The glasses are cut into the size of $5\times5\times1~\mathrm{mm}^3$ for optical measurements.

Table 1. Composition of Glasses (mol%)

Glass	(x+y<15.0)	(x+y > 15.0)
AlF_3	35.0	35.0/(85+x+y)
MgF_2	12.5	12.5/(85+x+y)
CaF_2	12.5	12.5/(85+x+y)
SrF_2	12.5	12.5/(85+x+y)
BaF_2	12.5	12.5/(85+x+y)
YF_3	15.0-x-y	
ErF_3	\boldsymbol{x}	\boldsymbol{x}
YbF_3	y	y

x = 0.5, 1.0, 3.0, 5.0, 7.0, 9.3, 11.9, 14.9, 18.2, 22.5, 26.0, y = 0.5, 1.0, 2.0, 3.0, 5.0, 7.0, 9.3, 10.0, 11.9, 14.9, 18.2, 22.5, 26.0.

The DTA is performed with a Rigaku Thermo Plus TG-DTA TG8110 apparatus under Ar atmosphere at a heating rate of 10 K·min $^{-1}$. Absorption spectra are measured with a SHIMADZU UV-2200 spectrophotometer. The 1.54- $\mu \rm m$ emission spectra are obtained by excitation with a 980 nm InGaAs laser diode. Up-conversion luminescence spectra are measured with a HITACHI F-3010 fluorescence spectrophotometer under the 980 nm excitation. The spectra are recorded in similar experimental conditions, and the relative errors in these spectra measurements are estimated to be $<\pm5\%$. All measurements are carried out at room temperature.

Figure 1 illustrates the observed absorption cross-section of the glasses with the compositions of $35.0 \mathrm{AlF_3 \cdot 12.5 MgF_2 \cdot 12.5 CaF_2 \cdot 12.5 SrF_2 \cdot 12.5 BaF_2 \cdot 10.0 \mathrm{YF_3 \cdot 5.0 ErF_3}$ and $35.0 \mathrm{AlF_3 \cdot 12.5 MgF_2 \cdot 12.5 CaF_2 \cdot 12.5 SrF_2 \cdot 12.5 BaF_2 \cdot 5.0 \mathrm{YF_3 \cdot 5.0 ErF_3 \cdot 5.0 YbF_3}$ in the range of 3500-30000 cm $^{-1}$. The observed spectra consist of thirteen absorption bands from the $^4I_{15/2}$ ground state to the $^4I_{13/2},~^4I_{11/2},~^4I_{9/2},~^4F_{9/2},~^4S_{3/2},~^2H_{11/2},~^4F_{7/2},~^4F_{5/2},~^4F_{3/2},~^2H_{9/2},~^4G_{11/2},~^4G_{9/2},~^4G_{11/2},~^2F_{5/2}$ excited states, respectively. The absorption cross section around 10250 cm $^{-1}$ (980 nm) due to the Yb $^{3+}$: $^2F_{5/2} \leftarrow ^2F_{7/2}$ transition is stronger than that due to the Er $^{3+}$: $^4I_{11/2} \leftarrow ^4I_{15/2}$ transition. The absorption cross section around 980 nm in the Er $^{3+}/\mathrm{Yb}^{3+}$ co-doped glass is 0.75×10^{-20} cm 2 , which is larger than that 0.14×10^{-20} cm 2 in the Er $^{3+}$ singly-doped glass. This indicates that

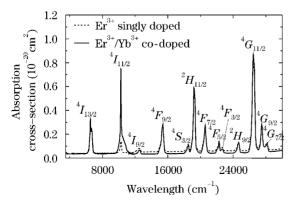


Fig. 1. Calculated absorption cross-section of $\rm Er^{3+}$ single doped and $\rm Er^{3+}/Yb^{3+}$ co-doped AlF₃-based glasses. The concentration of $\rm Er^{3+}$ and $\rm Yb^{3+}$ is 5 mol%, respectively.

the ${\rm Er^{3+}/Yb^{3+}}$ co-doped fluoroal uminate glasses have higher absorption efficiencies than the ${\rm Er^{3+}}$ singly doped glasses under 980-nm excitation and the ${\rm Yb^{3+}}$ ion is particularly suitable in order to efficiently transfer its excitation energy to the ${\rm Er^{3+}}$ ion.

A high power and high efficiency microchip laser requires that the Er³⁺ concentration should be sufficiently high to ensure a net gain with such a thin (several hundred micrometer) active material. Because of the serious clustering and concentration quenching, it is difficult to obtain a high gain at 1.54 µm in a microchip laser based on glasses with a doping of high concentrations of rare earth ions. Since Yb^{3+} has only one excited state of ${}^{2}F_{5/2}$, which locates at about 980 nm above the ground state of ${}^2F_{7/2}$, no concentration quenching occurs among the Yb³⁺ ions. An idea of the use of rare earth co-doping is to take advantage of the fact that Yb³⁺ acts as a sensitizer for Er³⁺. The mechanism has been known from a long time ago^[17]. Figure 2 shows the fluorescence emission spectra of the Er³⁺ singly doped and Er³⁺/Yb³⁺ co-doped fluoroaluminate glasses in the range of 1400-1700 nm under 980-nm excitation. As seen from Fig. 2, the strong Er³⁺: ${}^4I_{13/2} \rightarrow {}^4I_{15/2}$ fluorescence is observed around 1.54 μ m in both Er³⁺ singly doped and $\mathrm{Er^{3+}/Yb^{3+}}$ co-doped glasses, and the 1.54- $\mu\mathrm{m}$ emission intensity increases with increasing Yb3+-addition when the Yb³⁺/Er³⁺ concentration ratio does not exceed 1:1. Therefore, it may be expected to obtain higher gain in the addition of Yb³⁺ ion to the Er³⁺ singly doped fluoroaluminate glasses in this work.

In glasses with low Er^{3+} concentration doping (below 10 mol%), the Er^{3+} : 1.54 $\mu\mathrm{m}$ fluorescence intensity depends upon the Er^{3+} concentration in the Er^{3+} singly doped and $\mathrm{Er}^{3+}/\mathrm{Yb}^{3+}$ co-doped glasses under 980-nm excitation are shown in Fig. 3. In the $\mathrm{Er}^{3+}/\mathrm{Yb}^{3+}$ co-doped glasses the concentration ratio of $\mathrm{Er}^{3+}/\mathrm{Yb}^{3+}$ is 1:1. It can be seen that concentration quenching begins to occur slightly when the Er^{3+} concentration is up to about 5 mol%. However, in both of the Er^{3+} singly doped and $\mathrm{Er}^{3+}/\mathrm{Yb}^{3+}$ co-doped glasses, no concentration quenching is evidently observed even the Er^{3+} concentration reaches about 10 mol%. Wetenkam et al. have reported that concentration quenching easily occurs from the $^4I_{11/2}$

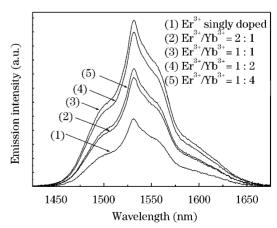


Fig. 2. Fluorescence spectra around 1.54 μ m of Er³⁺ singly doped and Er³⁺/Yb³⁺ co-doped glasses under 980-nm excitation. The Er³⁺ concentration is 10 mol% and the Er³⁺/Yb³⁺ concentration ratio is 0, 2:1, 1:1, 1:2, and 1:4 respectively.

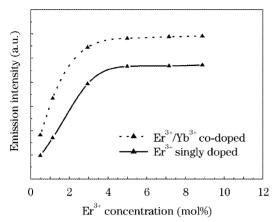


Fig. 3. Dependence of fluorescence intensity at 1.54 μm upon ${\rm Er^{3+}}$ concentration in ${\rm Er^{3+}}$ single doped and ${\rm Er^{3+}/Yb^{3+}}$ co-doped AlF₃-based glasses under 980-nm excitation. The ${\rm Er^{3+}/Yb^{3+}}$ concentration ratio is 1:1.

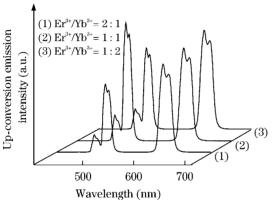


Fig. 4. Dependence of up-conversion luminescence intensity upon ${\rm Er^{3+}/Yb^{3+}}$ concentration ratio in ${\rm Er^{3+}/Yb^{3+}}$ co-doped AlF₃-based glasses. The ${\rm Er^{3+}}$ concentration is 10 mol%.

and $^4I_{13/2}$ levels when the Er³⁺ concentration exceeds 4 mol% in ZBLAN glasses^[18]. The present highly Er³⁺/Yb³⁺ co-doped fluoroaluminate glasses give intense fluorescence efficiency at 1.54 μ m and low concentration quenching. This fact may be considered to be a hopeful host for a 1.54- μ m microchip laser and other optical laser applications.

On the other hand, up-conversion phenomenon takes place in a low phonon energy matrix, and brings some loss mechanisms for the infrared emission. The up-conversion emission spectra of ${\rm Er^{3+}/Yb^{3+}}$ co-doped glasses under 980-nm excitation are shown in Fig. 4. In the glasses the concentration of ${\rm Er^{3+}}$ is fixed to 10 mol% and the concentration ratio of ${\rm Er^{3+}}$ energy levels, the green (around 550 nm) and red (around 660 nm) emission bands correspond to the transitions from the $(^4H_{11/2}, \, ^4S_{3/2})$ and $^4F_{9/2}$ states to the $^4I_{15/2}$ ground state, respectively. The red emission intensity increases while the green emission intensity decreases with an increase in the Yb³⁺ concentration in ${\rm Er^{3+}/Yb^{3+}}$ co-doped glasses.

An energy-transfer mechanism proposed for the ${\rm Er^{3+}/Yb^{3+}}$ co-doped glasses is schematically depicted in Fig. 5. The Yb³⁺ ion has only one excited manifold (${}^2F_{5/2}$ level) located at approximately 10000 cm⁻¹.

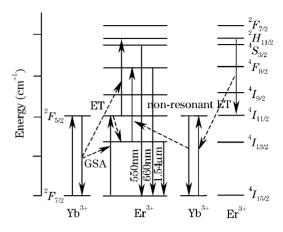


Fig. 5. Schematic diagram of energy transfer between Er³⁺ and Yb³⁺ in Er³⁺/Yb³⁺ co-doped AlF₃-based glasses. The upward and downward arrows indicate photon absorption and fluorescence emission, respectively.

When excitation is performed at the ${}^2F_{7/2}$ level of Yb³⁺ with a diode laser operating at 980 nm, the Yb³⁺ emission band due to the ${}^2F_{5/2} \rightarrow {}^2F_{7/2}$ ransition just overlaps the Er³⁺ absorption band due to the ${}^4I_{11/2} \rightarrow {}^4I_{15/2}$ transition, indicating the energy transfer from Yb³⁺ to Er³⁺ in the glasses.

In the first step of energy-transfer, the excited Yb³⁺ ions transfer their energies to Er^{3+} ions, the 4f electrons that are on the ${}^4I_{15/2}$ ground state are excited to the ${}^4I_{11/2}$ level, and the 1.54- μ m emission is observed due to the ${}^4I_{13/2} \rightarrow {}^4I_{15/2}$ transition after a multi-phonon relaxation process. The 4f-electrons on the ${}^4I_{11/2}$ level reach to the ${}^2H_{11/2}$ level by absorbing another photon due to the ${}^2F_{5/2} \rightarrow {}^2F_{7/2}$ transition. The green and red emissions, which are due to the $({}^2H_{11/2}, {}^4S_{3/2}) \rightarrow {}^4I_{15/2}$ and ${}^4F_{9/2} \rightarrow {}^4I_{15/2}$ transitions, respectively, are observed. In the high ${\rm Er^{3+}/Yb^{3+}}$ dopant values, non-resonant energy-transfer occurs from ${\rm Er^{3+}}$ to ${\rm Yb^{3+}}$ when high population of Er^{3+} ions on the ${}^{2}H_{11/2}$ state occurs at the same time. In this energy-transfer process, Yb³⁺ ions that absorbed the energy from ${\rm Er}^{3+}$ transfer the energies to another neighboring ${\rm Er}^{3+}$ ions that on the $^4I_{13/2}$ level, and then the Er^{3+} ions are excited to the ${}^4F_{9/2}$ level. Since the population on the ${}^4I_{13/2}$ state is reduced, the red emission intensity increases, while the 1.54- μm emission intensity decreases. Therefore, an optimum concentration ratio of Er³⁺/Yb³⁺ is desired for highly Yb³⁺/Er³⁺ doped fluoroaluminate glasses. Based on the present experimental result, the best Er³⁺/Yb³⁺ doping ratio is 1:1 in mol% when the Er³⁺ concentrations is below 10 mol%. Since the concentration quenching due to the back energy-transfer from Er³⁺ to Yb³⁺ rapidly occurs when the Er³⁺ concentration is above 10 mol%, the Yb³⁺ concentration should be lowered to obtain higher 1.54- μ m emission efficiency of Er³⁺.

In addition, an increase of the Yb³⁺ concentration in the low dopant value will result in an increased non-radiative energy-transfer from Yb³⁺ to Er³⁺, improving the Er³⁺: 1.54- μ m emission efficiency. In the high dopant value, however, excessive Yb³⁺ concentration will cause an increase in the back energy-transfer from

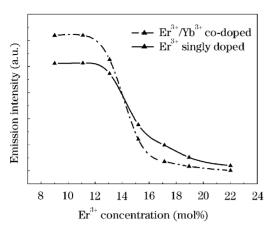


Fig. 6. Dependence of 1.54- μm fluorescence intensity upon ${\rm Er}^{3+}$ concentration in ${\rm Er}^{3+}/{\rm Yb}^{3+}$ co-doped AlF₃-based glasses with high dopant contents. The ${\rm Er}^{3+}/{\rm Yb}^{3+}$ concentration ratio is 1:1.

 ${\rm Er^{3+}}$ to ${\rm Yb^{3+}}$. It can be found that the fluorescence intensity of ${\rm Er^{3+}/Yb^{3+}}$ co-doped glasses decreases very faster than that of ${\rm Er^{3+}}$ singly doped glasses when the ${\rm Er^{3+}}$ concentration exceeds 10 mol%, as shown in Fig. 6. In highly ${\rm Er^{3+}}$ singly doped glasses, the decrease is due to cross relaxation between two neighboring ${\rm Er^{3+}}$ ions. In highly ${\rm Er^{3+}/Yb^{3+}}$ co-doped glasses, the decrease in ${\rm Er^{3+}}$ emissions including 1.54-mm emission, the green and red up-conversion luminescence indicates that excitation energies are transferred from ${\rm Er^{3+}}$ to ${\rm Yb^{3+}}$. The rate of energy transfer by a dipole-dipole interaction is obtained by the Dexter equation [19] described as follows

$$P_{\rm SA} = \frac{3\eta c^2 Q_{\rm A} Q_{\rm S}}{4\pi^3 n^2 R^6} \int \frac{f_{\rm S}(E) f_{\rm A}(E)}{E^2} dE, \tag{1}$$

where n is the refractive index, R is the average distance between the sensitizer and activator, $Q_{\rm A}$ and $Q_{\rm S}$ are the integrated absorption and emission cross sections of activator and sensitizer, respectively, and $f_{\rm A}$ and $f_{\rm S}$ are the normalized line shape functions of the absorption and emission spectra of the same ions. In high ${\rm Er}^{3+}$ and ${\rm Yb}^{3+}$ dopant contents, as can be seen from Fig. 6, the back energy-transfer process becomes more significant since the distance R between ${\rm Er}^{3+}$ and ${\rm Yb}^{3+}$ becomes closer. This leads to a situation that the 1.54- μ m emission intensity becomes much weaker in highly ${\rm Er}^{3+}/{\rm Yb}^{3+}$ co-doped glasses than in ${\rm Er}^{3+}$ singly doped glasses.

In conclusion, the effects of $\mathrm{Er^{3+}/Yb^{3+}}$ concentration quenching on the spectroscopic properties are investigated in the highly $\mathrm{Er^{3+}/Yb^{3+}}$ co-doped fluoroaluminate glasses by the 980-nm excitation. Strong 1.54- μ m emission is observed in both of the $\mathrm{Er^{3+}}$ singly doped and $\mathrm{Er^{3+}/Yb^{3+}}$ co-doped glasses, and no concentration quenching is obviously observed even the $\mathrm{Er^{3+}}$ concentration reaches about 10 mol%.

In the glasses with Er³+ concentrations below 10 mol%, concentration quenching is low and the Er³+/Yb³+ co-doped fluoroaluminate glasses have high quantum efficiency and strong fluorescence at 1.54 μ m which corresponds to the Er³+: ${}^4I_{13/2} \rightarrow {}^4I_{15/2}$ transition than

that of Er³⁺ singly-doped glasses.

In the glasses with ${\rm Er}^{3+}$ concentration above 10 mol%, concentration quenching of 1.54 $\mu{\rm m}$ occurs more obviously than that of the ${\rm Er}^{3+}$ singly-doped samples as a result of the back energy-transfer from ${\rm Er}^{3+}$ to ${\rm Yb}^{3+}$ and higher probabilities of the cross relaxation between ${\rm Er}^{3+}$ ions. Consequently the fluorescence intensity at 1.54 $\mu{\rm m}$ decreases, while the red up-conversion emission intensity increases and the green upconversion emission intensity decreases. To obtain the highest emission efficiency at 1.54 $\mu{\rm m}$, the best doping-concentration ratio ${\rm Er}^{3+}/{\rm Yb}^{3+}$ is found to be approximately 1:1 in mol fraction when the ${\rm Er}^{3+}$ concentration is less than 10 mol%. The glasses presented here are considered to be an excellent candidate for the use as compact optically pumped eye-safe microchip lasers.

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References

- D. R. MacFarlane, J. Javorniczky, P. J. Newman, V. Bogdanov, D. J. Booth, and W. E. K. Gibbs, J. Non-Cryst. Solids 213&214, 158 (1997).
- M. Qiu, J. B. David, W. B. Gregory, and C. B. Glenn, Appl. Opt. 32, 2085 (1993).
- T. Taira, A. Mukai, Y. Nozawa, and T. Kobayashi, Opt. Lett. 16, 1955 (1991).
- 4. F. Lin, H. Hu, G. Yi, and J. Feng, in *Proceeding of 8th International Symposium on Non-Oxide Glass* 364 (1992).
- P. Laporta, S. Taccheo, S. Longhi, and O. Sevlto, Opt. Lett. 18, 1232 (1993).
- 6. F. Gan, J. Non-Cryst. Solids 184, 9 (1995).
- 7. D. C. Hanna and A. C. Troppier, in *Optical Fibers Lasers* and *Amplifiers P. W. France and Blackie (eds.) (CRC Press, London, 1991) p. 164.*
- 8. W. J. Miniscalo, J. Lightwave Technol. 9, 234 (1991).
- V. K. Bogdanow, W. E. K. Gibbs, D. J. Booth, J. S. Javorniczky, P. J. Newman, and D. R. Macfarlane, Opt. Commun. 132, 73 (1996).
- X. Zuo and T. Izumitani, J. Non-Cryst. Solids 162, 68 (1993).
- M. Tsuda, K. Goga, H. Inoue, S. Inoue, and A. Makishima, J. Appl. Phys. 86, 6143 (1999).
- K. Soga, M. Tsuda, and S. Sakuragi, J. Non-Cryst. Solids 222, 272 (1997).
- L. Zhang, H. Hu, and F. Lin, Mater. Lett. 47, 189 (2001).
- G. H. Frischat, B. Hueber, and B. Rahmdohr, J. Non-Cryst. Solids 284, 105 (2001).
- 15. R. S. Quimby, Electron. Lett. 23, 32 (1987).
- 16. D. S. Snmida and T. Y. Fan, Opt. Lett. 19, 1343 (1994).
- 17. F. E. Auzel, Proc. IEEE 61, 758 (1973).
- L. Wetenkam, G. F. West, and H. Tobben, J. Non-Cryst. Solids 140, 30 (1992).
- 19. D. L. Dexter, J. Chem. Phys. 21, 836 (1953).